



Satellite-Based Modeling of Evapotranspiration and Uncertainties in Eddy Covariance Flux

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Outline

I: Satellite-based Modeling of ET at Fine and Large Scales

- 1. How does the satellite work for ET estimate?**
- 2. What is the Performance of this modeling at field scale?**

II: Uncertainty in Eddy Covariance Measurements

- 1. Flux spatial context vs. Sensor Heights**
- 2. High frequency flux loss vs. Sensor Heights**
- 3. Low frequency flux loss vs. Sensor Heights**
- 4. WPL corrections for CO₂ and N₂O Flux**
- 5. Trace gas analyzer's requirements for EC**

Satellite's Approach

Satellite-Based Land Surface Energy Balance:

Thermal images approach T_R for a simple or complicated relation of T_R vs. T_{AC} .

Visible and infrared images are responsible for the surface radiances, NDVI, LAI, albedo, biomass, and other biophysical variables.

Models for Large Scales:

1. One-source model

- a) Surface energy balance algorithm for land (SEBAL, Bastiaanssen, et al 1998).
- b) Surface energy balance system (SEBS, Su, 2003)
- c) Mapping evapotranspiration with internalized calibration (METRIC, Allen, et al., 2007).

2. Two-source model

- a) Two-source model (TSM, Norman et al., 1995).
- b) Two-source time-integrated model (TSTIM, Andersen et al, 1997 & 2007).

How does Satellite Information do for ET ?

Satellite-Based Land Surface Energy Balance:

--- Thermal images provide T_R Information.

--- Visible and infrared images are used for calculating:

- ❖ Spectral radiances,
- ❖ Spectral reflectance and transmittance,
- ❖ NDVI, LAI, albedo, biomass, and
- ❖ Other biophysical variables.

Sensible Heat Flux:

$$H = \rho C_p \frac{T_{AC} - T_A}{R_A}$$

Aerodynamic and Radiometric Temperatures:

