A modeling investigation of canopy-air oxygen isotopic exchange of water vapor and carbon dioxide in a soybean field

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The oxygen isotopes of CO$_2$ and H$_2$O ($^{18}$O-CO$_2$ and $^{18}$O-H$_2$O) provide unique information regarding the contribution of terrestrial vegetation to the global CO$_2$ and H$_2$O cycles. In this paper, a simple isotopic land surface model was used to investigate processes controlling the isotopic exchange of $^{18}$O-H$_2$O and $^{18}$O-CO$_2$ between a soybean ecosystem and the atmosphere. We included in a standard land surface model a nonsteady state theory of leaf water isotopic composition, a canopy kinetic fractionation factor, and a big-leaf parameterization of the $^{18}$O-CO$_2$ isoforcing on the atmosphere. Our model simulations showed that the Péclet effect was less important than the nonsteady state effect on the temporal dynamics of the water isotopic exchange. The model reproduced the highly significant and negative correlation between relative humidity and the ecosystem-scale $^{18}$O-CO$_2$ isoforcing measured with eddy covariance. But the model-predicted isoforcing was biased high in comparison to the observations. Model sensitivity analysis suggested that the CO$_2$ hydration efficiency must have been much lower in the leaves of soybean in field conditions than previously reported. Understanding environmental controls on the hydration efficiency and the scaling from the leaf to the canopy represents an area in need of more research.


1. Introduction

[2] Studying the $^{18}$O/$^{16}$O ratio in CO$_2$ and H$_2$O can provide constraints on the water and carbon exchange processes between the land and the atmosphere. The lower vapor pressure and diffusion rate of H$_2^{18}$O molecules compared to H$_2^{16}$O cause H$_2^{18}$O to accumulate in the leaf water during transpiration. Oxygen atoms exchange between the CO$_2$ and H$_2$O molecules in a hydration reaction catalyzed by carbonic anhydrase. Consequently, those CO$_2$ molecules that diffuse from the leaf back to the atmosphere carry the isotopic signal of the leaf water [Farquhar et al., 1993]. Understanding the fractionation processes and the mechanisms controlling

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land-atmosphere $^{18}$O-CO$_2$ and $^{18}$O-H$_2$O exchange can help to resolve a number of important questions related to global carbon and water cycles. At present, we lack the capacity to interpret long-term changes in the isotopic composition of the atmosphere and the ability to decipher if these changes are related to climate variability, changes in land use, or other anthropogenic activities.

[3] Land surface models (LSMs) are a powerful tool for integrating the isotopic fractionation processes with CO$_2$ and H$_2$O exchange in terrestrial ecosystems. Cintz et al. [2003a, 2003b] and Hoffmann et al. [2004] used LSMs to simulate $^{18}$O-H$_2$O and $^{18}$O-CO$_2$ budgets on the global scale. Farquhar et al. [1993] calculated the global $^{18}$O-CO$_2$ composition to investigate the oxygen fractionation mechanism by using the observed meteorology, and highlighted the different effects on atmospheric $^{18}$O-CO$_2$ composition of terrestrial and oceanic fluxes. Gillon and Yakir [2001] used the SiB2 model to calculate a global mean value for the extent of $^{18}$O equilibrium between CO$_2$ and leaf water and quantify large differences in carbonic anhydrase activity among major plant groups. Riley et al. [2002, 2003] developed a two-leaf isotopic model to simulate $^{18}$O-H$_2$O and $^{18}$O-CO$_2$ exchange at the ecosystem scale. So far, the validation of LSMs for the $^{18}$O-CO$_2$ flux have been inhibited by the lack of high-resolution isotopic data under field conditions [McDowell et al., 2008].

[4] This paper aims to investigate, using a simple isotopic LSM (SiLSM), the isotopic exchange of $^{18}$O-H$_2$O and $^{18}$O-CO$_2$ between a soybean ecosystem and the atmosphere.
The model has integrated the latest advances, both experimental and theoretical, on fractionation processes controlling the isotopic exchange. One unique feature of our work is that key isotopic variables were measured at a high temporal resolution to drive and validate the isotopic LSM. These data were obtained in a field experiment where the isotopic fluxes of $^{18}$O-$\text{CO}_2$ and $^{18}$O-$\text{H}_2\text{O}$ were measured with eddy covariance and flux-gradient methods, along with supporting measurements of $^{18}$O-$\text{H}_2\text{O}$ in ecosystem water pools. $^{18}$O/$^{16}$O ratio in atmospheric $\text{CO}_2$ and micrometeorological variables [Griffis et al., 2005b, 2008; Lee et al., 2005; Welp et al., 2008].

Our strategy is to constrain the standard flux parameterizations with the field observations but keep to a minimum the tuning of parameters related to the isotopic processes. The disagreement between the calculated and observed isotopic fluxes should therefore help us identify deficiencies in the current knowledge of the isotopic exchange.

[5] Our SiLSM adopts the system of equations of Farquhar and Cernusak [2005] for predicting the $^{18}$O-$\text{H}_2\text{O}$ composition of leaf water ($\delta^{18}$O) in nonsteady state. Modeling $\delta^{18}$O is a crucial part of isotopic LSMs because $\delta^{18}$O plays a major role in the $^{18}$O-$\text{CO}_2$ flux from the ecosystem to atmosphere [Farquhar et al., 1993]. An improved understanding of $\delta^{18}$O and the associated canopy $^{18}$O-$\text{CO}_2$ flux should benefit researchers who wish to partition the net $\text{CO}_2$ flux into gross photosynthesis and respiration components [Oge et al., 2004; Yakir and Wang, 1996], reconstruct paleoclimate with plant materials [Cullen et al., 2008; Epstein and Yapp, 1977; Gray and Thompson, 1976; Libby et al., 1976; Roden et al., 2000], and estimate the Dole effect [Bender et al., 1994; Hoffmann et al., 2004]. Dongmann et al. [1974] made the first attempt at calculating the isotopic composition of leaf water in nonsteady state using the Craig-Gordon model on the assumption that leaf water is evenly enriched in $^{18}$O. The study of Farquhar and Cernusak [2005] accounted for both the nonsteady state effects [Wang and Yakir, 1995] and progressive enrichment of $^{18}$O from the xylem to the site of evaporation according to the Péclet effect [Farquhar and Lloyd, 1993]. The in situ measurement of the isotopic composition of canopy transpiration [Welp et al., 2008] and the high-frequency measurement of the bulk leaf water $\delta$ [Farquhar and Cernusak, 2005] suggest the necessity to consider nonsteady state and the Péclet effect in field conditions. The original set of equations of Farquhar and Cernusak [2005] are developed for the leaf scale. Here we extend these concepts to the canopy scale.

[6] Kinetic fractionation is another crucial factor controlling the isotopic exchange between ecosystems and the atmosphere. In leaf-scale studies, kinetic fractionation is regarded as a function of the kinetic factors associated with the stomatal resistance and the leaf boundary layer resistance [Dongmann et al., 1974; Farquhar and Lloyd, 1993; Flanagan et al., 1991]. At the canopy scale the role of turbulent diffusion is not treated in a consistent manner [Ciais et al., 1997; Cuntz et al., 2003a; Dongmann et al., 1974; Farquhar et al., 1993; Hoffmann et al., 2004; Riley et al., 2002]. The first direct isotopic flux measurements mentioned above have confirmed the need to consider air turbulent diffusion when calculating the isoforcing of $^{18}$O-$\text{CO}_2$, and the enrichment of leaf water in $^{18}$O. Here, the canopy-scale fractionation factors and the big-leaf isoforcing parameterization developed by Lee et al. [2009] have been integrated into SiLSM.

[7] Another goal of this study is to perform model sensitivity analyses to identify potential sources of error for the isotopic LSM parameterizations and variables that exert large control on the isotopic fluxes. This goal is motivated by the fact that the observational data alone cannot disentangle the complex role of various fractionation processes. Specifically, we will address three issues including: (1) the importance of energy balance closure in model studies; (2) the sensitivity of canopy $^{18}$O-$\text{CO}_2$ exchange to the $\text{CO}_2$ hydration extent within the leaves and soil; (3) the effects of elevated $\text{CO}_2$ concentration, wind speed, humidity, temperature and soil moisture on the isotopic fluxes from the ecosystem to the atmosphere.

2. Experimental Methods

[8] The field measurements were taken in 2006 at the University of Minnesota's Rosemount Research and Outreach Center, about 25 km south of St. Paul, MN. The experimental site is part of the AmeriFlux network and managed in a corn-soybean rotation typical of the Upper Midwest. This experiment was conducted during the soybean (C3) phase of the rotation. Detailed information about this site and instruments can be found in other papers [Baker and Griffis, 2005; Griffis et al., 2005a, 2005b, 2007, 2008; Welp et al., 2008]. Soybeans were planted on 24 May (day of year DOY 144), with the maximum LAI of 8.15 reached around 3 August (DOY 215). The maximum plant height was about 1 m.

