



Hydrogen and oxygen isotope compositions of lake water and evaporation

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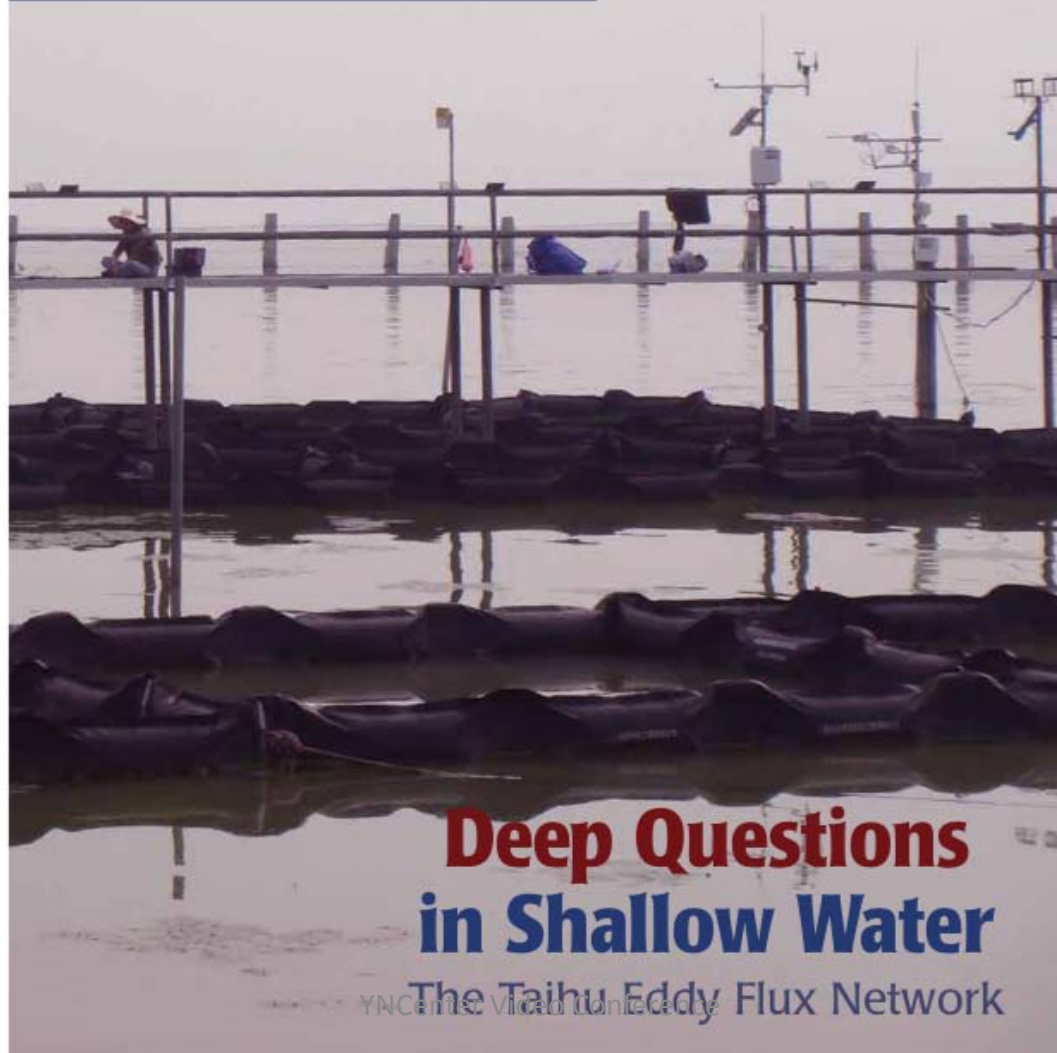
BAMS

Bulletin of the American Meteorological Society

MOORE EFS TORNADO ANALYZED

FIELD WORK FOR UNDERGRADUATES

LAND-CHANGE EFFECTS ON CLIMATE



Deep Questions in Shallow Water

The Taihu Eddy Flux Network

23 April 2015

YN Center Virtual Conference

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Outline

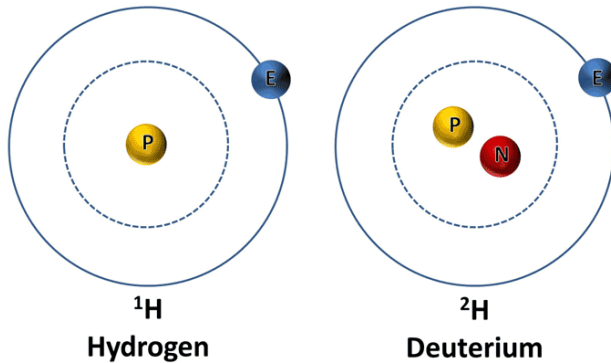
- Background information
- Lake water isotope
 - Lake and river survey
 - Spatial patterns and seasonality
- Isotopic lake evaporation
 - Craig-Gorden model
 - In-situ measurement
 - Model validation
- Isotopic mass balance method
 - Theory
 - Results

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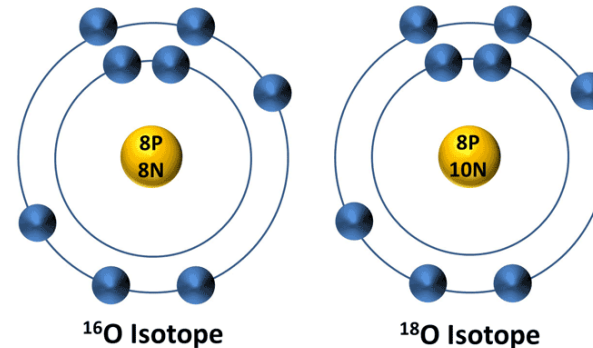
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Isotopes in water

Hydrogen Isotopes



Oxygen Isotopes



Vienna Standard Mean Ocean Water (VSMOW)

$^2\text{H}/^1\text{H} = 155.76 \pm 0.1 \text{ ppm}$ (a ratio of 1 part per approximately 6420 parts)

$^{18}\text{O}/^{16}\text{O} = 2005.20 \pm 0.43 \text{ ppm}$ (a ratio of 1 part per approximately 498.7 parts)

$$\delta = \left(\frac{R_{\text{sample}}}{R_{\text{standard}}} - 1 \right) \times 1000, \text{ ‰}$$

Global Meteoric Water Line

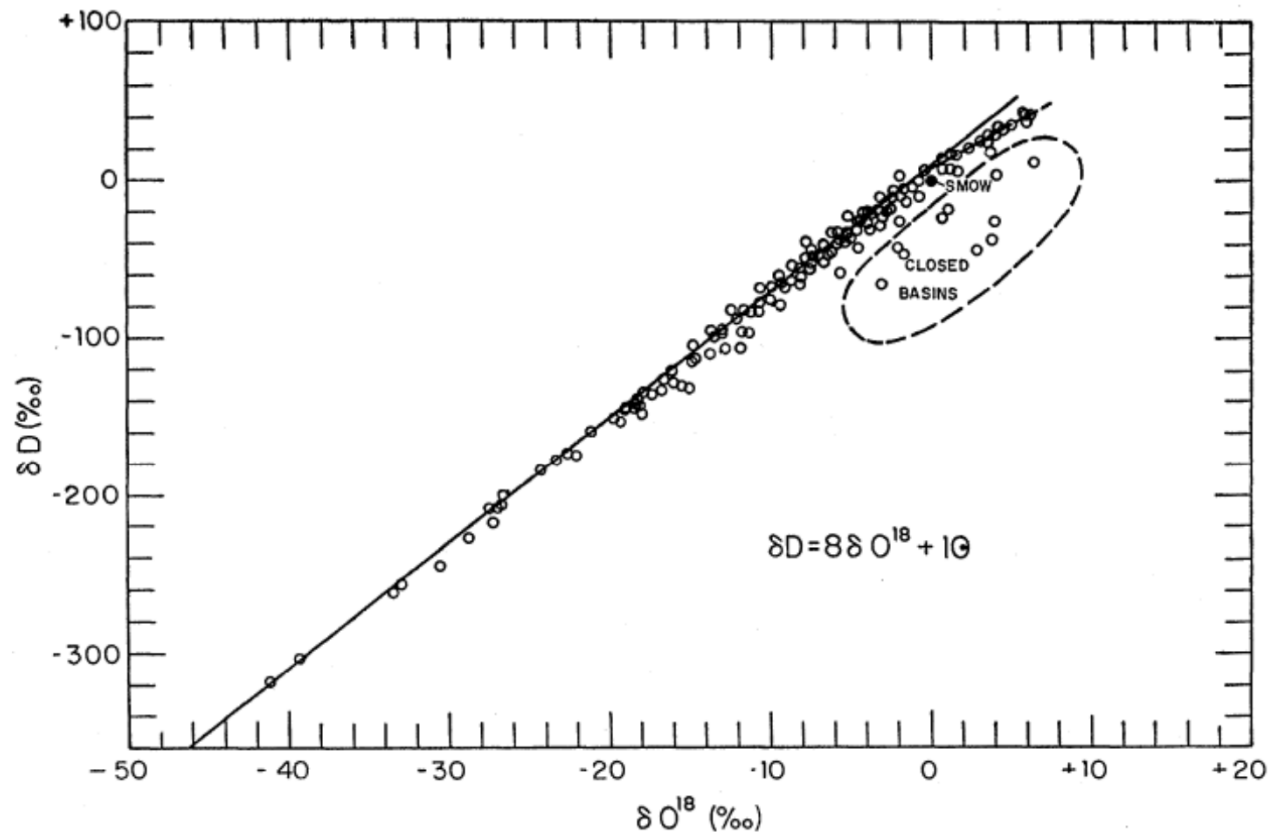
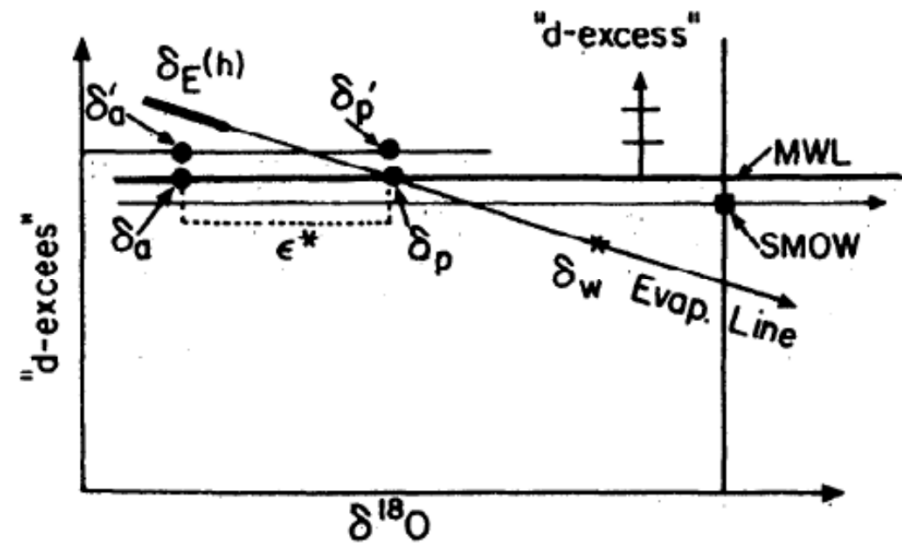
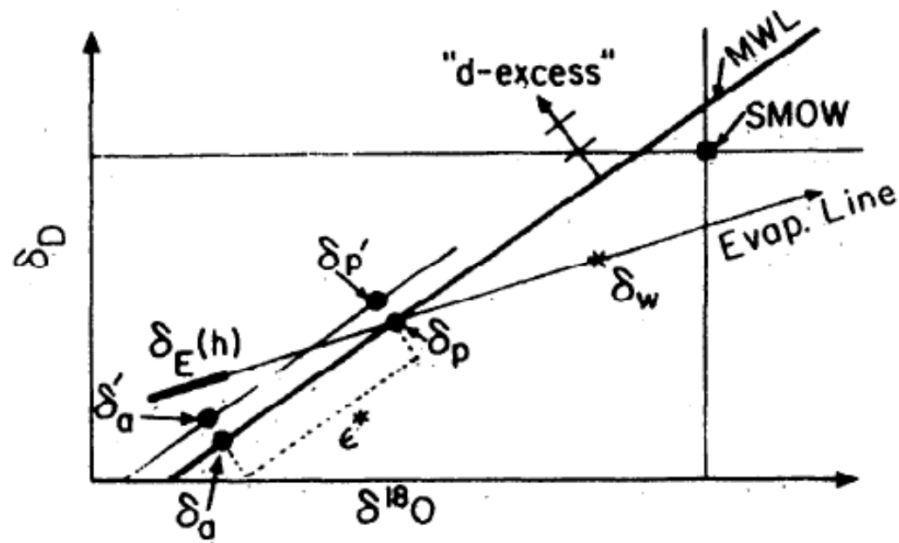