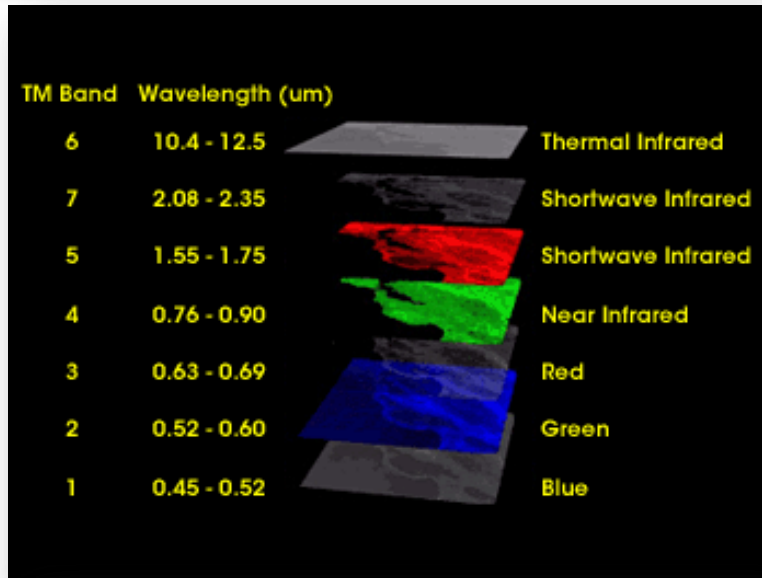
$$T_{AC} \propto T_R$$

Inputs: Landsat 5/7 and Weather Station/EC Tower

Discontinuous
Spatial Info



Continuous
Temporal Info



- ❖ All TM bands
- ❖ Calibrated pixel value [DN]
- ❖ Resampled thermal band

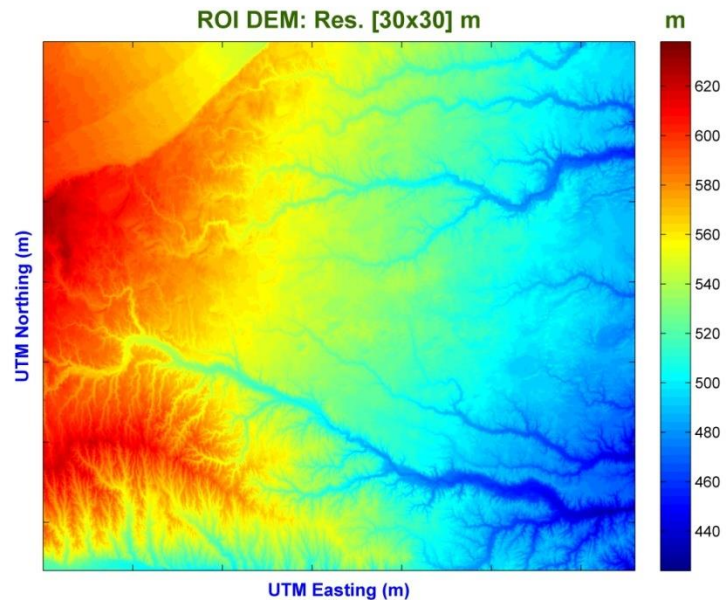
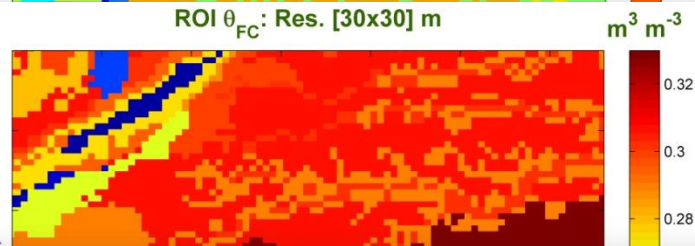
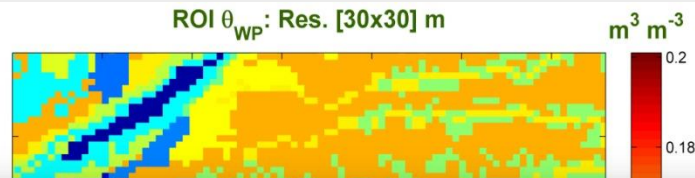
Spatial Resolution: 30x30m



- ❖ Air Temp, Air humidity
- ❖ Solar radiation, Precip.
- ❖ Wind speed and DIR

Temporal Resolution: 1 Hour

Inputs: Static Land Surface Data



Estimate initial surface
soil water balance