[9] Isotopic measurements of $\text{CO}_2$ and water vapor were made with three tunable diode laser (TDL) analyzers (model TGA100A, Campbell Scientific, Inc., Logan, Utah). One analyzer was used to measure the isotope ratio of water vapor ($\delta^{18}$O) at two heights above the canopy. The hourly $^{18}$O/$^{16}$O isotope ratio of evapotranspiration ($\delta^{18}$ET) was obtained from the flux-gradient approach [Welp et al., 2008]. The second TDL analyzer, also deployed in the flux-gradient mode, measured the $^{18}$O/$^{16}$O and $^{13}$C/$^{12}$C isotope ratio of atmospheric $\text{CO}_2$ at two heights over the canopy. From 18 July to 20 September, a third TDL analyzer was used in the closed-path eddy covariance (EC-TDL) mode to measure the covariance $w^3\delta^{18}$O, which is a direct measure of the $^{18}$O/$^{16}$O isoforcing [Griffis et al., 2008]. The TDL analyzers were installed at the north edge of the field and the data were sensitive to wind direction. The $^{18}$O/$^{16}$O ratios in atmospheric water vapor and $\text{CO}_2$ are among the driving variables of SiLSM and the measurements of the $^{18}$O-$\text{CO}_2$ isoforcing and $\delta^{18}$ET were used to evaluate the performance of the model.

[10] Supporting measurements consisted of standard micrometeorological variables and the $^{18}$O-$\text{H}_2\text{O}$ content of ecosystem water pools. We measured the eddy fluxes of heat, water vapor, momentum and standard micrometeorological variables (air temperature and humidity, canopy temperature, wind speed and direction, soil temperature and moisture). We sampled the $^{18}$O-$\text{H}_2\text{O}$ content of ecosystem water pools at varying time intervals: leaf samples were collected daily (at midday), and stem and 10 cm soil samples were collected every week, except during a 3 day intensive period (DOY 208–210) when leaf samples were collected every 3 h, stem and soil (0, 5, 10 cm depth) every 6 h, and 20 cm soil once per day.
Leaf water content is a critical variable in determining the leaf water δ in nonsteady state. It was measured at midday once every week from DOY 159 to 241 (Figure 1a). Leaf water content was 128.9 g m⁻² (mass of water per unit leaf area) at the beginning of the growing season and declined to 100.7 g m⁻² before leaf senescence, with a mean value 111.2 g m⁻². During the intensive period, it was measured every 3 h at the top and bottom of the canopy. The magnitude of diurnal leaf water content variation was bigger at the bottom of the canopy than at the top (Figure 1b). For the bottom leaves, it varied from 79.6 g m⁻² around midday to 125.5 g m⁻² at night, with a mean value 107.2 g m⁻². For the top leaves, it varied from 94.1 g m⁻² around midday to 120.7 g m⁻² at night, with a mean value 109.2 g m⁻².

3. Model Description

3.1. Model Structure

A detailed description of SiLSM is provided in Appendices A–C. Briefly, the model consists of three submodels (Figure 2). A big leaf parameterization of the ¹⁸O-CO₂ isoforcing on the atmosphere derived by Lee et al. [2009], the central part of the model, calculates ecosystem ¹⁸O-CO₂ isoforcing and its canopy and soil components as the final outputs (Appendix A). Here the isoforcing is represented by the covariance of the vertical velocity and the ¹⁸O-CO₂ composition in air, wδ (in units of %o m s⁻¹). Lee et al. [2009] showed that this covariance is the proper lower boundary condition for evaluating atmospheric ¹⁸O-CO₂ budget. For historical reasons, we also use the quantity C_a (wδ), termed as eddy isoforcing, which carries the dimensions of isoflux (µmol m⁻² s⁻¹ %o). The driving variables of this submodel are the concentration (C_a) and ¹⁸O isotopic composition (δ_a) of the atmosphere CO₂, both measured at a reference height of 3.0 m above the ground. A complete list of symbol definitions is provided in the notation section.
The second submodel deals with $^{18}$O in leaf water. Several studies show that leaf water is usually in nonsteady state in a diurnally varying humidity regime, wherein the isotopic compositions of the source water and the transpiration water are not the same [Cernusak et al., 2002, 2005; Harwood et al., 1998; Lee et al., 2009; Wang and Yakir, 1995]. A system of equations developed by Farquhar and Cernusak [2005] was employed to determine a critical but nonmeasurable variable, the $^{18}$O-H$_2$O composition at the evaporative site $\delta_{Lw}^{18}$, and predict the $^{18}$O-H$_2$O composition of bulk leaf water ($\delta_{L,b}^{18}$) and evapotranspiration ($\delta_{ET}^{18}$) for comparison with the measurement (Appendix B).

The canopy and soil CO$_2$ flux, evapotranspiration rate, canopy temperature and resistance terms were computed using the big-leaf LSM of Ronda et al. [2001], with three important changes (Appendix C). This LSM was selected for several reasons. First, because it is a big leaf model, it can be easily interfaced with the big leaf version of the Farquhar and Cernusak [2005] model for the leaf water isotope and the big-leaf isoforcing parameterization we have recently developed [Lee et al., 2009]. Second, this LSM was recently coupled to the NCAR’s large eddy simulation model (LES) [Huang et al., 2008]. Efforts are underway to expand the LES model to simulate the carbon and water isotopic budgets in the atmospheric boundary layer. Finally, the LSM considers the nonlinear response of plant physiology to light penetration inside the canopy, which is usually ignored in other big-leaf LSMS. Its treatment of the response is crude in comparison to the two-leaf sunlit and shade model of Riley et al. [2002] and the multilayer models of Baldocchi and Bowling [2003] and Ogee et al. [2007]. However, the choice of the simple LSM is justified by the fact that we did not have detailed micrometeorological measurements inside the canopy to verify the predictions of the multilayer schemes. Also it is not straightforward to implement the Farquhar’s nonsteady state method in the two-leaf model because it requires tracking of the leaf water $^{18}$O budget in a fix number of leaves whereas in a two-leaf scheme the fractions of sunlit and shade leaves change through the course of the day [Riley et al., 2002, 2003; Wang and Leuning, 1998].

Soil variables, except for the soil CO$_2$ flux, were not parameterized; instead they were provided by the measurement. In this regard, our model is suitable for the intended purpose of diagnostic analysis but is less useful for prognostic prediction.

The $^{18}$O-CO$_2$ composition was referenced to the Vienna Pee Dee Belemnite (VPDB) scale, and $^{18}$O-H$_2$O composition was referenced to the Vienna Standard Mean Ocean Water (VSMOW).

### 3.2. Input Data

The SiLSM model was driven by field observations of:

1. Plant variables including leaf area index (LAI), leaf water content per unit ground area ($W$) and canopy height ($h$),
2. Micrometeorological variables including air temperature ($T_a$), soil temperature ($T_s$), relative humidity of air ($R_h$), soil moisture content ($\theta$), solar radiation ($R_s$), sky long-wave radiation ($R_d$), atmospheric CO$_2$ concentration ($C_a$), wind speed ($u_w$) and friction velocity ($u_*$), and $^{18}$O composition of atmospheric CO$_2$ ($\delta_{a}^{18}$) and H$_2$O vapor ($\delta_{v}^{18}$) measured at the reference height, and the $^{18}$O-H$_2$O composition of xylem water ($\delta_{x}^{18}$) and soil water ($\delta_{w}^{18}$). Here $T_s$ and $\theta$ were measured at 10 cm depth of soil, and all other variables were measured at the reference height of 3.0 m above the ground.

### 3.3. Model Parameterization

The lack of energy balance closure in eddy covariance measurement introduced a dilemma for the LSM model validation since the model was based on the principle of energy budget conservation. The sum of the measured latent heat flux ($LE$), sensible heat flux ($H$) and soil heat flux ($G$) accounted for 69% of the net radiation ($R_n$), with heat storage in the canopy layer being ignored. Such imbalance is typical of experiments over low vegetation [Foken, 2008]. In another synthesis study, Wilson et al. [2002] reported an average 20% imbalance among the FluxNet sites. To satisfy energy conservation, we adjusted the $LE$ and $H$ measurement by forcing energy balance closure with the assumption that the available energy ($R_n - G$) and the Bowen ratio $H/LE$ were accurately measured [Blanken et al., 1997]. Other modelers have also reported the need to force energy balance closure for model parameterization and validation [Arainbar et al., 2006].