Fig. 1. Deuterium and oxygen-18 variations in rivers, lakes, rain, and snow, expressed as per millage enrichments relative to "standard mean ocean water" (SMOW). Points which fit the dashed line at upper end of the curve are rivers and lakes from East Africa.

400 samples of water from rivers, lakes, and precipitation.

Deuterium-excess (过量氘)

$$d = \delta D - 8 \delta^{18}O$$



Rainout: invariant with respect to the *d-excess*.

Transpiration: no change in the *d-excess*.

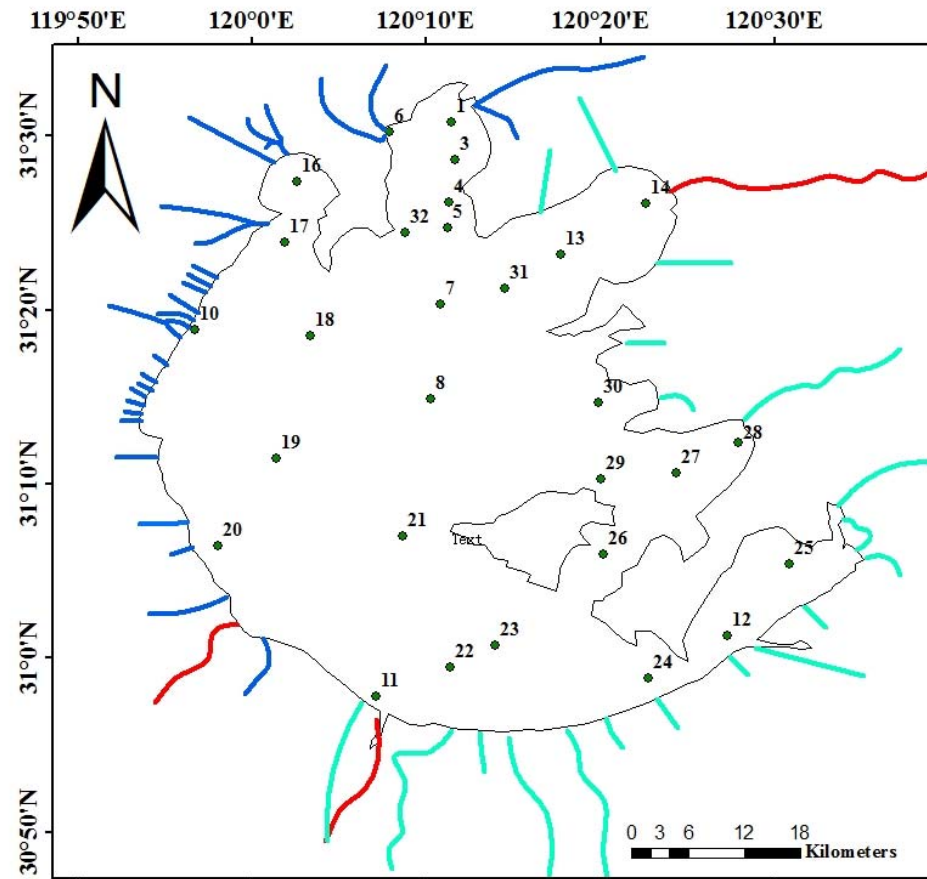
Evaporation: The evaporated waters usually have a higher *deuterium-excess* value.

(Dansgaard 1964; Gat et al. 1994)

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Lake and river surveys



Dots: lake survey sites Blue: inflow rivers
Green: outflow rivers Red: inflow/outflow rivers

Whole-lake survey:

29 sites

Since August 2011

Seasonally (Feb, May,
Aug, Nov)

River survey:

51 rivers

27 inflow rivers

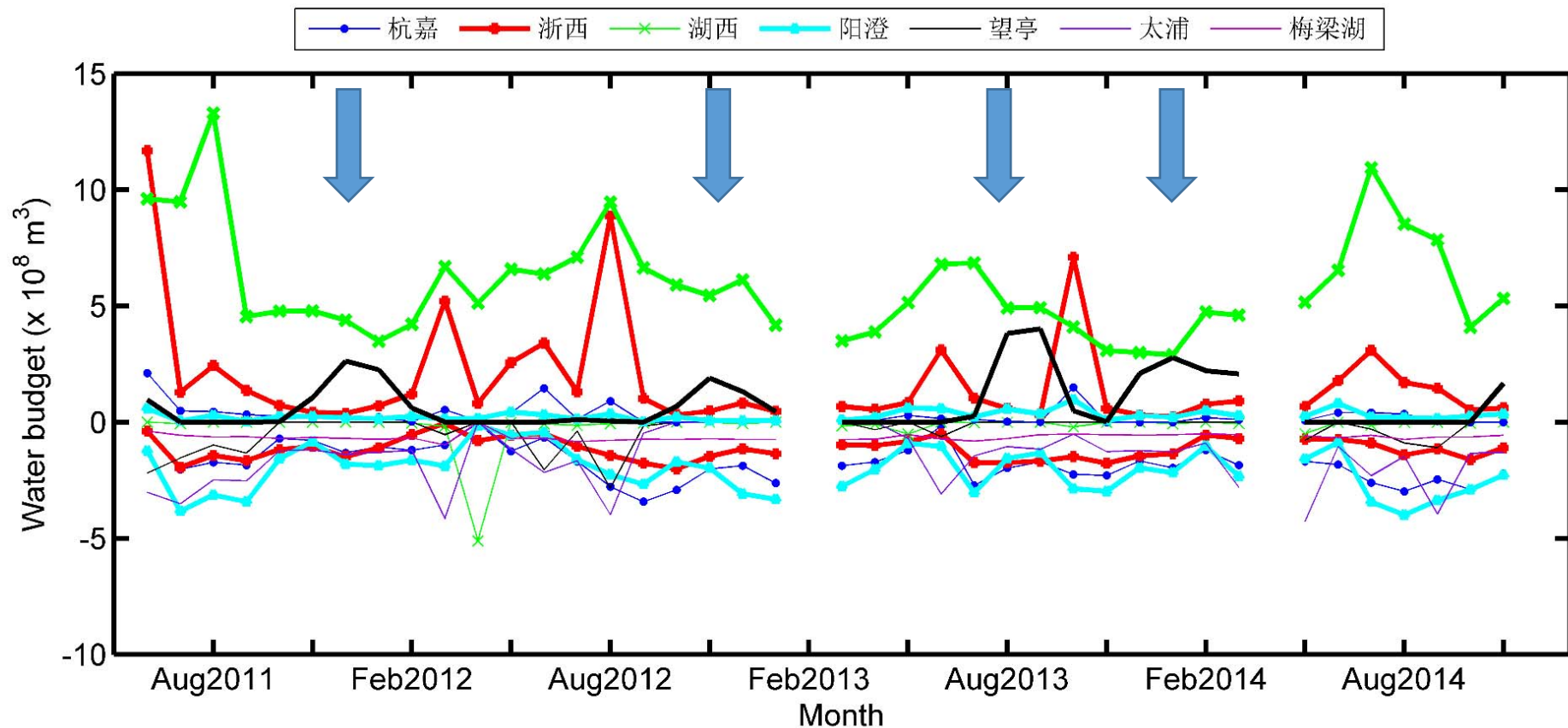
21 outflow rivers

3 inflow/outflow rivers

Since May 2013

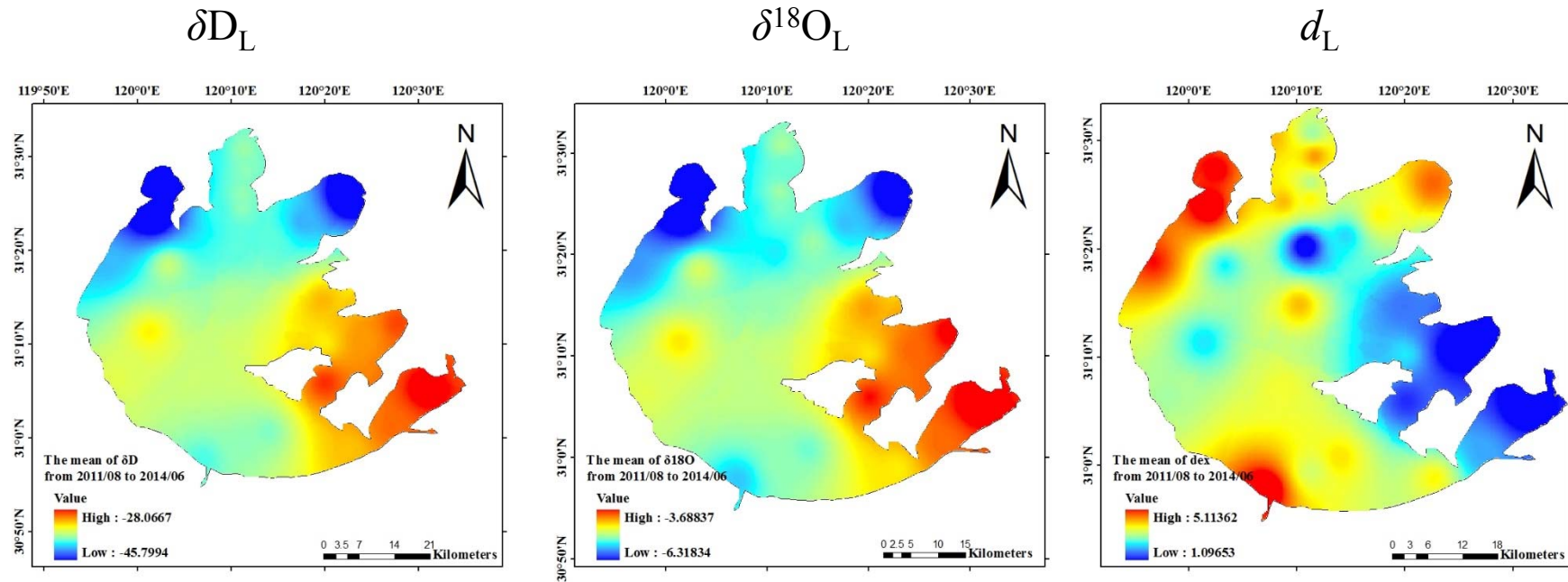
Seasonally (Feb, May,
Aug, Nov)