adjust Zom – Very effective

- 1) adjust solar radiation
- 2) adjust Zom

Basic Computations

Spectral Radiances

$$L_{\lambda} = G_{\text{rescale}} Q_{\text{cal}} + B_{\text{rescale}}$$

$$\rho_p = \frac{\pi \cdot L_{\lambda} \cdot d^2}{ESUN_{\lambda} \cdot \cos \theta_s}$$

---Chander et al. 2009.

Surface Scalar Quantities

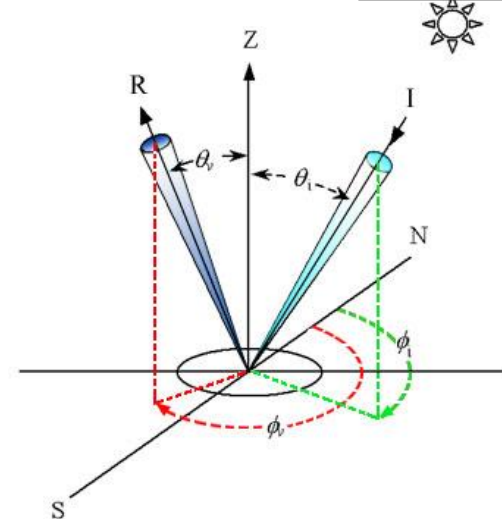
$$T_R = \frac{K_2}{\ln \left(\frac{\epsilon_{NB} K_1}{R_c} \right) + 1}$$

$$NDVI = \frac{\rho_{(x,y,4)} - \rho_{(x,y,3)}}{\rho_{(x,y,4)} + \rho_{(x,y,3)}}$$

$$\alpha = \int_{b=1}^7 \rho_{s,b} w_b db$$

---Allen et al. 2007.