The LSM submodel contains four tunable parameters. Two of them ($b_1$ and $b_2$) describe the dependence of photosynthesis on soil moisture (equation (C15)) and the other two appear in the stomatal resistance parameterization (the vapor pressure deficit constant $D_0$ and CO$_2$ concentration constant $a_1$ in equation (11) of Ronda et al. [2001]). Since no leaf-scale ecophysiological measurements were available to constrain these parameters, they were tuned with the ecosystem-scale data. First, $D_0$ and $a_1$ were tuned by a nonlinear least squares method so that the predicted net ecosystem CO$_2$ flux ($F_N$) was optimized to match the observed $F_N$. Next, $b_1$ and $b_2$ were tuned to optimize the prediction of $LE$. The optimized values were $D_0 = 0.44$ kPa, and $a_1 = 16.2$, $b_1 = -5.8$ and $b_2 = -24.9$ for $\theta \leq 0.21$, $b_1 = -1.5$ and $b_2 = -24.9$ for $\theta > 0.21$.

The $^{18}$O-H$_2$O submodel contains one free parameter, $L_{eff}$ the scaled effective “radial” length in the Péclet number. It was optimized with the $^{18}$O composition of the bulk leaf water ($\delta_{L,s}^{18}$) measured in midday hours. The optimized value of $L_{eff}$ was less than 0.01 mm. This is much lower than the values of 6.25 mm in Phaseolus vulgaris and 13.5 mm in Ricinus communis found by other authors [Barbour and Farquhar, 2000; Barbour et al., 2000; Cernusak et al., 2003; Flanagan et al., 1994]. Welp et al. [2008] obtained a $L_{eff}$ value of 20 mm by tuning the Farquhar and Cernusak predicted $\delta_{L,s}^{18}$ against the measured $\delta_{L,b}^{18}$ using kinetic fractionation factors that ignore aerodynamic diffusion. The extremely low $L_{eff}$ suggests that the Péclet effect was negligible.

The $^{18}$O-CO$_2$ isoforcing submodel contains two free parameters, $\theta_{eq,s}$ and $\theta_{eq,b,s}$. We used the value of 0.75 for soybean $\theta_{eq}$ reported by Gillon and Yakir [2000] and set $\theta_{eq,b,s}$ to 1. No tuning of these parameters was made, so the disagreement between the calculated and observed isoforcing helps us identify deficiencies in the current knowledge of the isotopic exchange.
Our model simulation was restricted to the period from day of year (DOY) 195 to 239. In this period, the canopy was fully closed (LAI > 2). The soil contribution to \( H \) and \( LE \), which was ignored in our model, should be very small. Although not available during the 2006 experiment, subsequent automated chamber observations from this site suggested that soil evaporation was generally less than 10% of ET.

4. Results

4.1. Water, Heat, and CO\(_2\) Fluxes

Here we use the index of agreement \( I \) and root mean square difference (RMSD) to measure the model performance. The index of agreement [Willmott, 1981] is defined by

\[
I = 1 - \frac{\sum_{i=1}^{N} (p_i - o_i)^2}{\sum_{i=1}^{N} (|p_i - \bar{o}| + |o_i - \bar{o}|)^2}
\]

where \( p_i \) and \( o_i \) are the predicted and observed values, respectively, for measurement \( i \), \( N \) is the total number of observations, and \( \bar{o} \) represents the average value of the observations. An index value of 1 indicates perfect agreement and 0 means no agreement between the simulation and the observation. The root mean square difference RMSD is defined by

\[
RMSD = \left[ \frac{1}{N} \sum_{i=1}^{N} (p_i - o_i)^2 \right]^{1/2}
\]

Figure 3 represents the time series of latent and sensible heat fluxes (\( LE \) and \( H \)) and net ecosystem CO\(_2\) exchange \( F_N \) (positive for CO\(_2\) emission and negative for CO\(_2\) absorption). Here the measured \( LE \) and \( H \) were adjusted to achieve perfect energy balance closure. The maximum (minimum) observed value was 748 (−293) W m\(^{-2}\), 15.6 and −8.5 \( \mu \)mol m\(^{-2}\) s\(^{-1}\), respectively. The seasonal and diurnal variation was captured by the model, with the index of agreement \( I \) for the \( LE \), \( H \) and \( F_N \) simulation equal to 0.97, 0.78 and 0.94 and RMSD of 57 W m\(^{-2}\), 46 W m\(^{-2}\) and 6 \( \mu \)mol m\(^{-2}\) s\(^{-1}\), respectively.

Obvious biases in the modeled fluxes occurred in two periods, including DOY 209 to 212 and DOY 226 to 235, suggesting that the model breaks down during conditions of water stress. This is common to many models. In the first period, the magnitudes of midday (from 1000 to 1500 LST) \( LE \) and \( F_N \) were overestimated and \( H \) was underestimated by the model. For example, on the midday of DOY 211, the modeled and observed \( LE \) was 448 and 305 W m\(^{-2}\), \( F_N \) was 15.6 and −8.5 \( \mu \)mol m\(^{-2}\) s\(^{-1}\) and \( H \) was 72 and 144 W m\(^{-2}\), respectively. The last significant precipitation event (>31 mm) occurred on DOY 200. Following this event, soil moisture declined steadily to 0.19 m\(^{-3}\) (the lowest of the season) at the 10 cm depth. Even though the highest LAI of ∼8 was recorded on DOY 212, the magnitude of the observed \( F_N \) was only 1/3 of that on DOY 215 when PAR was similar but \( q \) was much higher (0.26 m\(^{-3}\)) following precipitation events with amount of 39 and 47 mm on DOY 213 and 214, respectively. In the second period, the magnitude of the \( LE \) and \( F_N \) were underestimated and \( H \) was overestimated by the model. In this period, \( \theta \) was very low ranging from 0.19 to

![Figure 3. Comparison of the simulated (solid line) and observed (dots) of latent heat flux (\( LE \)), sensible heat flux (\( H \)), and net ecosystem CO\(_2\) exchange (\( F_N \)).](image-url)
The high sensitivity of the soybean system to soil moisture, as indicated by the measurements, was not adequately captured by the model. A better parameterization of the photosynthetic response to the root zone soil moisture is needed to improve the modeled results.

4.2. The $^{18}$O Composition of Leaf Water and Evapotranspiration

Figure 4 shows the modeled and observed time series of the isotopic composition of the bulk leaf water ($\delta_{L,b}^{w}$). The index of agreement was 0.78 and RMSD was 2.9% for the midday isotopic composition. The observed mean midday $\delta_{L,b}^{w}$ value ranged from $-2.9$ to $13.2\%$ for bottom leaves and from $-4.5$ to $10.8\%$ for top leaves, and the modeled values ranged from $-1.0$ to $14.2\%$. The midday $\delta_{L,b}^{w}$ was underestimated by the model on most days before DOY 212, and overestimated from DOY 224 to 234. Reasonable agreement was achieved between DOY 215 to 223. During the intensive experimental period (from DOY 208 to 210), the diurnal variation was captured by the model although the magnitude of $\delta_{L,b}^{w}$ variations was underestimated.

Figure 5 reveals the impact of the steady state assumption and the choice of $L_{eff}$ on the prediction of leaf water $^{18}$O. Here $\delta_{L,b}^{w}$ is the average of the upper and lower canopy values. Nonsteady state (dots) improved the simulation slightly, with $R^2 = 0.39$ ($N = 39$), compared to steady state simulation (Figure 5a, pluses) with $R^2 = 0.33$. The marginal improvement confirms that nonsteady state effects were small near midday when the measurement was made. Simulation using a typical value of 15 mm for $L_{eff}$ found in the literature introduced an obvious bias (crosses), with $R^2 = 0.22$. In the scatterplot of the predictions for $\delta_{L,e}^{w}$ in nonsteady state and in steady state (Figure 5b), most data points deviated from the 1:1 line except during some nighttime periods when dew events occurred. During the dew events, both predictions gave identical results. Figure 5c presents the diurnal composite of the deviation between the two predictions (nonsteady state minus steady state $\delta_{L,c}^{w}$ value). From 0730 to 1430 LST, the deviation was negative with the most negative value of $-0.6\%$ occurring around 1030 LST, which indicates that $\delta_{L,c}^{w}$ was lower than that of source (xylem) water $\delta_{L}^{x}$ and $^{18}$O-H$_2$O was accumulating in the leaf water. Over the time period from 1500 to 0700 LST, the deviation was positive with the maximum value of $1.3\%$ occurring at 1900 LST, which indicates that $\delta_{L}^{c}$ was greater than $\delta_{L}^{x}$.