Inflow and outflow water budget of Lake Taihu



Water diversion from Yangze river to Lake Taihu (引江济太)

Seasonal mean spatial patterns of the lake water isotope

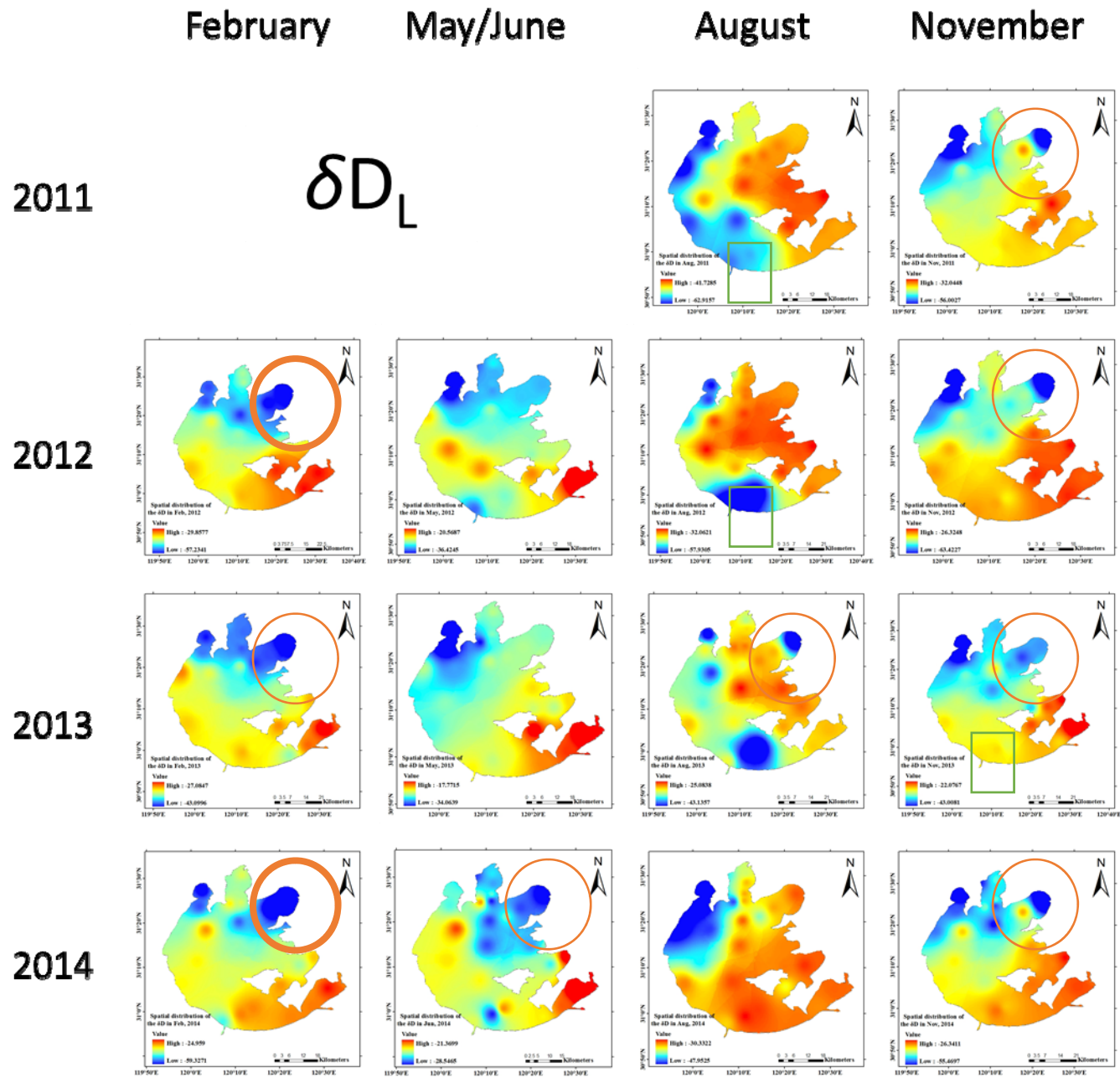


Inflow region: lower δD_L and $\delta^{18}O_L$, higher d_L

Outflow region: higher δD_L and $\delta^{18}O_L$, lower d_L

water in the outflow region: stayed in the lake, underwent more evaporation, so d became lower.

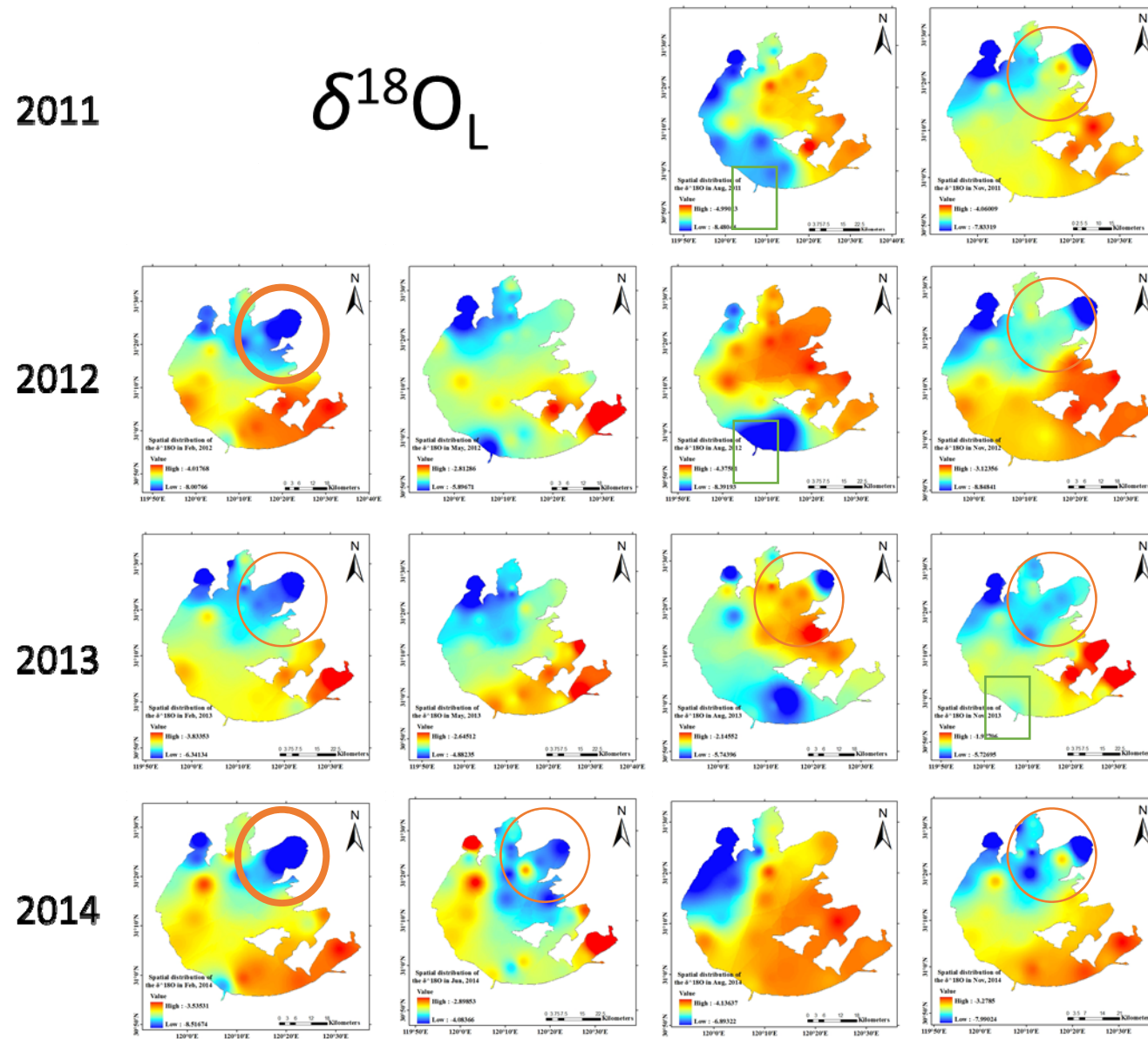
Note: Mean value of 12 seasonal lake surveys (Aug 2011 to Jun 2014)