Sun, Satellite and Earth



Surface Available Energy

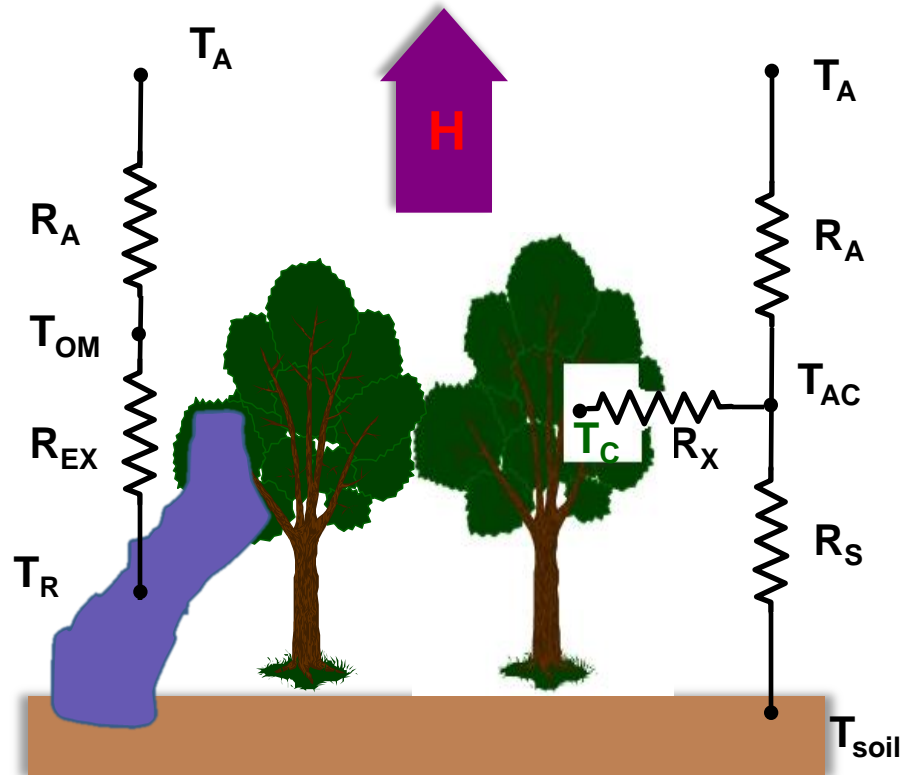
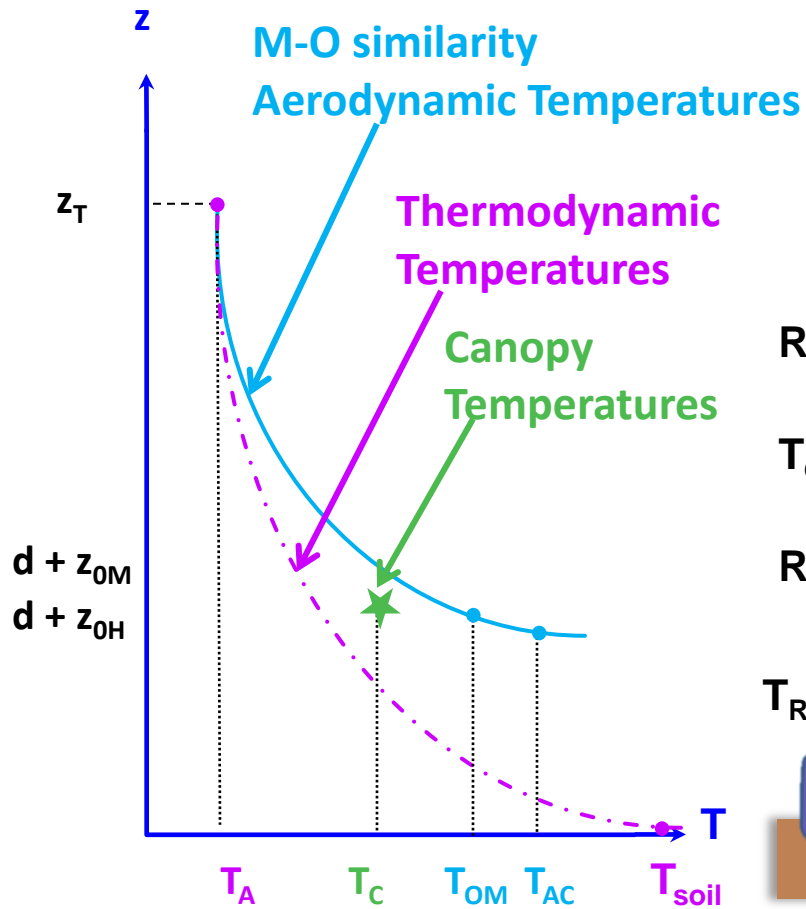
$$R_n = (1 - \alpha) R_s \downarrow + \epsilon_a \sigma T_a^4 - (1 - \epsilon_s) \epsilon_a \sigma T_a^4 - \epsilon_s \sigma T_s^4$$