Figure 6 shows the diurnal composite of the modeled and observed $\delta_{ET}^{w}$. The reader is reminded that SiLSM ignored the soil evaporation contribution to ET, which is expected to have a small influence when LAI $>$ 2 and would act to lower $\delta_{ET}^{w}$. Both composites include periods influenced by nighttime dew events. In the whole study period, $\delta_{ET}^{w}$ ranged from $-5.5\%$ to $-8.4\%$, with a mean value of $-7.4\%$. During the daytime (from 0800 to 1800 LST), the modeled $\delta_{ET}^{w}$ ranged from $-9.6$ to $-4.3\%$, and the observed value ranged from $-7.3$ to $-2.8\%$. The simulated and observed $\delta_{ET}^{w}$ reached their daily peak value $11.6\%$ and $6.9\%$, respectively, at almost the same time in the evening (around 2000 LST). From 1830 to 0730 LST, the observed $\delta_{ET}^{w}$ was noisy and reached a minimum value of $-24.9\%$, while the simulated $\delta_{ET}^{w}$ did not get lower than $-9.6\%$. The deviation of the observed and modeled $\delta_{ET}^{w}$ from $\delta_{ET}^{x}$ provides strong evidence for nonsteady state of the leaf water isotopic exchange.

Figure 6 shows that the Farquhar and Cernusak model, when scaled to the whole canopy, captured reasonably well the temporal dynamics of $\delta_{ET}^{w}$ in the dew-free period (1000–1800 LST). In the hours between 1900 and 0900 LST, the $\delta_{ET}^{w}$ observation was confounded by the influence of dew formation which occurred around 80% of the nights between DOY 195 and 239. The performance of their model was inadequate during these periods.
4.3. The $^{18}$O-CO$_2$ Isoforcing

Figure 7 shows the time series of the modeled and observed eddy isoforcing both in good fetch and poor fetch conditions. The seasonal and diurnal variation was captured by SiLSM, with the index of agreement ($I$) between all the observation and those model results at the corresponding time of 0.81, and RMSD of 142 $\mu$mol m$^{-2}$ s$^{-1}$ %$_o$ ($N = 1522$).

Both the model simulation and the observation indicate that the $^{18}$O-CO$_2$ exchange was strongly influenced by relative humidity (in reference to canopy temperature, Figure 9). The observed relationship can be expressed by the linear regression $y = 470 - 6.2x$ with $R^2 = 0.45$. The model data for the same periods can be described by a linear regression with roughly the same slope but different intercept ($y = 760 - 8.3x$, $R^2 = 0.71$). The offset between the modeled and observed relationships was mostly likely a model bias (see also Figure 8).

4.4. Sensitivity Analyses

Three sets of sensitivity analysis were performed, including sensitivity to unconstrained model parameters, to the way processes was handled in the model, and to driving variables (Table 1). The first set concerns the impact of the two unconstrained model parameters, CO$_2$ hydration efficiency in the leaves ($\theta_{eq}$) and in soil ($\theta_{eq,s}$). We found that $\theta_{eq}$ had a significant effect on the eddy CO$_2$ isoforcing. The default value of 0.75 was employed in SiLSM [Gillon and Yakir, 2000]. If we change it to 0.5 (a relative change of $-33\%$) or 1.0 ($+33\%$), the diurnal peak value of the eddy isoforcing changes to 175 ($-39\%$) and 396 $\mu$mol m$^{-2}$ s$^{-1}$ %$_o$ ($+39\%$), respectively (Table 1 and Figure 10). Very small changes in the nighttime simulation were detected (Figure 10), with the minimum value of $-44$ and $-48$ $\mu$mol mol m$^{-2}$ s$^{-1}$ %$_o$ for $\theta_{eq}$ of 0.5 and 1, respectively, in comparison of $-46$ $\mu$mol m$^{-2}$ s$^{-1}$ %$_o$ corresponding to the default $\theta_{eq}$. The above result agrees with the sensitivity analysis of Riley et al. [2002, 2003] suggesting that lowering $\theta_{eq}$ results in less daytime ecosystem CO$_2$ flux enrichment to the atmosphere and little effect at night. The sensitivity to $\theta_{eq}$ may have been the primary cause of the model overprediction.
The default value of 1.0 was employed for \( q_{eq,s} \) in SiLSM. If we lower it to 0.5, the ecosystem eddy isoforcing increased to 330 \( \mu \text{mol} \text{m}^{-2} \text{s}^{-1} \% \) for daily peak value (a relative change of 16%) and to 18 \( \mu \text{mol} \text{m}^{-2} \text{s}^{-1} \% \) for minimum value (Figure 10).

The second set of analyses deals with how the key exchange processes are handled in the SiLSM submodels. In the LSM submodel, the adjusted \( LE \) and \( H \) measurements were used for parameter optimization. If the original measurement without adjustment for energy balance closure was used instead, the coefficients in the soil moisture function (equation (C15)) \( b_1 \) and \( b_2 \) would change to −5.4 and 19.3 from −5.8 and 24.9 for \( \theta \) below 0.21 and to −1.0 and −1.5 from −1.5 and 0.5 for \( \theta \) higher than 0.21, respectively. The two parameters in the stomatal function \( D_0 \) and \( a_1 \) changed to 0.32 kPa and 8.1 from 0.44 and 16.2, respectively. The diurnal peak value of the eddy \( ^{18}\text{O-CO}_2 \) isoforcing decreased to 279 \( \mu \text{mol} \text{m}^{-2} \text{s}^{-1} \% \) (a relative change of −2%) and the minimum value at night increased to 40 \( \mu \text{mol} \text{m}^{-2} \text{s}^{-1} \% \).

The 24 h mean value increased by 18%.

Figure 7. Time series of the ecosystem eddy \( ^{18}\text{O-CO}_2 \) isoforcing (solid line, simulation; circles, observations with poor fetch; dots, observations with good fetch).

Figure 8. Diurnal composite of the eddy \( ^{18}\text{O-CO}_2 \) isoforcing (solid line, simulated ecosystem eddy isoforcing; dashed line, simulated canopy eddy isoforcing; dotted line, simulated soil eddy isoforcing; dots, observation).

Figure 9. The relationship between ecosystem isoforcing and relative humidity referenced to canopy temperature. Dots, measurement; pluses, simulation.
[37] In the $^{18}$O submodel, assuming steady state caused the daily peak value of eddy $^{18}$O-CO$_2$ isoforcing to increase slightly to 289 $\mu$mol m$^{-2}$ s$^{-1}$ %o ($+1\%$) and shifted the peak time earlier by 1.5 h, consistent with the difference between steady versus nonsteady state prediction of $\delta_{le}$ (Figure 5c). Even though the peak eddy isoforcing value did not change much, ignoring the nonsteady state can cause errors in the timing of the predicted eddy isoforcing.

[38] In the isoforcing submodel, turbulence diffusion had a significant effect on the eddy isoforcing. Ignoring turbulent diffusion in the kinetic effects by dropping aerodynamic resistance $r_s$ from equations (A8), (A9), and (B4), increased the daily peak eddy isoforcing to 575 $\mu$mol m$^{-2}$ s$^{-1}$ %o, or a relative change of $+102\%$, substantially worsening the comparison with the measured values.

[39] The third set of analyses aims to quantify the sensitivity of the isoforcing to the observed driving variables of the model. For example, a doubling of $C_a$ increased the diurnal peak value of $C_a$ (w$^{18}$O) to 681 $\mu$mol m$^{-2}$ s$^{-1}$ %o ($+139\%$), although in terms of isoforcing $w^{18}$O, the increase was minor, from 0.019 to 0.023 $\mu$mol s$^{-1}$ (%o ($+21\%$) (more on this point in section 5.4). Lee et al. [2009] showed that $w^{18}$O, not $C_a$ (w$^{18}$O), is the appropriate flux boundary condition for calculating the atmospheric budget of $^{18}$O-CO$_2$. Additional information on the isoforcing sensitivity can be found in Table 1.

5. Discussion

5.1. Effect of Energy Imbalance on Model Simulations

[40] The lack of energy balance closure in the eddy covariance measurements introduces an important problem in the LSM model validation [Wilson et al., 2002]. Since LSM models are based on the principle of energy budget conservation, optimization against the measured flux time series may lead to erroneous parameters for calculating $LE$, $H$, and $F_{rs}$. For example, by training the parameters $D_{00}$, $a_1$, $b_1$, and $b_2$ to optimize the fit of $LE$, we found that the predicted $H$ was biased high in comparison to the (unadjusted) observed values. This is because to satisfy energy conservation, the model was forced to assign the missing energy to $H$. Assuming that the Bowen ratio, as defined by the eddy covariance measurement of $H$ and $LE$, and the available energy were accurately measured, we trained the LSM model using the adjusted $H$ and $LE$. This method seems logical. Similar conclusions can be found in the study of Aranibar et al. [2006].

Forcing energy balance closure can therefore improve the LSM model performance.