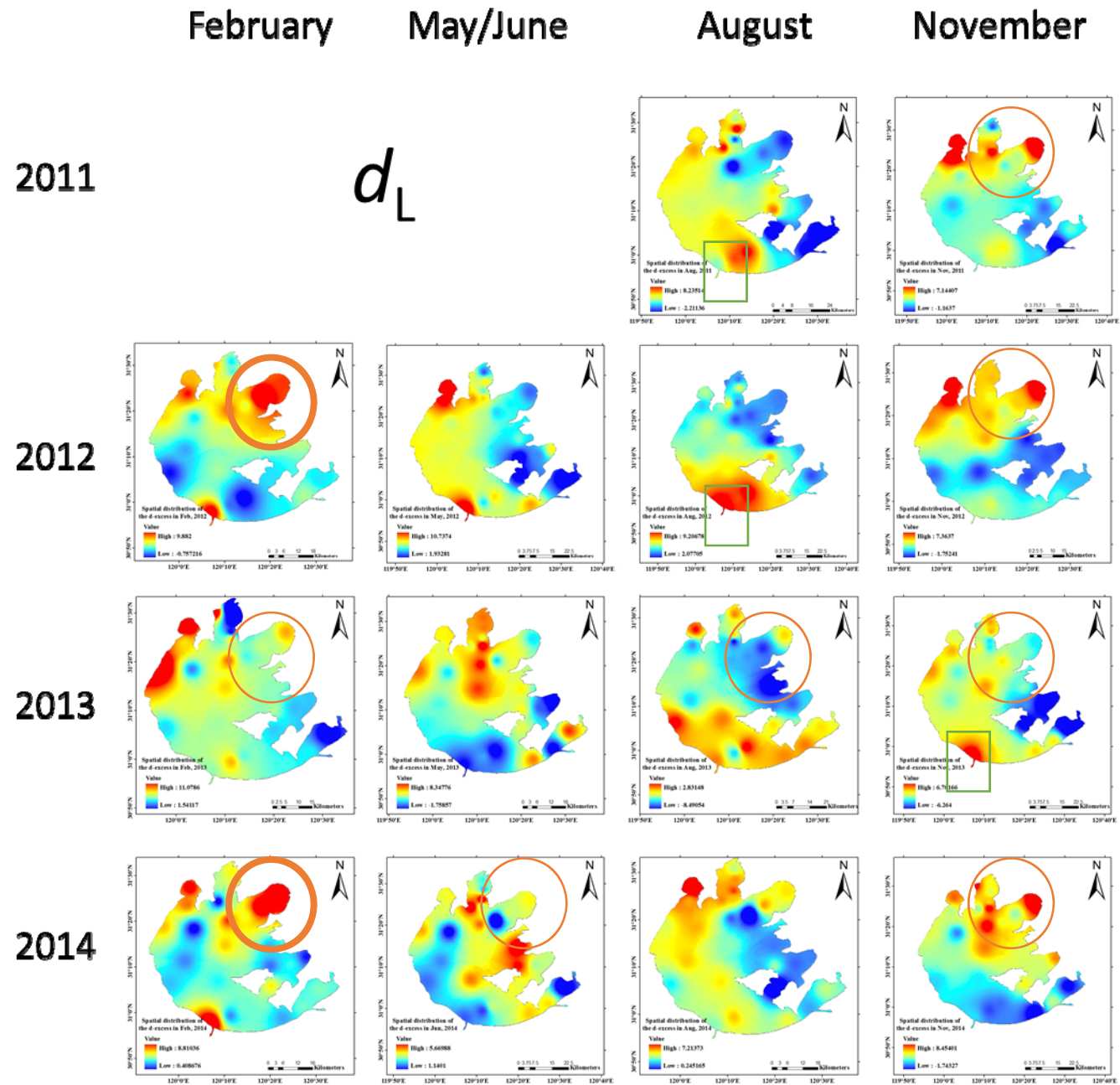
Note: circle – inflow from Wangyu river; square – inflow from Hangjia lake region

February May/June August November

2011 $\delta^{18}\text{O}_L$

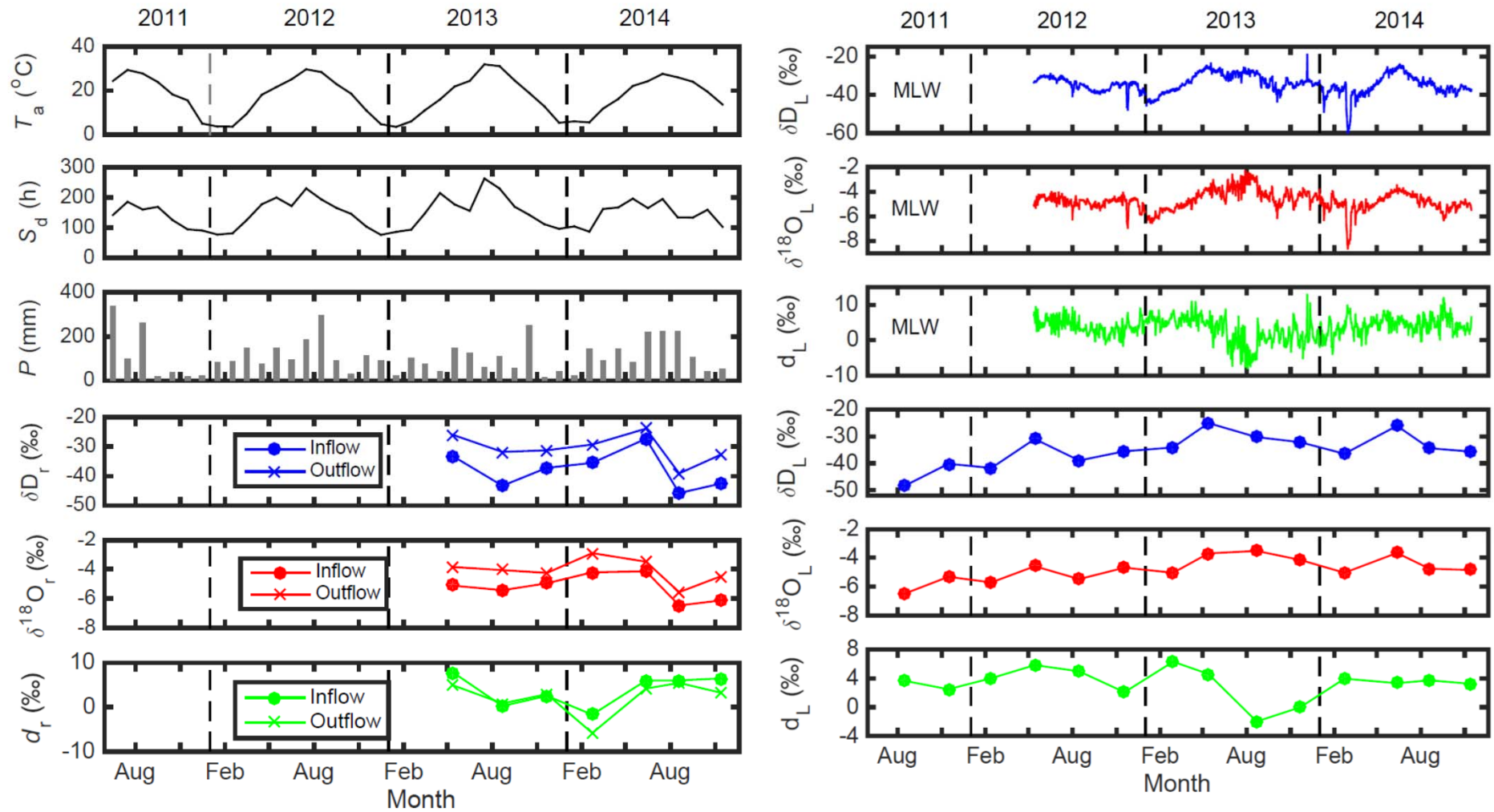


Note: circle – inflow from Wangyu river; square – inflow from Hangjia lake region

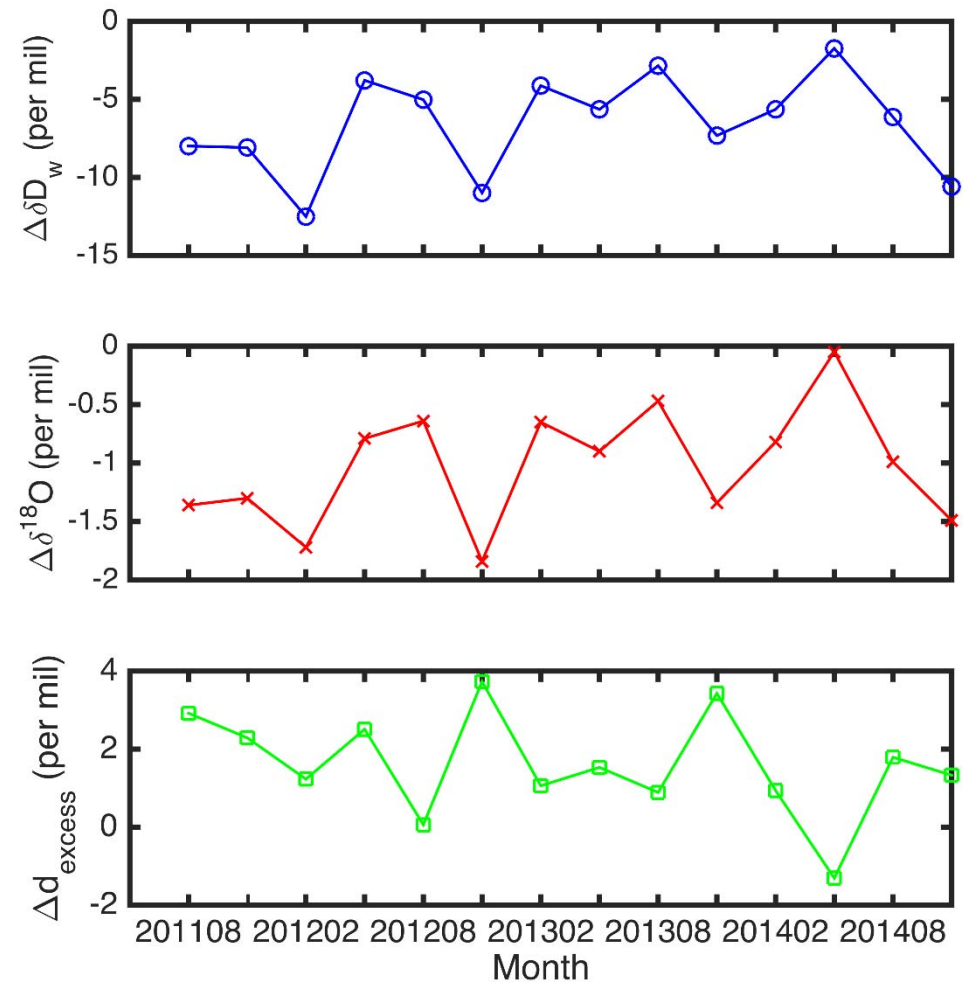
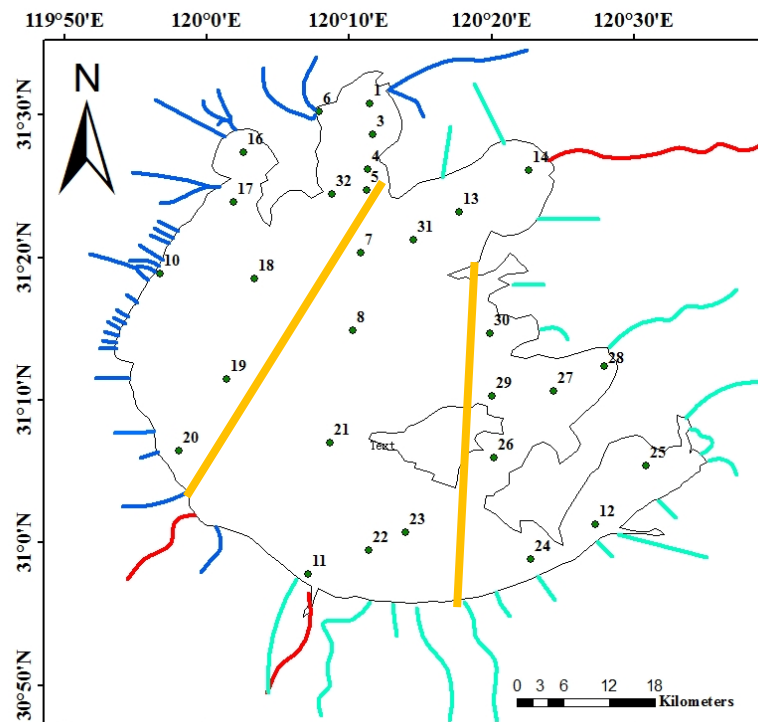


Note: circle – inflow from Wangyu river; square – inflow from Hangjia lake region

Seasonality of meteorological variables, lake and river water isotopes



Difference of lake water isotope between inflow and outflow regions

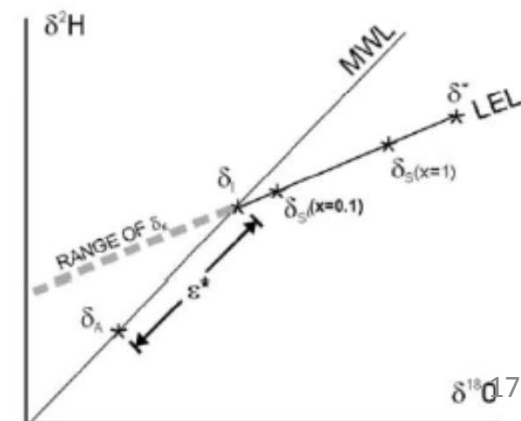
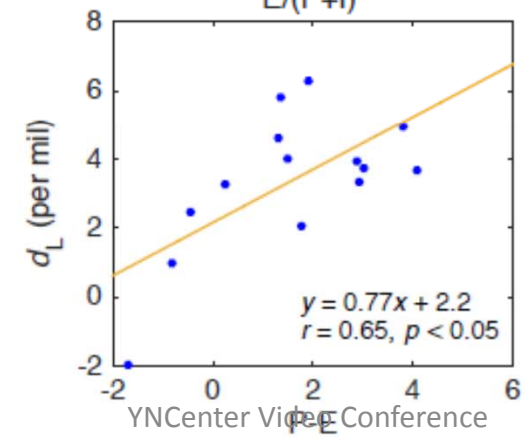
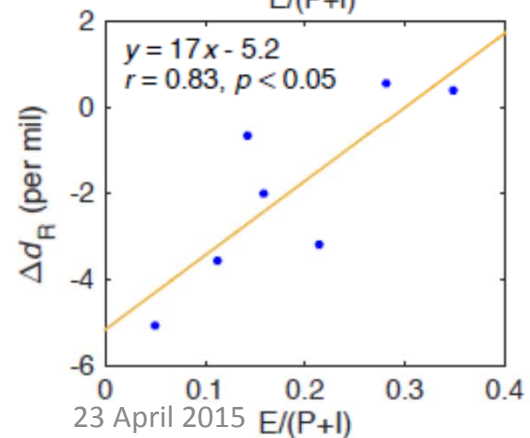
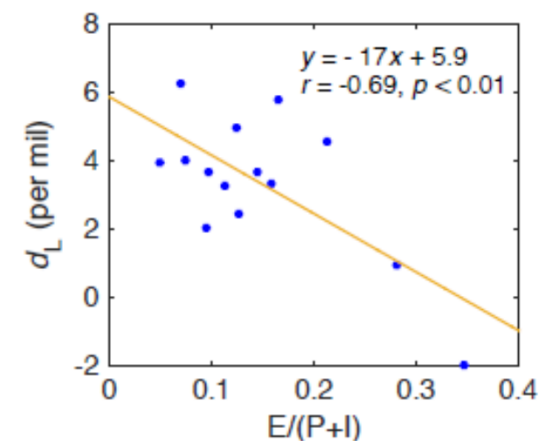
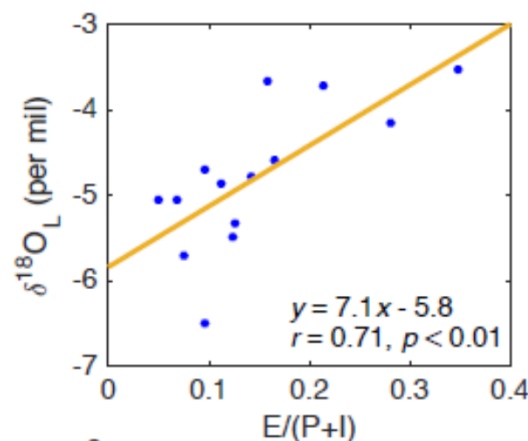
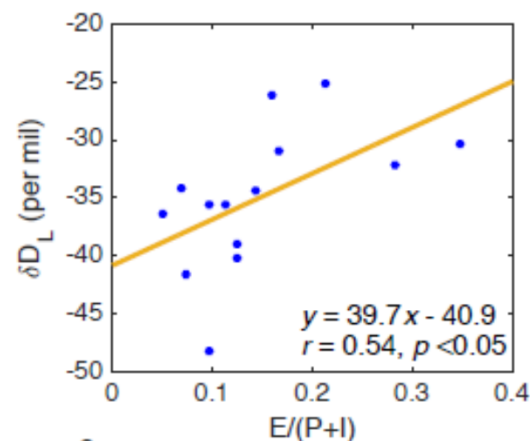


- The Gradients of δD and $\delta^{18}O$ were low in warm seasons and high in cold seasons.
- d-excess gradient is high in cold season is high low in warm season.

Lake and river water isotope versus P-E, E/(P+I), and depth

	whole-lake water			lake outflow region - inflow region			river outflow-inflow		
r	δD_L	$\delta^{18}O_L$	d_L	$\Delta\delta D_L$	$\Delta\delta^{18}O_L$	Δd_L	$\Delta\delta D_R$	$\Delta\delta^{18}O_R$	Δd_R
P-E	-0.32	-0.50	0.65*	-0.08	-0.15	0.25	-0.69	-0.27	-0.54
E/(P+I)	0.54*	0.71**	-0.69**	-0.40	-0.30	-0.05	0.33	-0.21	0.83*
depth	-0.40	-0.42	0.16	0.02	0.06	-0.12	-0.22	-0.47	0.48

$x = E/(P+I)$ throughflow index, i.e. the fraction of total water inputs lost by evaporation.



23 April 2015

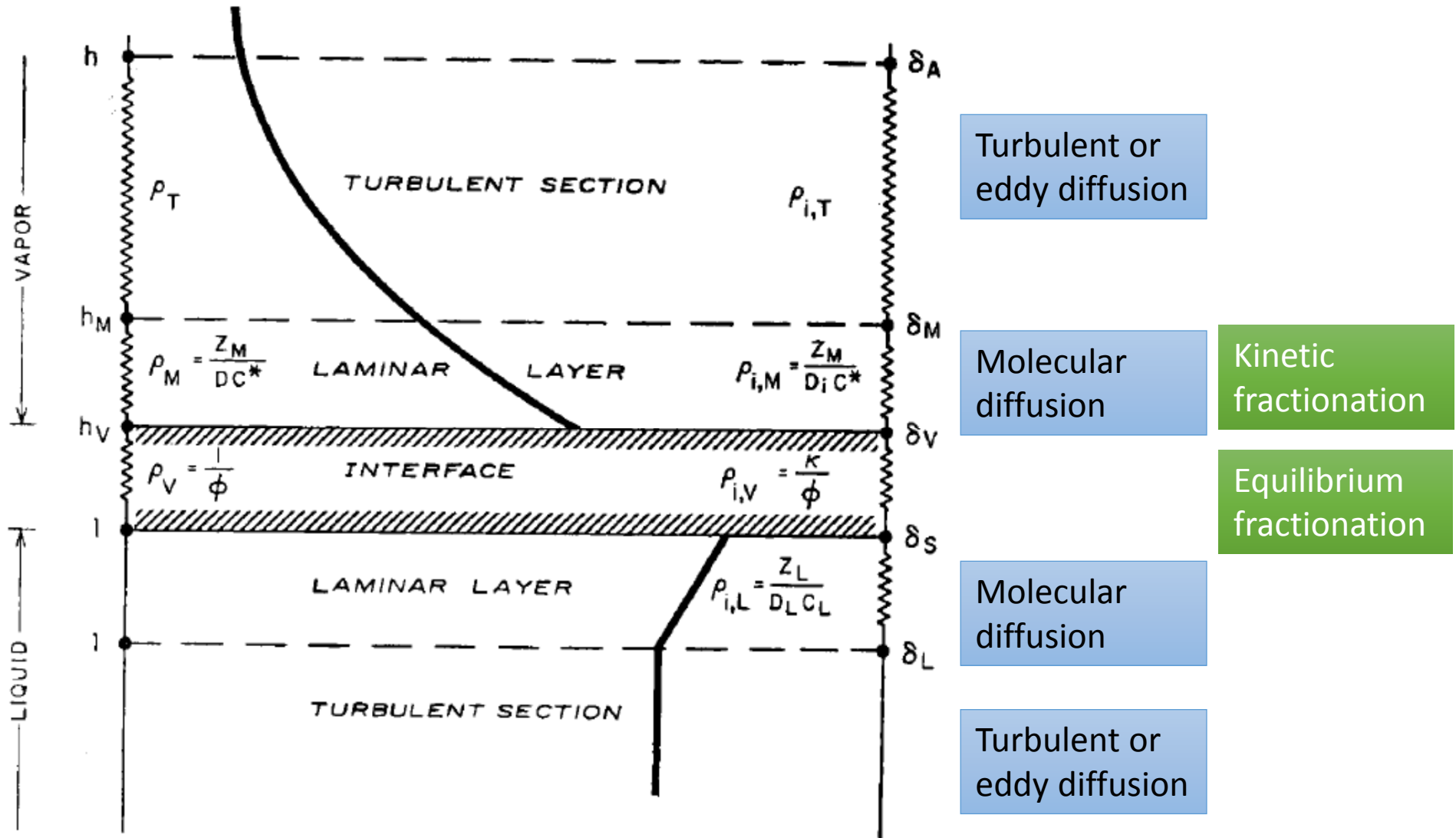
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$\delta^{18}O$

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A laminar layer model for an isolated liquid



Equilibrium fractionation effect

The fractionation factor between liquid (or solid) and vapor at equilibrium.

$$\alpha_{eq} = \left(\frac{R_{liquid}}{R_{vapor}} \right)_{eq} = \frac{p_{H_2O}^{16}}{p_i} = 1 + \varepsilon_{eq}$$

p_i : saturation vapor pressure of HDO or $H_2^{18}O$

$$\alpha_{eq,O} = \exp \left(\frac{1.137 \times 10^3}{T_s^2} - \frac{0.4156}{T_s} - 2.0667 \times 10^{-3} \right)$$

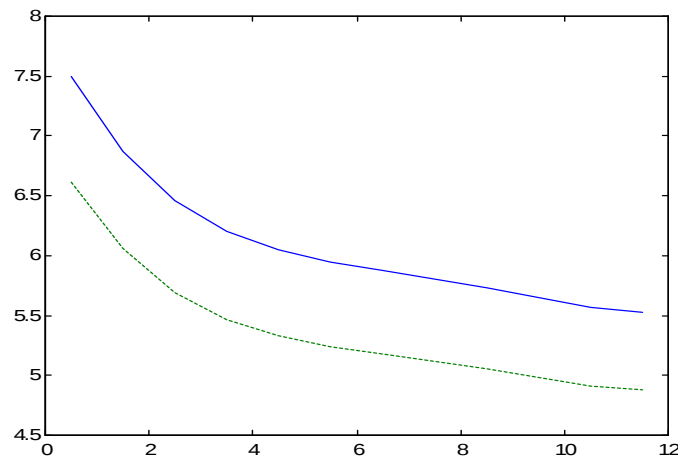
$$\alpha_{eq,D} = \exp \left(\frac{24.844 \times 10^3}{T_s^2} - \frac{76.248}{T_s} + 52.612 \times 10^{-3} \right)$$

(Majoube 1971)

Kinetic fractionation effect

Due to different molecular diffusion rate of the heavier (HDO and H_2^{18}O) molecules and the lighter (H_2^{16}O) molecules at the air-liquid interface.