[41] The effect of energy balance closure on the isotopic flux prediction is less straightforward. In comparison to the original model results with forced energy balance closure, the diurnal peak eddy isoforcing, simulated with the LSM model optimized against the unadjusted flux measurement, was $2\%$ lower (Table 1). The apparent small sensitivity was a result of two opposing processes. On the one hand, if the LSM was trained against the original $H$ and $LE$ measurement, the midday (from 1000 to 1500 LST) predicted $H$ increased to an average of 127 W m$^{-2}$ in comparison to the default prediction of 29 W m$^{-2}$, the midday $LE$ decreased to 264 W m$^{-2}$ in comparison to the original 372 W m$^{-2}$, and the midday predicted canopy temperature $T_c$ was on average 301.6 K in comparison to the original 299.9 K, over the simulation period...
period (DOY 195–239). A higher $T_e$ would mean a lower relative humidity RH, and therefore a higher $\delta_{L,b}^v$, $\delta_{L,e}^v$ and $^{18}$O-CO$_2$ isoforcing (Figures 7 and 8). The reduction in $LE$ was linked to a larger canopy resistance, which acted to increase the kinetic factors ($\varepsilon_k^e$ and $\varepsilon_k^w$). Both an increased $\delta_{L,e}^v$ and increased canopy kinetic factors resulted in an increase in the magnitude of terms in the square brackets of equation (A2), and tended to increase the eddy isoforcing. On the other hand, the canopy CO$_2$ flux $F_c$ changed to $-23$ $\mu$mol m$^{-2}$s$^{-1}$ in comparison to the original $-24$ $\mu$mol m$^{-2}$s$^{-1}$. In the daytime, $F_c < 0$ and $C_a - C_e < 0$ because of photosynthesis, a less negative $F_c$ would offset the isoforcing enhancement due to $\delta_{L,e}^v$ and $\varepsilon_k^w$.

5.2. The $^{18}$O-H$_2$O Exchange

Our results suggest that nonsteady effects may be more important than the Péclet effect in controlling $\delta_E^{T_F}$. Optimization of the Farquhar and Cernusak model resulted in a vanishingly small radial diffusion length (equation (B9)) or the Péclet number. In other words, the Dongmann’s approximation that $\delta_{L,e}^v = \delta_{L,b}^v$ was acceptable at the canopy scale in the present study [Dongmann et al., 1974]. The same approximation was also found to give reasonable prediction of $\delta_{L,t}^{eq}$ over a forest ecosystem [Lee et al., 2007]. The negligibly small Péclet effect may be an emergent property at the ecosystem scale. In the physical space of a canopy, transpiration occurs at numerous sites, the leaves, that are dispersed throughout a fragmented media. So true diffusion does not exist at the canopy scale because liquid water molecules cannot move across these isolated transpiration sites.

[42] The accuracy of the SiLSM $^{18}$O-H$_2$O calculations also depends on factors that are external to the $^{18}$O-H$_2$O submodel. For example, we found that the prediction error in $\delta_{L,b}^v$ was correlated with the error in $T_e$ (Figure 11). On most days before DOY 212, $\delta_{L,b}^v$ was underestimated by SiLSM, when $H$ and $T_e$ were underestimated and RH$_t$ was overestimated. From DOY 224 to 234, the simulated $H$ was higher than the observation, and $\delta_{L,b}^v$ was overestimated (Figures 4 and 5).

5.3. Extent of CO$_2$ Hydration

[44] The extent of CO$_2$ hydration ($\theta_{eq}$) in the leaves and the canopy kinetic fractionation ($\varepsilon_k$) were the two most crucial factors controlling the $^{18}$O-CO$_2$ flux according to the sensitivity analysis (Table 1). If turbulence was ignored in the kinetic factors, the simulated eddy isoforcing was much too high in comparison to the observation. But even with accounting for turbulent diffusion, the simulated eddy isoforcing was still biased high (Figures 7 and 8). The sensitivity analysis suggests that the default $\theta_{eq}$ of 0.75 was likely too high. This value was adopted from Gillon and Yakir [2000], who calculated the CO$_2$ hydration extent from in-vitro CA activity and gas exchange by adapting the equation developed by Mills and Urey [1940]. Cousins et al. [2006] showed that $\theta_{eq}$ derived from C$^{18}$O discrimination measurements is sensitive to irradiance. They found that in field conditions, $\theta_{eq}$ of the wild-type Flaveria bidentis changed from 1.06 in low radiation (PAR = 150 $\mu$mol m$^{-2}$ s$^{-1}$) to 0.45 in high radiation (PAR = 2000 $\mu$mol m$^{-2}$ s$^{-1}$). Our analyses also suggest that the extent of CO$_2$ hydration should be much lower for plants growing in field conditions than the value derived from the CA activity and photosynthetic flux measurement: Optimization against the eddy isoforcing observed in midday periods yielded a value of 0.46 for $\theta_{eq}$.

[45] Three alternative explanations exist for the disagreement shown in Figures 7 and 8, but none of them seems plausible. First, the predicted $\delta_{L,b}^v$ may have been biased high. However, forcing a good agreement for the eddy isoforcing would require that the midday $\delta_{L,b}^{eq}$ be 1.6% lower than the observed $\delta_{L,b}^{eq}$ which is an unacceptable result.

[46] Second, the estimate of the soil isoforcing component could be in error because it assumes that soil CO$_2$ was in equilibrium with soil water at a single depth of 10 cm. In reality, soil CO$_2$ flux originates from multiple layers. For example, Jacinthe and Lai [2009] found that around 81% of soil respiration comes from the 0 to 20 cm soil layer in a soybean field and the remaining contributed by deeper soil. Over the period DOY 195 to 239, the 10 cm soil water $\delta_{L,b}^v$ was 1.5 per mil higher than that of the root zone average [Welp et al., 2008]. If the latter value was used for the soil isoforcing calculation, the peak ecosystem isoforcing would be lower by less than 7% (Table 1), and not enough to explain the discrepancy in Figure 8. Furthermore, the discrepancy would be even larger if a value less than 1 were used for $\theta_{eq,s}$ (Table 1 and Figure 10).

[47] The third explanation is related to uncertainties in the isoforcing measurement. The eddy isoforcing data, obtained from the first attempt at measuring the ecosystem-scale isotopic fluxes with eddy covariance, was very noisy (Figure 7). The noise, however, appears to be random. One could suppose that the 31% deficit in the energy budget implies a similar amount of bias of the isoforcing measurement. If an adjustment of this size was made, the disagreement between the model and the observation would largely vanish. However, no mechanisms are known to cause identical biases in the eddy covariance measurement of energy fluxes (sensible and latent heat) and in those of passive scalars such as CO$_2$ and its isotopes [Baldocchi, 2003; Huang et al., 2008]. An
independent estimate of the eddy isoforcing based on the gradient-diffusion theory shows good agreement with the eddy covariance measurement, indicating that a large systematic bias in the latter was unlikely (L. R. Welp et al., manuscript in preparation, 2010). We are, therefore, left with a low hydration efficiency at the most logical explanation for the disagreement shown in Figures 7 and 8.

5.4. Implication of Elevated CO₂ Concentration, Humidity, and Temperature

[48] In the interest of understanding how the isoforcing may change in a future CO₂-enriched world, the sensitivity test with CO₂ concentration deserves additional scrutiny. The results show that the isoforcing \( w^\delta \) is moderately sensitive to CO₂, increasing by 19% in response to a doubling of the observed CO₂ level. In CO₂-enriched conditions, plants tend to increase their photosynthesis and reduced transpiration via increasing the stomatal resistance [Anderson et al., 2001; Drake et al., 1997; Long et al., 2004; Maherali et al., 2002, 2003]. In our 2 \( \times \) CO₂ sensitivity test, the magnitude of the canopy CO₂ flux \( (F_c) \) increased by 17% (from \(-24\) to \(-28\) \( \mu \)mol m\(^{-2}\) s\(^{-1}\)), mean values for periods 1000 to 1500 LST), \( LE \) decreased by 19% (from 372 to 300 W m\(^{-2}\)) and the stomatal resistance \( (r_s^w) \) increased by 94% (from 1.05 to 2.04 m\(^{-1}\)) s\(^{-1}\)). The small change in isoforcing \( w^\delta \) was a result of several opposing mechanisms. The increase of \( r_s^w \) and reduction of \( r_a^w \) (due to air being more unstable) increased the kinetic fractionation factor for \( ^{18}O-H_2O \) \( \varepsilon_k^w \) by 5.4\%o, \( \delta_{L,e}^{C_16/C_17} \) by 2.9\%o and the kinetic factor for \( ^{18}O-CO_2 \) \( \varepsilon_i^w \) by 1.3\%o, in the midday periods, all acting to increase the canopy isoforcing according to equation (A2). Similarly, the increase in \( F_c \) magnitude should also enhance the isoforcing. However, increased \( C_C \) had the opposite effect, acting to reduce the isoforcing through a reduction in the magnitude of the concentration ratio \( C_C/(C_C - C_s) \) in equation (A2).

[49] The isotopic fractionation processes may also respond to increasing atmospheric humidity. Our observational and modeling results show that relative humidity was an important driver on the short-term (hourly) variations in the \( ^{18}O-CO_2 \) isoforcing (Figure 10). The model sensitivity analysis revealed that a 2\% absolute change in the air relative humidity (RH) would cause a 15% reduction in the daytime peak isoforcing (Table 1), primarily through the reduction in \( \delta_{L,b}^w \) (by 1.3\%o). The \( \delta_{L,b}^s \) sensitivity (−0.7 per mil change per 1\% absolute increase in air relative humidity) was higher than the Craig-Gordon model prediction [Still et al., 2009] in part because of the reduction in canopy temperature in high-humidity conditions, which further amplified the humidity effect on \( \delta_{L,b}^s \). The significant negative correlation between RH and \( \delta_{L,b}^s \) have been reported in the literature [Welp et al., 2008]. Some of the humidity effect may be offset by the concurrent rise in air temperature although the temperature sensitivity appears very small (Table 1). It is not known whether the documented rise in humidity [Willett et al., 2007; Santer et al., 2007; Dai, 2006] can cause a measureable reduction in the global mean \( ^{18}O \) composition of atmospheric CO₂.

6. Conclusions

[50] The diagnostic analysis using SiLSM suggests that the Péclet effect played a much less important role than the nonsteady effect on the \( ^{18}O-H_2O \) exchange in the soybean ecosystem. In the LSM modeling framework, the accuracy of the prediction of the foliage \( ^{18}O-H_2O \) enrichment depended critically on the accuracy of the canopy temperature calculations and on the proper handling of turbulent diffusion in the kinetic fractionation process.

[51] The modeled results demonstrate that in agreement with the observation, relative humidity exerted a large influence on the short-term (hourly) \( ^{18}O-CO_2 \) exchange between the ecosystem and the atmosphere. The SiLSM prediction of the \( ^{18}O-CO_2 \) isoforcing was 49% higher than the observed midday mean value. Forcing agreement of the predicted with the observed isoforcing yielded a value of 0.46 for \( \theta_{eq} \), suggesting a low hydration efficiency in the leaves of soybean in field conditions.

[52] Atmospheric humidity is likely to increase in a future CO₂-enriched world. Our model sensitivity analysis revealed that a 2\% absolute change in the air relative humidity would cause a 15% reduction in the daytime peak isoforcing. Some of the humidity effect may be offset by the effect of the rise in CO₂. It is not known whether the documented rise in humidity [Willett et al., 2007; Santer et al., 2007; Dai, 2006] can cause a measureable reduction in the global mean \( ^{18}O \) composition of atmospheric CO₂.

Appendix A: Big-Leaf Parameterization for \( ^{18}O-CO_2 \) Isoforcing

[53] Lee et al. [2009] showed that the covariance between the vertical velocity and isotope composition in delta notation (\( w^\delta \)) is the eddy flux of \( \delta \). Physically, this covariance term represents the surface boundary condition for the atmospheric budget of \( \delta \) and can be parameterized through the big-leaf analogy. The total covariance consists of a canopy (\( w^\delta \)) and a soil (\( w^\delta_s \)) component.

\[
\langle w^\delta \rangle = \langle w^\delta \rangle_c + \langle w^\delta \rangle_s
\]  
(A1)

\[
\langle w^\delta \rangle_c = \frac{F_c}{C_a} \left[ \frac{C_s}{C_s - C_a} \left( \delta_{L,e}^s - \delta_{eq}^s \right) + (1 - \theta_{eq}) \varepsilon_k^s \frac{C_c}{C_a} - \varepsilon_k^s \right]
\]  
(A2)

\[
\langle w^\delta \rangle_s = \frac{F_s}{C_a} \left[ \frac{C_s}{C_s - C_a} \left( \delta_{L,b}^s - \delta_{eq,s}^s \right) + (1 - \theta_{eq,s}) \varepsilon_x^s \frac{C_c}{C_a} - \varepsilon_x^s \right]
\]  
(A3)

where \( F_c \) and \( F_s \) are the canopy and soil components of the net ecosystem CO₂ exchange calculated by the LSM model, \( \delta_{L,e}^s \) is the \( ^{18}O-CO_2 \) composition of the ambient air, \( \delta_{L,b}^s \) and \( \delta_{eq,s}^s \) are \( ^{18}O \) compositions of CO₂ in the stomatal cavity and the soil pore space and in full equilibrium with the leaf and soil laminar water, respectively, \( \varepsilon_k^s \) and \( \varepsilon_x^s \) are canopy and soil kinetic fractionation factors for \( ^{18}O-CO_2 \). The CO₂ hydration extent in the leaves (\( \theta_{eq} \)) was assigned a value of 0.75 for the soybean ecosystem [Gilton and Yakir, 2000], and that in the soil (\( \theta_{eq,s} \)) was set to 1. In the present study, the simulated average daytime minimum \( C_s \) was 1.3 \( \times \) \( 10^4 \) \( \mu \)mol m\(^{-3}\) (296 ppm), \( C_c \) was 1.1 \( \times \) \( 10^4 \) \( \mu \)mol m\(^{-3}\) (269 ppm) and \( C_s \)
was 2.4 × 10^4 μmol m^{-3} (567 ppm) and the observed daytime minimum \( C_n \) at the reference height was 1.5 × 10^3 μmol m^{-3} (357 ppm).

[54] The CO₂ concentration in the chloroplasts of the leaves \( (C_c) \) and soil air \( (C_s) \) are calculated from

\[
C_c = C_a + F_c (r_a + r_f + r_{es} + r_m) \quad (A4)
\]

\[
C_s = C_a + F_s (r_a + r_{ac} + r_{soil}) \quad (A5)
\]

where \( C_a \) is the atmospheric CO₂ concentration, \( r_a \) and \( r_{ac} \) are aerodynamic resistance from canopy top to the reference height and that from soil surface to canopy top, \( r_f, r_m, r_{es} \) and \( r_{soil} \) are canopy-scale boundary layer, mesophyll, stomatal and soil resistances to CO₂.

[55] According to [Brenninkmeijer et al., 1983], \( \delta_{L,c} \) and \( \delta_{c} \) are given by

\[
\delta_{L,c} = \delta_{c} + \frac{17604}{T_c} - 17.93 \quad (A6)
\]

\[
\delta_{c} = \delta_{a} + \frac{17604}{T_c} - 17.93 \quad (A7)
\]

where \( \delta_{L,c} \) and \( \delta_c \) are ¹⁸O-H₂O composition at the evaporating site in the leaf and that in the soil at the 10 cm depth, respectively, \( T_a \) and \( T_c \) are soil temperature at 10 cm depth and canopy temperature.

[56] The canopy kinetic fractionation factor for ¹⁸O-CO₂ \( \varepsilon_k \) are given by

\[
\varepsilon_k = \frac{5.8r_f + 8.8r_c + 0.8r_m}{r_a + r_f + r_c + r_m} (\%o) \quad (A8)
\]

where the coefficient 0.8 represents the mesophyll fractionation factor [Farquhar and Lloyd, 1993].

[57] The soil kinetic fractionation factor for ¹⁸O-CO₂ \( \varepsilon_{k,s} \) is given by

\[
\varepsilon_{k,s} = \frac{8.8r_{soil}}{r_a + r_{ac} + r_{soil}} (\%o) \quad (A9)
\]

Appendix B: Equations for Nonsteady State ¹⁸O-H₂O Composition of Leaf Water

[58] Accounting for the change in the water content and the Péclet effect, Farquhar and Cernusak [2005] describe the ¹⁸O-H₂O at the evaporating site in the nonsteady state \( \delta_{L,es} \) as

\[
\delta_{L,es} = \delta_{es} - \alpha_{es} \alpha_{w} \frac{W}{w_j} \cdot \frac{d}{dt} \left( \frac{\delta_{L,es} - \delta_{s}}{\delta_{s}} \right) \quad (B1)
\]

where \( r_w \) is the canopy resistance to diffusion of water vapor to the atmosphere from the sites of evaporation within the leaf including stomata resistance \( r_a \) and boundary layer resistance \( r_f \) in series, \( \delta_{s} \) is ¹⁸O-H₂O composition of xylem water, and \( t \) is time. The equilibrium fractionation factor \( \alpha_{eq} \) (1) is given by Majoube [1971], and

\[
\varepsilon_{eq} = \left( 1 - \frac{1}{\alpha_{eq}} \right) \times 1000 (\%o) \quad (B2)
\]

[59] The kinetic fractionation factor for water vapor diffusion \( \alpha_{k}^{w} \) (1) is calculated as,

\[
\alpha_{k}^{w} = 1 + \frac{\varepsilon_{k}^{w}}{1000} \quad (B3)
\]

\[
\varepsilon_{k}^{w} = \frac{21r_{es}^{w} + 32r_{soil}^{w}}{r_a + r_{ac} + r_{soil}} (\%o \%o) \quad (B4)
\]

[60] The water content in the foliage, \( W \) is expressed as mass of water per unit ground area (g m⁻²). In the paper of Farquhar and Cernusak [2005], equation (B1) is based on the principle of ¹⁸O-H₂O mass conservation of leaf water. Here we applied it to the canopy scale. To be consistent with the canopy scale application, \( W \) is computed as the product of LAI and the leaf water content measured in the field. The Péclet number \( P \) is related to transpiration rate \( (E) \) via:

\[
P = \frac{EL_{eff}}{CD} \quad (B5)
\]

where \( C \) is the density of liquid water \( (55.5 \times 10^3 \text{ mol m}^{-3}) \), \( D \) is the diffusivity of ¹⁸O-H₂O in water depending on temperature [Cuntz et al., 2007], \( L_{eff} \) is the scaled effective "radial" length from the evaporative site.