The determination of ε_k requires the characterization of the degree of molecular and turbulent diffusion.



Regression fit to the kinetic fractionation factors produced by the Merlivat and Jouzel (1979) smooth regime model for evaporation from a water surface.

$$\varepsilon_{k,O} = 4.6351u^4 \times 10^{-4} - 0.01465u^3 + 0.1696u^2 - 0.9261u + 7.9230$$

$$\varepsilon_{k,D} = 4.0917u^4 \times 10^{-4} - 0.01293u^3 + 0.1497u^2 - 0.8174u + 6.9882$$

(Merlivat and Jouzel, 1979)

Craig-Gordon model:

$$\delta_E = \frac{\alpha_{eq}\delta_L - h\delta_a - \varepsilon_{eq} - (1 - h)\varepsilon_k}{(1 - h) + (1 - h)\varepsilon_k \times 10^{-3}}$$

?



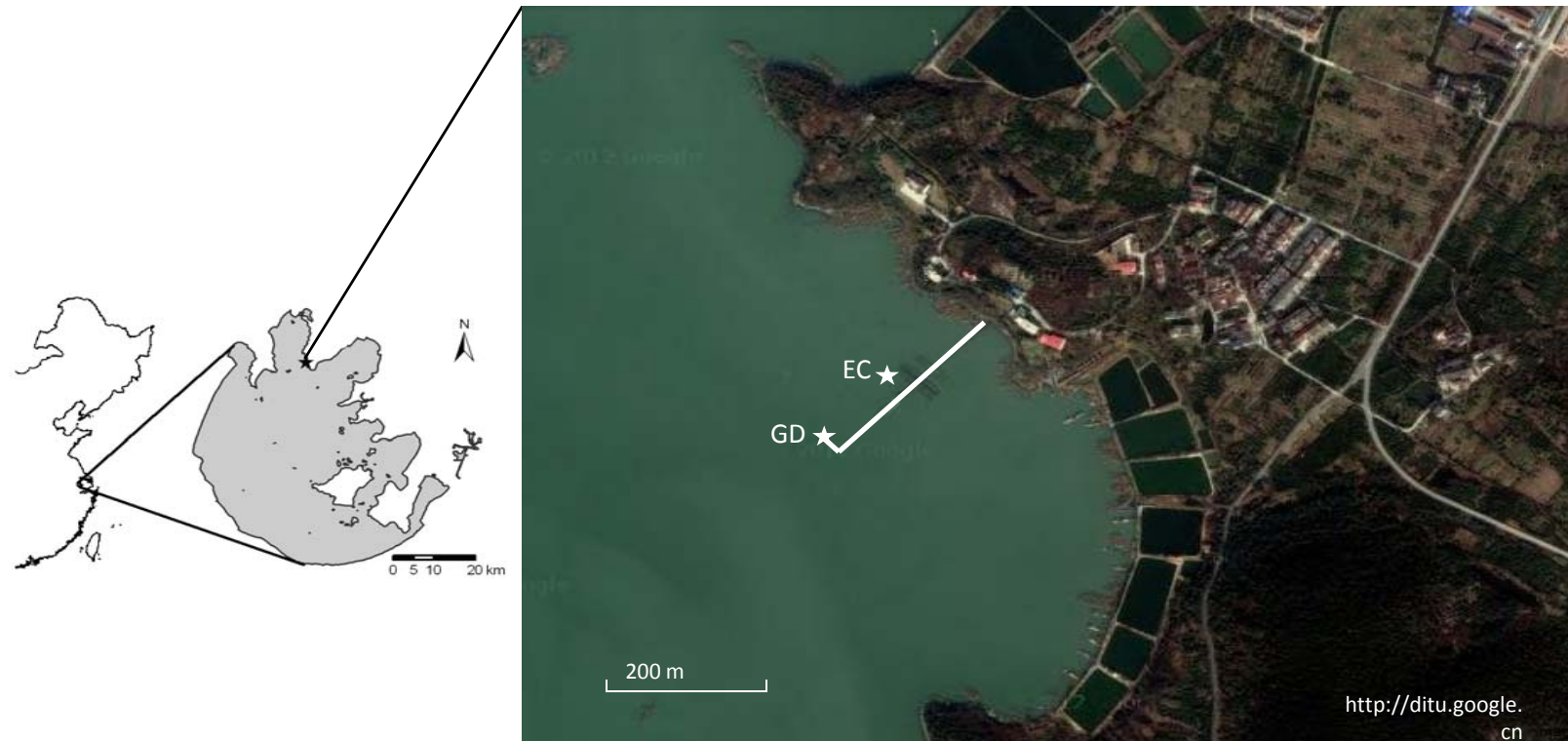
δ_E : isotopic composition of evaporation
 δ_L : isotopic composition of lake water
 δ_a : isotopic composition of atmospheric vapour

?



h : relative humidity reference to water surface temperature
 ε_k : kinetic fractionation factor
 $\varepsilon_{eq}, \alpha_{eq}$: equilibrium fractionation factors

In-situ measurement of isotopic water vapor and evaporation



The experiment site ($31^{\circ}24'N$, $120^{\circ}13'E$) was in the north part of Lake Taihu, which is the third largest freshwater lake in China, with a water surface area of 2400 km^2 and a mean water depth of 1.9 m

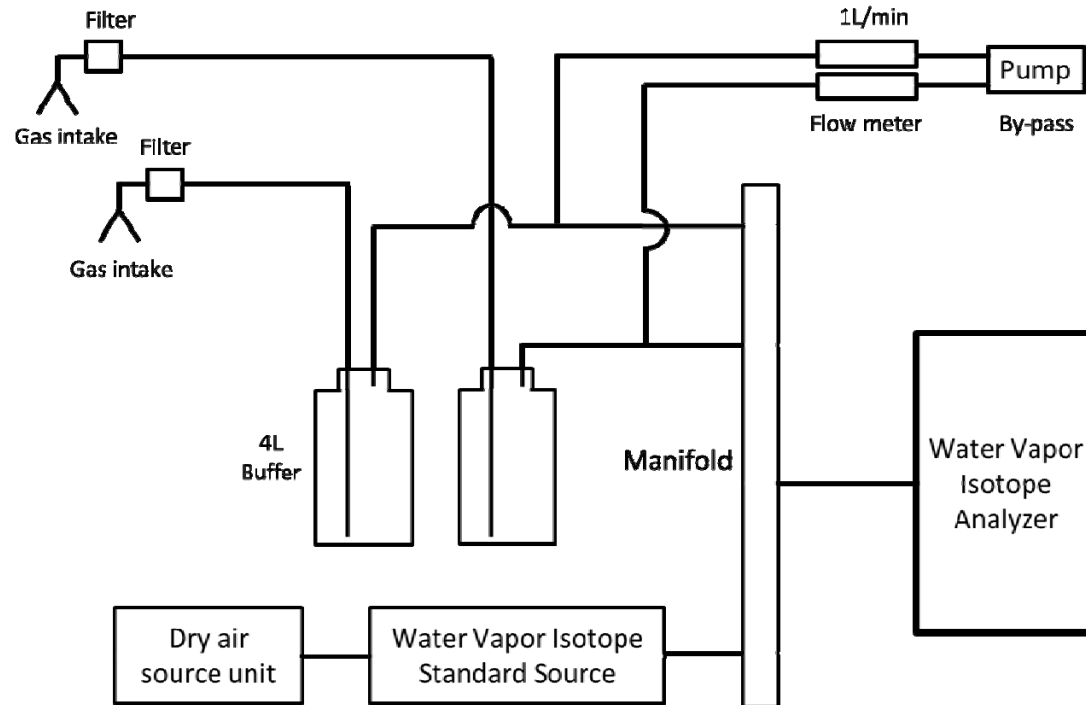
Instrument



- The key instrument was a water vapor analyzer based on the off-axis integrated cavity output spectroscopy.
- The analyzer switched between the two intakes at the 1.1 and 3.5 m height above water surface every 30s, measuring the H_2^{16}O , HDO and H_2^{18}O water vapor mixing ratios.



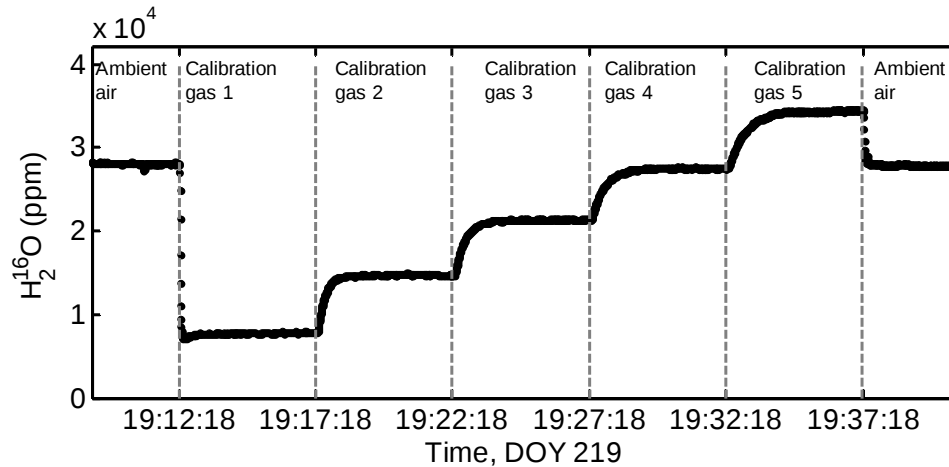
Schematic Design Diagram



The flux-gradient method was used to obtain the isotopic compositions of lake evaporation. Buffer volumes were used to improve the accuracy of the gradient measurement. Small short tubing was used between the manifold and the analyzer to minimize the transient time between valve switching.