[61] In equation (B1), \( \delta_{L,es} \) is the isotopic enrichment of water at the evaporating site in steady state,

\[
\delta_{L,es} = (R_{es}/R_{VSMOW}) - 1 \times 1000 (\%o) \quad (B6)
\]

\[
R_{es} \frac{R_c}{R_s} = \alpha_{eq} \left[ \alpha_{k}^{w} (1 - RH_i) + RH_i \frac{R_c}{R_s} \right] \quad (B7)
\]

where \( R_{es}, R_c \) and \( R_s \) are ¹⁸O/¹⁶O in ambient vapor, xylem water and leaf water at the evaporative site in steady state, respectively, \( RH_i \) is relative humidity in fraction in reference to the canopy temperature, and \( R_{VSMOW} \) is the standard ¹⁸O/¹⁶O ratio of the Vienna Standard Mean Ocean Water (VSMOW).

[62] In this paper, \( \delta_{L,es}^{w} \) was used to determine the isotope exchange between CO₂ and H₂O. However, \( \delta_{L,es}^{w} \) is not directly observable. For the purpose of model verification, the predicted ¹⁸O-H₂O composition of evapotranspiration \( \delta_{ET}^{w} \) and of the bulk leaf water \( \delta_{L,b}^{w} \) were compared with the measurements. Here, \( \delta_{ET}^{w} \) and \( \delta_{L,b}^{w} \) were calculated according to the departure from steady state as

\[
\delta_{ET}^{w} = \delta_{L,es}^{w} - \alpha_{k}^{w} \frac{W}{w_j} + \delta_{s} \quad (B8)
\]
and
\[
\delta_{L,b}^w = \delta_{L,b}^w - \frac{\alpha L \alpha \rho p \rho}{W}, \frac{1 - e^{-\rho}}{P}, \frac{d}{dt} \left( W \cdot \left( \delta_{L,b}^w - \delta_{L,b}^w \right) \right)
\] (B9)

where \( \delta_{L,b}^w \) is \(^{18}\)O-H\(_2\)O of bulk leaf water in steady state and calculated from \( \delta_{L,c}^w \) and \( P \) as
\[
\delta_{L,b}^w = \frac{\delta_{L,c}^w (1 - e^{-\rho})}{P}
\] (B10)

Equations (B1) and (B9) were solved iteratively by finding a zero difference between the left and right-hand sides of each equation. Usually 30 to 40 steps of iteration were needed for each time step of SiLSM to reach a preset zero threshold.

Dew events were considered explicitly because of their frequent occurrence (around 80% of nights) [Welp et al., 2008]. In our model, \( r_{c}^w \) was set to zero during dew events, and the \(^{18}\)O-H\(_2\)O compositions of the leaf water at the site of evaporation (\( \delta_{L,c}^w \)) and evapotranspiration water (\( \delta_{ET}^w \)) were assumed to equilibrate with that of water vapor in ambient air (\( \delta_{a}^w \)) as
\[
\delta_{ET}^w = \delta_{a}^w + \varepsilon_{eq}^w
\] (B11)
\[
\delta_{L,c}^w = \delta_{a}^w + \varepsilon_{eq}^w
\] (B12)

Appendix C: Big-Leaf Land Surface Model

C1. Water, Heat, and CO\(_2\) Fluxes

In the LSM the bulk exchange relation is used to calculate the sensible and latent heat flux densities [Beljaars and Holtslag, 1991], in conjunction with the energy budget equation
\[
(1 - \alpha)R_S + \varepsilon R_L - \varepsilon \sigma T_a^4 = H + LE + G
\] (C1)

where \( R_S \) and \( R_L \) are incoming short-wave and long-wave radiation flux, \( H \) is sensible heat flux, \( LE \) is latent heat flux, \( G \) is soil heat flux, \( \varepsilon \) is surface emissivity, \( \alpha \) is canopy surface albedo, \( \sigma \) is the Stefan-Boltzmann constant and \( T_a \) is canopy surface or skin temperature. The sensible and latent heat fluxes are given by
\[
H = \frac{\rho_a c_p (T_a - T_d)}{r_a}
\] (C2)
\[
LE = \frac{\rho_a \lambda}{r_a} \frac{q_a - q_d}{r_a + r_d^w}
\] (C3)

where \( \rho_a \) is air density, \( c_p \) is isobaric specific heat, \( T_d \) is air temperature at reference height, \( \lambda \) is latent heat of vaporization, \( q_a(T_a) \) is saturation specific humidity at canopy surface, \( q_d \) is specific humidity at reference height. Canopy temperature (\( T_a \)) is solved from a linearized form of equation (C1).

The canopy CO\(_2\) flux is calculated as
\[
F_c = \frac{C_i - C_a}{r_a + r_d^w + r_b^w}
\] (C4)

To get the stomatal resistances \( r_c^w \) and \( r_b^w \), an analytic formulation based on radiation transfer within the canopy is used to upscale the leaf stomatal conductance \( g_l^e \) to the canopy conductance \( g_l^e \) [Ronda et al., 2001].

At leaf scale, the stomatal conductance is solved from the plant physiological approach as
\[
g_l^e = \frac{g_{min,c} + \frac{a_1 A_g}{(C_l - \Gamma) \left( 1 + \frac{b_1}{A_g} \right)}}{A_m + A_{m,max}}
\] (C5)

where \( A_g \) is the gross assimilation rate, \( g_{min,e} \) is the cuticular conductance, \( C_l \) is the CO\(_2\) concentration at the leaf surface, \( D_o \) is the vapor pressure deficit at plant level, \( a_1 \) and \( A_m \) are empirical parameters.

The gross assimilation rate is computed as a function of \( T_c \), photosynthetically active radiation (PAR) and the intercellular CO\(_2\) concentration \( (C) \) [Jacobs, 1994].
\[
A_g = (A_m + R_d) \left\{ 1 - e^{-[\alpha PAR/(A_m + R_d)]} \right\}
\] (C6)

with
\[
A_m = A_{m,max} \left\{ 1 - e^{-[g_a(C_l - \Gamma)/A_{max}]^2} \right\}
\] (C7)

The dark respiration \( R_d \) is calculated as
\[
R_d = 0.11 A_m
\] (C8)

The effect of soil moisture on net photosynthesis and canopy conductance is accounted for by relating the gross assimilation rate to soil moisture in the root zone so that the water-stressed gross assimilation rate is expressed as
\[
A_g = A_g^* f(\theta)
\] (C9)

where \( A_g^* \) is the unstressed rate, and \( f(\theta) \) is a function of soil moisture (see below).

C2. Resistance Terms

The canopy-scale stomatal resistance to CO\(_2\) \( r_c^w \) is the inverse of \( g_l^e \), and the stomatal resistance to H\(_2\)O \( r_b^w \) is calculated from
\[
r_b^w = r_c^w / 1.6
\] (C10)
[73] The canopy-scale mesophyll resistance to CO$_2$ $r_m^w$ is calculated as

$$r_m^w = 1/(g_{eq} \times LAI)$$  \hspace{1cm} (C11)

[74] The canopy-scale boundary layer resistance to H$_2$O $r_b^w$, aerodynamic resistance $r_a$, and the aerodynamic resistance from the soil surface to the canopy top $r_{as,c}$ are computed using the methods described by Lee et al. [2009].