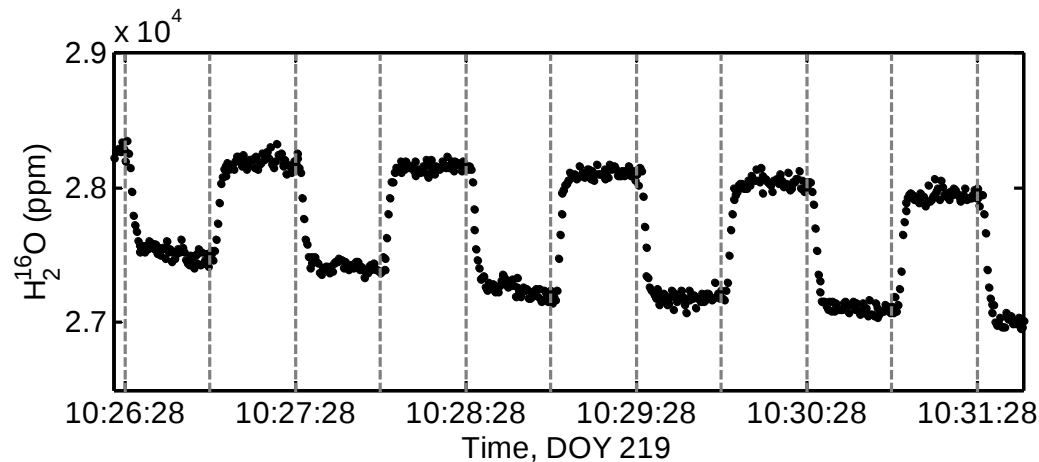
Instrument Performance (1/2)

Calibration gases:



To eliminate the effect of non-linearity and signal drift, we calibrated the analyzer every 3 h against 5 water vapor standards of identical isotopic compositions.

Ambient air:



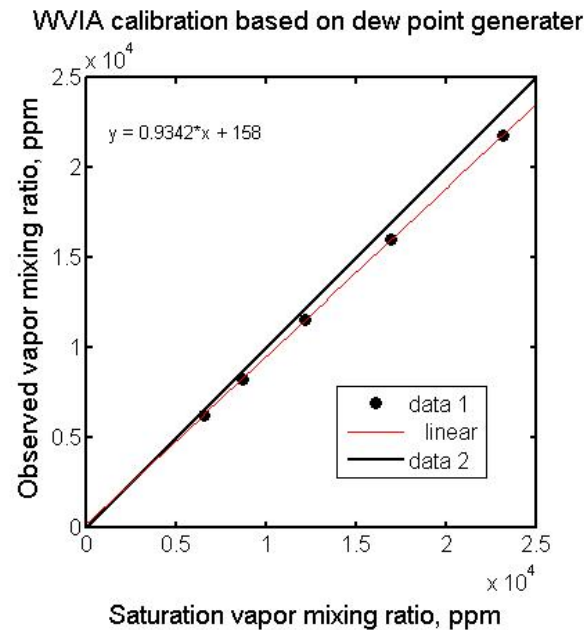
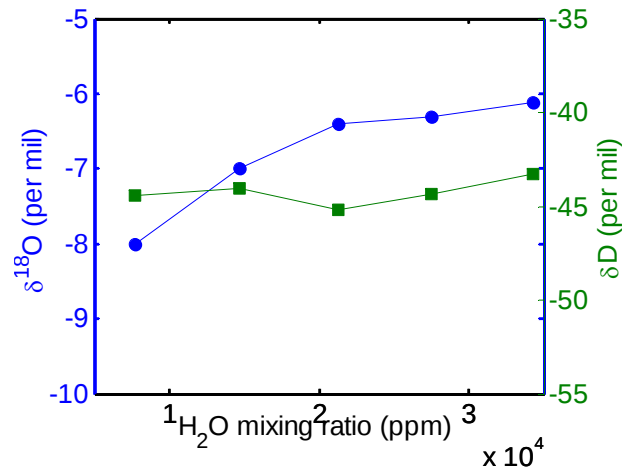
When measuring the ambient air, the manifold switched between the two intakes every 30 s.

The measurement approached steady state in less than 10 s after each switching.

Instrument Performance (2/2)

Non-linearity & calibration

The analyzer displayed nonlinear behavior. The measured $\delta^{18}\text{O}$ and δD of the calibration gases ranged from -8.0 to -6.1‰ and -45.2 to -43.3‰, respectively. The true values were -7.0‰ and -44.0‰, respectively.



Calibration methods

Step 1: calibrate the ambient air using calibration gas 1 & 2

$$R_1 = R_c \cdot \frac{x_{s,1}}{x'_{s,1}} \cdot \frac{x'_a}{x_a} \quad \delta_1 = (R_1 / R_{\text{VSMOW}} - 1) \times 1000$$
$$R_2 = R_c \cdot \frac{x_{s,2}}{x'_{s,2}} \cdot \frac{x'_a}{x_a} \quad \delta_2 = (R_2 / R_{\text{VSMOW}} - 1) \times 1000$$

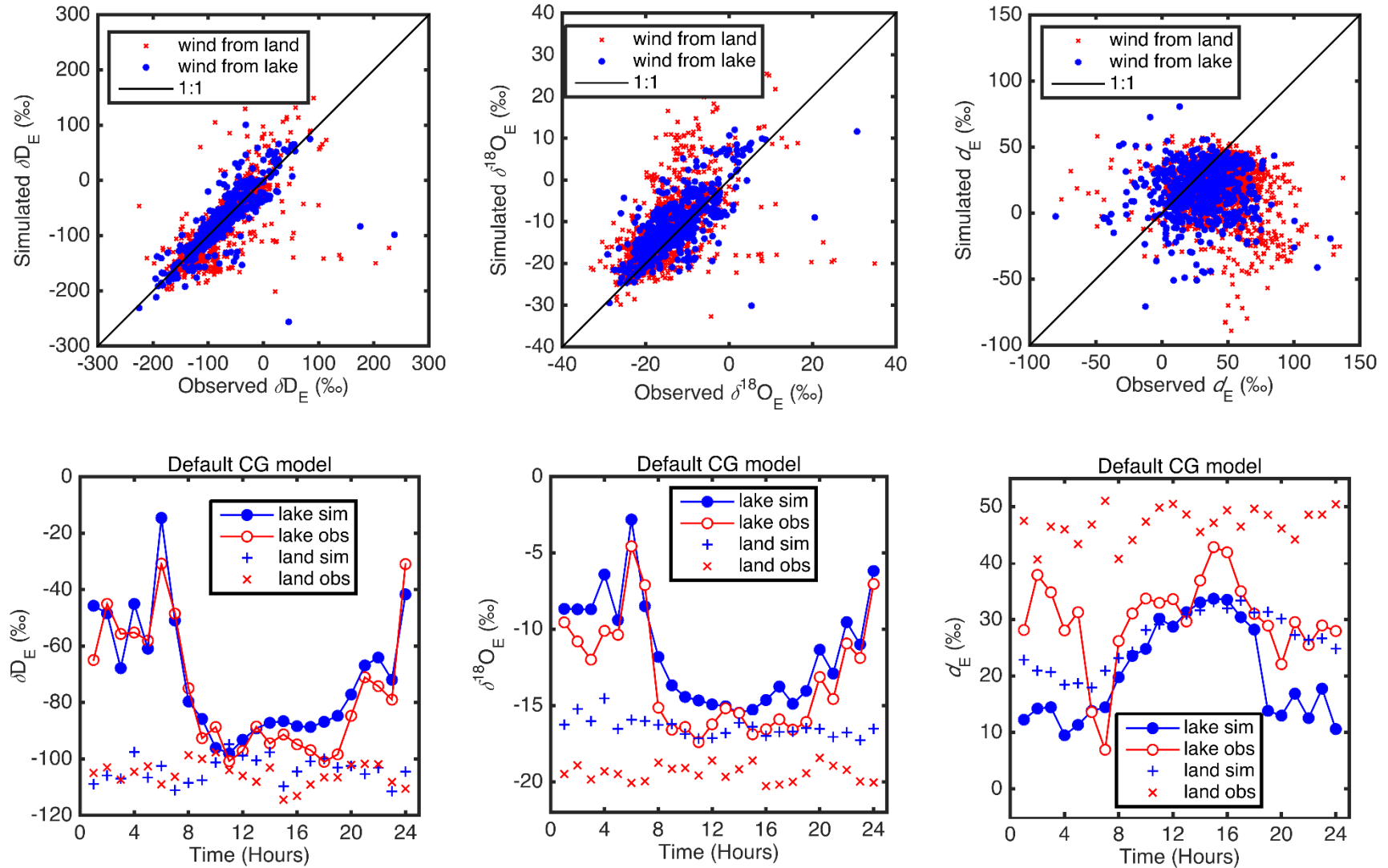
Step 2: calculate the isotopic value of ambient water vapor

$$\delta_v = \delta_1 + \frac{\delta_2 - \delta_1}{x_{s,2} - x_{s,1}} (x_a - x_{s,1})$$