[75] Soil resistance for H$_2$O is calculated from soil moisture [Sellers et al., 1992],

$$r_{soil}^w = \exp(8.206 - 4.225 \times \theta) \text{ (s m}^{-1})$$  \hspace{1cm} (C12)

[76] The resistance terms to CO$_2$ are given by

$$r_{soil}^r = 1.6r_{soil}^w$$  \hspace{1cm} (C13)

$$r_b^r = 1.4r_b^w$$  \hspace{1cm} (C14)

C3. Major Changes to the Big-Leaf LSM

[77] Three important changes are made to the big-leaf LSM. First, a logistic expression for the soil moisture effect is used instead of the original quadratic one since our optimization analyses show that the original formulation does not work well under very dry soil conditions.

$$f(\theta) = 1/(1 + \exp(-b_1 - b_2 \beta(\theta)))$$  \hspace{1cm} (C15)

with $\beta(\theta)$ given by

$$\beta(\theta) = \max \left[ 0, \min \left( 1, \frac{\theta - WP}{FC - WP} \right) \right]$$  \hspace{1cm} (C16)

where $FC$ and $WP$ are the soil moisture content at field capacity and at permanent wilting point, respectively, and $b_1$ and $b_2$ are empirical coefficients determined in the above analysis. The soil moisture content at 10 cm depth ($\theta$) is expressed as a volume fraction.

[78] Second, the original LSM does not consider soil respiration ($F_s$). Here, $F_s$ is expressed as a function of soil temperature measured at 10 cm depth ($T_s$) according to the total nighttime ecosystem respiration measured with eddy covariance,

$$F_s = (-0.19 \exp(0.003(T_s - 273.15))) \times 0.81$$  \hspace{1cm} (C17)

where the factor 0.81 acknowledges that 81% of ecosystem respiration is soil respiration according to the soil chamber and eddy covariance observations for the soybean field [Bavin et al., 2009].

[79] The original LSM does not consider dew formation. At this site, dew was a common phenomenon at night. We consider dew formation in the evening and the subsequent evaporation of the dew water in the morning in the energy budget calculation. The dew formation routine is activated whenever the dew point of canopy air exceeded the surface skin temperature. When a dew event occurs, the stomatal resistance to H$_2$O ($r_d^w$) is set to zero in the energy budget calculation. Dew forms at the rate of water vapor flux determined from the energy budget calculation. Once RH$_L$ reduces to a value lower than 1, the dew water would evaporate at the rate of the predicted water vapor flux. Leaf transpiration would turn on after all the dew that formed in the previous evening had evaporated.

Notation

- $^1$O CO$_2$.
- $^2$H$_2$O.
- $\alpha$ albedo, dimensionless.
- $\alpha$ light use efficiency, mg J$^{-1}$.
- $\alpha_{eq}$ equilibrium fractionation factor for water (>1), dimensionless.
- $\alpha_{ke}$ kinetic fractionation factor for water vapor (>1), dimensionless.
- $\Gamma$ CO$_2$ compensation point, mg m$^{-3}$.
- $\delta_{LO}$ $^18$O-CO$_2$ of air at height $z_m$, %.
- $\delta_{LS}$ $^18$O-CO$_2$ of soil air, %.
- $\delta_{L,e}$ $^18$O-CO$_2$ in equilibrium with water at leaf evaporative site, %.
- $\delta_{L,sa}$ $^18$O-H$_2$O of water vapor at reference height $z_m$, %.
- $\delta_{L,sa}$ $^18$O-H$_2$O of bulk leaf water, %.
- $\delta_{L,bs}$ steady state value of $\delta_{L,sa}$, %.
- $\delta_{L,le}$ $^18$O-H$_2$O at evaporative site in leaf, %.
- $\delta_{L,es}$ steady state values of $\delta_{L,le}$, %.
- $\delta_{L,ea}$ $^18$O-H$_2$O of soil water, %.
- $\delta_{L,ea}$ $^18$O-H$_2$O of xylem water, %.
- $\varepsilon_k$ canopy kinetic fractionation factor for $^18$O-CO$_2$, %.
- $\varepsilon_{ke}$ soil kinetic fractionation factor for $^18$O-CO$_2$, %.
- $\varepsilon_{eq}$ equilibrium $^18$O fractionation between liquid water and vapor, %.
- $\varepsilon_k$ canopy kinetic fractionation factor for $^18$O-H$_2$O, %.
- $\theta$ volumetric soil moisture content at 10 cm depth.
- $\theta$ extent of CO$_2$ hydration in leaves, equal to 0.75.
- $\theta$ extent of CO$_2$ hydration in soil, equal to 1.
- $\theta_{eq}$ whole-ecosystem (kinematic) isoforcing, % m s$^{-1}$.
- $C_a (w^\theta)$ ecosystem eddy $^18$O-CO$_2$ isoforcing, \( \mu \text{mol} \text{ m}^{-2} \text{ s}^{-1} \) %.
- $A_g$ gross assimilation rate, mg m$^{-2}$ s$^{-1}$.
- $A_m$ primary productivity, mg m$^{-2}$ s$^{-1}$.
- $a_1$ empirical coefficient in the canopy resistance model, equal to 16.2.
- $b_1$ empirical coefficient for soil moisture stress, equal to $-5.8$ for $\theta \leq 0.21$, $-1.5$ for $\theta > 0.21$.
- $b_2$ empirical coefficient for soil moisture stress, equal to $-0.249$ for $\theta \leq 0.21$, $0.5$ for $\theta > 0.21$.
- $C$ molar concentration of water, equal to $55.5 \times 10^3$ mol m$^{-3}$.
- $C_a$ CO$_2$ molar concentration of the air at height $z_m$, \( \mu \text{mol} \text{ m}^{-3} \).
- $C_c$ CO$_2$ molar concentration in leaf chloroplasts, \( \mu \text{mol} \text{ m}^{-3} \).
$C_i$ CO$_2$ molar concentration in the intercellular space, $\mu$mol m$^{-2}$.

$C_l$ CO$_2$ concentration at the leaf surface, $\mu$mol m$^{-3}$.

$C_s$ CO$_2$ molar concentration in soil air, $\mu$mol m$^{-3}$.

$D$ diffusivity of $^{18}$O-H$_2$O in water, m$^2$ s$^{-1}$.

$D_v$ vapor pressure deficit constant, equal to 0.44 kPa.

$D_s$ vapor pressure deficit at plant level, kPa.

$E$ transpiration rate, mol m$^{-2}$ s$^{-1}$.

$FC$ volumetric soil moisture content at field capacity, equal to 0.36.

$F_c$ canopy CO$_2$ flux, $\mu$mol m$^{-2}$ s$^{-1}$.

$F_N$ net ecosystem CO$_2$ flux, $\mu$mol m$^{-2}$ s$^{-1}$.

$g'_c$ canopy-scale stomatal conductance, m s$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$g'_l$ leaf-scale stomatal conductance, m s$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$g'_m$ leaf-scale mesophyll conductance, m s$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$g'_{min}$ leaf-scale cuticular conductance for CO$_2$, m s$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$h$ canopy height, m.

$H$ sensible heat flux density, W m$^{-2}$.

$L_e$ scaled effective "radial" length, m.

$LE$ latent heat flux, W m$^{-2}$.

$P$ Péclet number, dimensionless.

$q_a$ specific humidity at reference height $z_{ref}$ g g$^{-1}$.

$q^*(T_c)$ saturation specific humidity at canopy temperature, g g$^{-1}$.

$r_a$ aerodynamic resistance in the surface layer, s m$^{-1}$ or m$^2$ s$^{-1}$.

$r_{a,c}$ aerodynamic resistance in the canopy air layer, s m$^{-1}$ or m$^2$ s$^{-1}$.

$r_b$ canopy-scale boundary layer resistance, s m$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$r'_m$ canopy-scale mesophyll resistance to CO$_2$, s m$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$r_r$ canopy-scale stomatal resistance, s m$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$r_{soil}$ soil resistance, s m$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$r'_c$ canopy-scale total resistance to water vapor and heat from canopy surface to reference height, s m$^{-1}$ or mol m$^{-2}$ s$^{-1}$.

$R_{es}$ $^{18}$O/16O in leaf water at the evaporative site in steady state, dimensionless.

$R_v$ $^{18}$O/16O of water vapor in ambient air, dimensionless.

$R_x$ $^{18}$O/16O of xylem water, dimensionless.

$R_L$ incoming longwave radiation flux density, W m$^{-2}$.

$R_S$ incoming shortwave radiation flux density, W m$^{-2}$.

$R_H$ relative humidity of the ambient air reference to $T_a$ (fraction).

$T_a$ air temperature at the reference level, K.

$T_c$ canopy temperature, K.

$T_s$ soil temperature at 10 cm depth, K.

$w_l$ mole fraction of (light) water vapor in the intercellular spaces, mol mol$^{-1}$.

$W$ leaf water content (mass of water per unit ground area at the canopy scale), g m$^{-2}$.

WP volumetric soil moisture content at permanent wilting point, equal to 0.18.

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