Step 3: calculate the isotopic value of evaporation

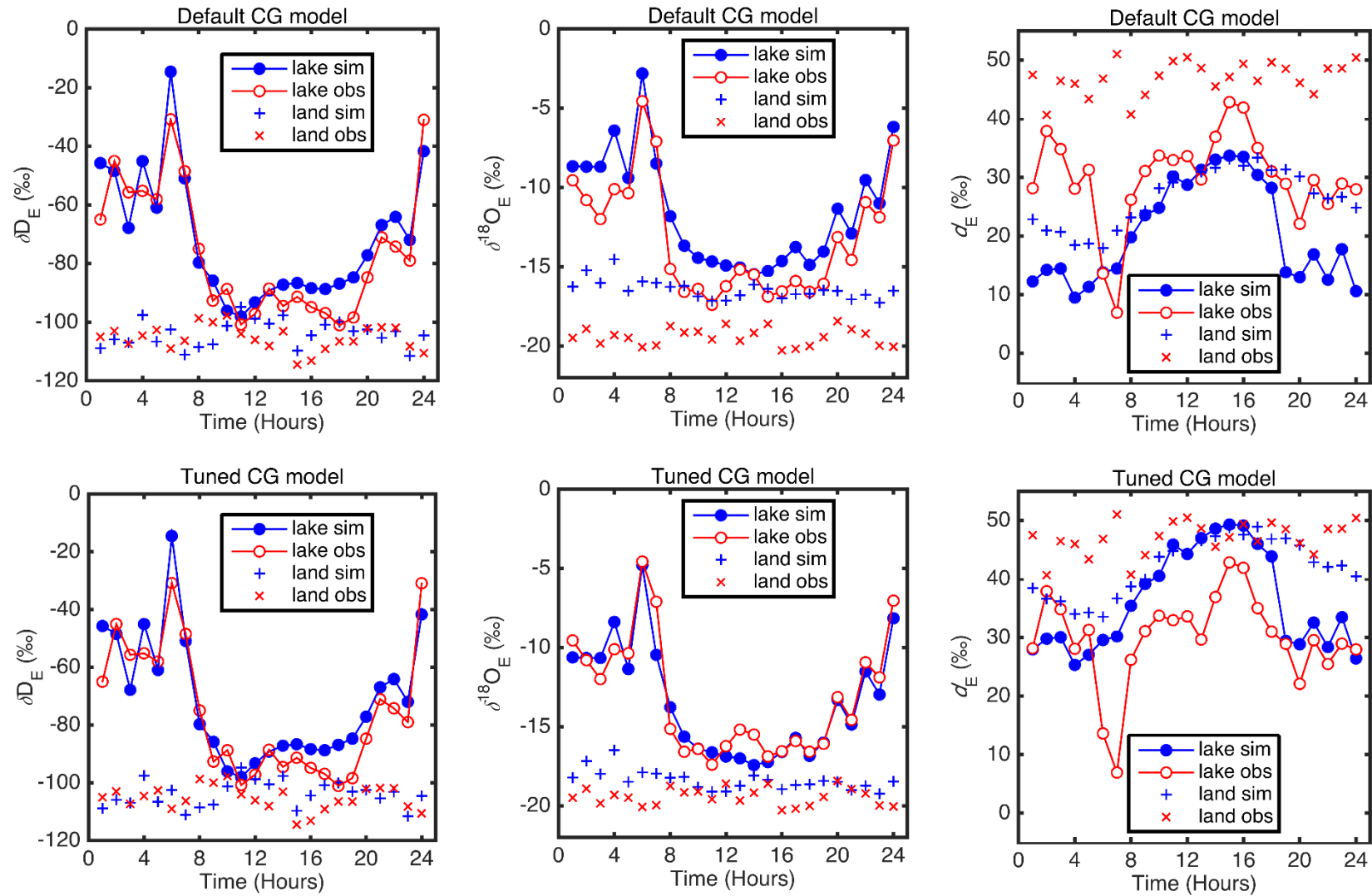
$$R_E = R_c \cdot \frac{x_{s,2} - x_{s,1}}{x'_{s,2} - x'_{s,1}} \cdot \frac{x'_{a,2} - x'_{a,1}}{x_{a,2} - x_{a,1}}$$

Validation of CG model



Note: continuous days, DOY 225-233, 482-530, 1000-1020

Sensitivity analysis on kinetic fractionation factors

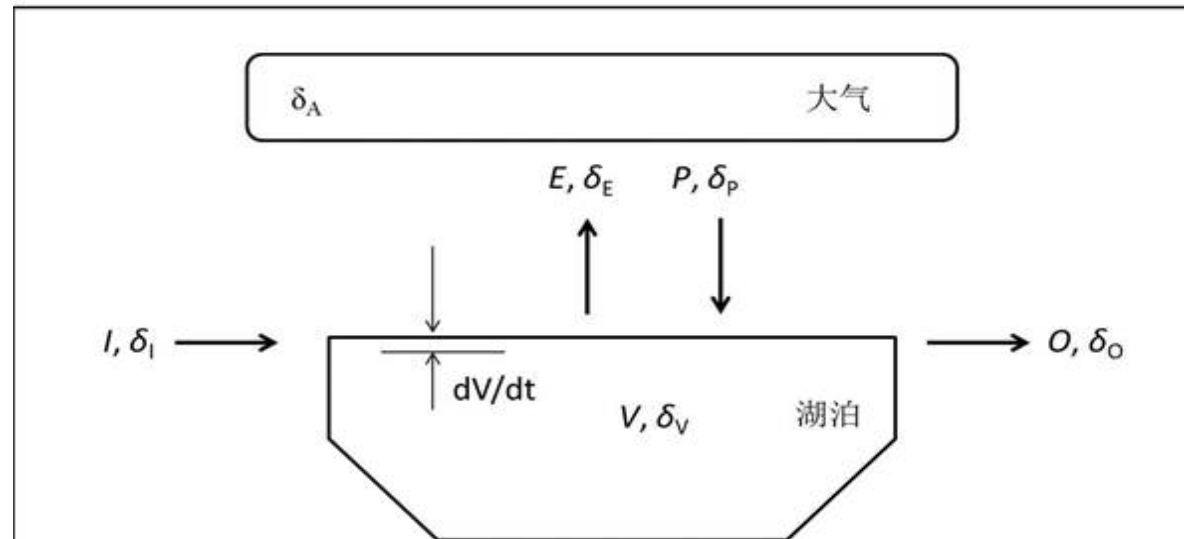


Tuned CG model: $\epsilon_k^{18}O + 2$ ‰, $\epsilon_k D$ default.

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Isotopic mass balance equation



水分平衡方程为：

$$I + P = E + dV + O \quad (6)$$

同位素质量守恒方程为：

$$\delta_I I + \delta_P P = \delta_E E + \delta_V dV + \delta_O O \quad (7)$$

湖泊蒸发的同位素含量计算公式为：

$$\delta_E = (\delta_I I + \delta_P P - \delta_V dV - \delta_O O) / E \quad (8)$$

Isotopic mass balance method

Month	Water budgets ($\times 10^8 \text{ m}^3$)						δD (per mil)					$\delta^{18}\text{O}$ (per mil)				
	S	ΔS	P	I	O	E	$\Delta(S\delta_s)$	δD_p	δD_I	δD_O	δD_E	$\Delta(S\delta_s)$	δD_p	δD_I	δD_O	δD_E
201305	47.0	3.3	3.6	7.0	5.0	2.3	-72.4	-42.0	-36.7	-28.0	-86.2	12.7	-6.4	-5.2	-4.0	-23.1
201306	51.3	5.4	3.0	10.6	6.2	2.0	-142.2	-62.6	-39.7	-29.7	-138.9	-96.2	-8.7	-5.3	-4.0	19.0
201307	51.5	-5.1	1.4	8.5	11.1	3.9	148.1	-43.8	-42.5	-31.4	-57.0	-61.3	-6.6	-5.4	-4.1	13.3
201308	48.4	-0.9	2.6	9.9	9.1	4.3	25.7	-51.5	-41.6	-31.6	-65.6	-58.2	-7.5	-5.3	-4.2	5.5
201309	48.3	0.7	1.4	9.6	7.7	2.6	-32.3	-47.0	-39.5	-31.4	-65.7	-31.8	-6.9	-5.2	-4.2	2.0
201310	52.3	7.7	6.0	14.1	10.8	1.7	-254.4	-32.2	-37.6	-31.2	-80.8	-63.0	-5.3	-5.0	-4.3	3.9
201311	51.8	-8.6	0.3	3.8	11.5	1.2	264.0	-26.8	-36.7	-30.7	-49.5	-7.3	-4.6	-4.8	-3.9	28.5
201312	46.1	-2.3	1.0	5.7	8.4	0.5	63.5	-19.8	-36.2	-30.0	-69.1	-53.6	-3.9	-4.5	-3.4	109.0
201401	43.6	-2.6	0.6	6.1	9.1	0.2	77.9	-21.0	-35.6	-29.4	-185.9	-48.1	-4.0	-4.3	-3.0	217.4
201402	46.0	7.2	3.5	8.4	4.1	0.6	-265.5	-37.2	-33.8	-28.2	-54.9	-54.7	-5.8	-4.2	-3.0	19.8
201403	49.3	-0.7	2.2	8.0	10.0	0.9	42.8	-23.0	-31.5	-26.7	-88.5	143.1	-4.2	-4.2	-3.2	-174.3
201404	50.6	3.5	3.5	8.1	6.5	1.6	-89.8	-35.3	-29.2	-25.2	-64.8	123.6	-5.6	-4.2	-3.4	-94.3
201405	50.1	-4.4	2.0	6.2	10.4	2.2	145.2	-37.3	-29.2	-25.4	-61.8	160.0	-5.8	-4.4	-3.7	-73.7
201406	50.9	5.9	5.3	9.5	6.5	2.3	-167.3	-61.2	-36.8	-31.7	-127.0	-81.4	-8.6	-5.4	-4.6	6.4
201407	57.2	7.0	5.3	14.6	10.4	2.6	-239.8	-57.6	-44.3	-37.8	-125.4	-239.4	-8.2	-6.3	-5.4	62.3
201408	61.3	1.2	5.3	10.8	12.6	2.3	-58.0	-67.9	-44.7	-37.0	-138.1	-150.6	-9.3	-6.4	-5.2	42.6
201409	59.7	-4.4	2.5	9.5	14.4	2.1	151.8	-61.3	-43.5	-34.7	-107.5	-3.1	-8.6	-6.2	-4.8	-3.9
201410	54.2	-6.5	1.0	4.9	10.5	1.9	227.8	-28.8	-42.8	-33.1	-62.1	8.8	-4.9	-6.1	-4.6	2.4
201411	50.7	-0.5	1.3	7.9	8.7	1.0	16.0	-37.9	-41.8	-32.9	-108.2	-5.6	-5.9	-6.0	-4.5	-10.7

Data source:

S, ΔS , I: Taihu bureau

P: mean precipitation of Wuxi, Dongshan and Huzhou meteorological station

E: Priestly-Taylor equation based on the MLW observation

O: calculated using water mass balance equation

$\Delta(S\delta_s)$: $\Delta(S\delta_s) = \Delta S * \delta_s + S * \Delta\delta_s$, first interpolate seasonal lake water isotope to daily value, then calculate monthly average δ_s and $\Delta\delta_s$ (month end – month begin) based on the daily data.

δD_p , $\delta^{18}\text{O}_p$: calculated from monthly mean air temperature and month total sunshine duration using the regression equation of Liu et al. (2014), calculated δD_p for Wuxi, Dongshan and Huzhou respectively, then got mean value.

δD_I , δD_O , $\delta^{18}\text{O}_I$, $\delta^{18}\text{O}_O$: interpolated to daily value from [seasonal lake survey](#), then calculate month mean using daily data.

δD_E , $\delta^{18}\text{O}_E$: calculated using isotopic mass balance equation.

Isotopic mass balance method vs Craig-Gorden model

Results of May 2013

Isotopic mass balance method

$$\delta D_E = -86.2 \text{ ‰}$$

$$\delta^{18}O_E = -23.1 \text{ ‰}$$

Flux weighted isotope based on tuned CG model

$$\delta D_E = -86.7 \text{ ‰}$$

$$\delta^{18}O_E = -15.8 \text{ ‰}$$

Sensitivity analysis on precipitation isotope

$$\delta^{18}O_p = -1.8 \text{ ‰}$$



Thanks for your attention!

<http://yncenter.sites.yale.edu>