$$\frac{G}{R_n} = (T_R - 273.15)(0.0038 + 0.0074\alpha - 0.98NDVI^4)$$

---Bastananssen et al. 2000.

Key Computations in Modeling

$$ET = (R_n - G) - H$$



$$R_{EX} = \left[\sum_{i=1}^6 a_i LAI^i \right] u_*^{-1}$$

Iterative Estimate of Sensible Heat

$$R_A = \frac{[\ln(\frac{z_U - d}{z_{OM}} - \psi_M)][\ln(\frac{z_T - d}{z_{OM}} - \psi_H)]}{k^2 U}$$

$$R_X = \frac{180}{LAI} \left(\frac{L_w}{U_{d+z_{OM}}} \right)^{0.5}$$

$$R_S = \frac{1}{a(T_S - T_C)^{\frac{1}{3}} + bU_S}$$

$$T_R = f_c(\varphi)T_C + (1 - f_c(\varphi))T_S$$

$$H_C = \rho C_p \frac{T_C - T_{AC}}{R_X}$$

$$H_S = \rho C_p \frac{T_S - T_{AC}}{R_S}$$

$$H = H_C + H_S = \rho C_p \frac{T_R - T_A}{R_A + R_{EX}}$$

$$ET = (R_n - G) - H$$

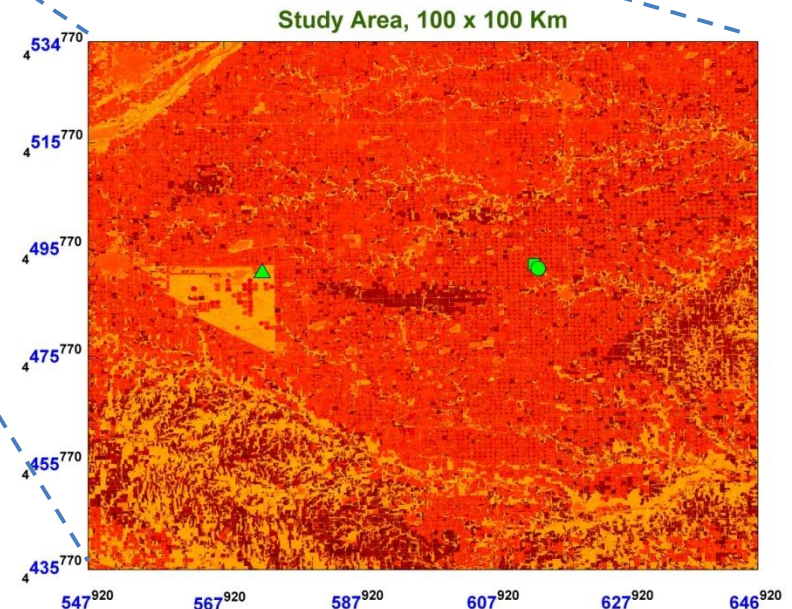
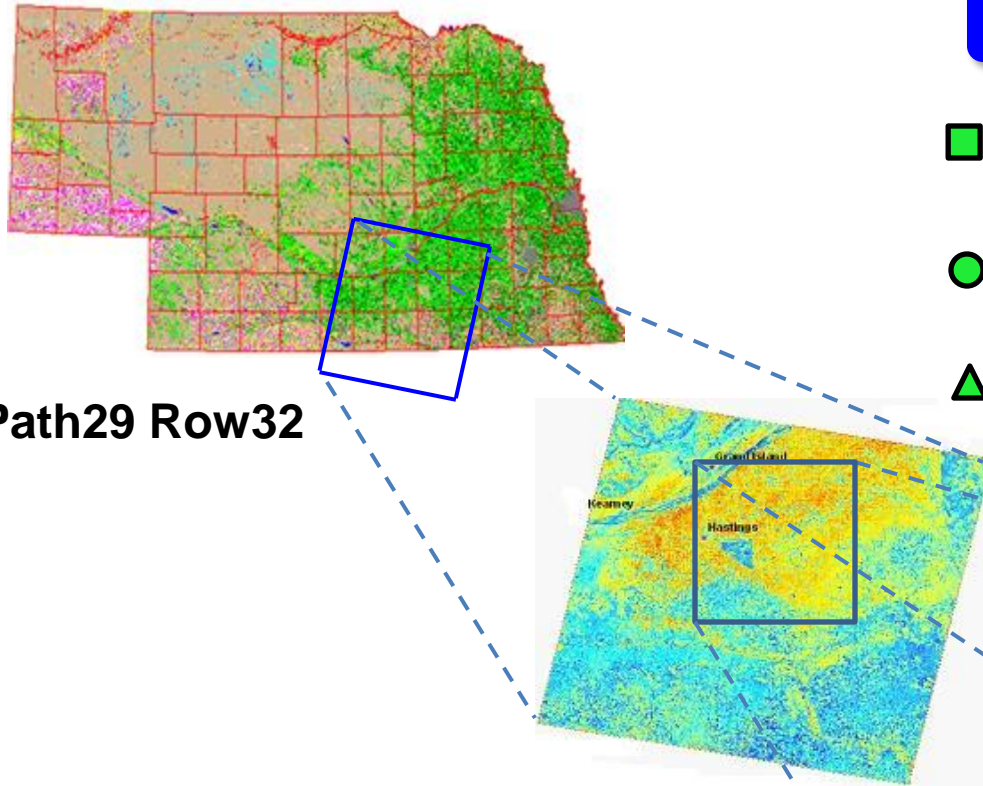
Study Area

- No till corn field, Bowen ratio tower
Lat. 40.5801°, Lon. -97.6552°, Ele: 573.6 m
- Disk till corn field, Bowen ratio tower
Lat. 40.5729°, Lon. -97.6481°, Ele: 576.0 m
- ▲ Weather Station
Lat. 40.570°, Lon. -98.13°, Ele: 552.0 m

Path29 Row32

Landsat 5 Three Scenes:

- ❖ July 01 2009, 17:01:11 (GMT)
- ❖ July 17 2009, 17:01:27
- ❖ Aug. 02 2009, 17:01:42



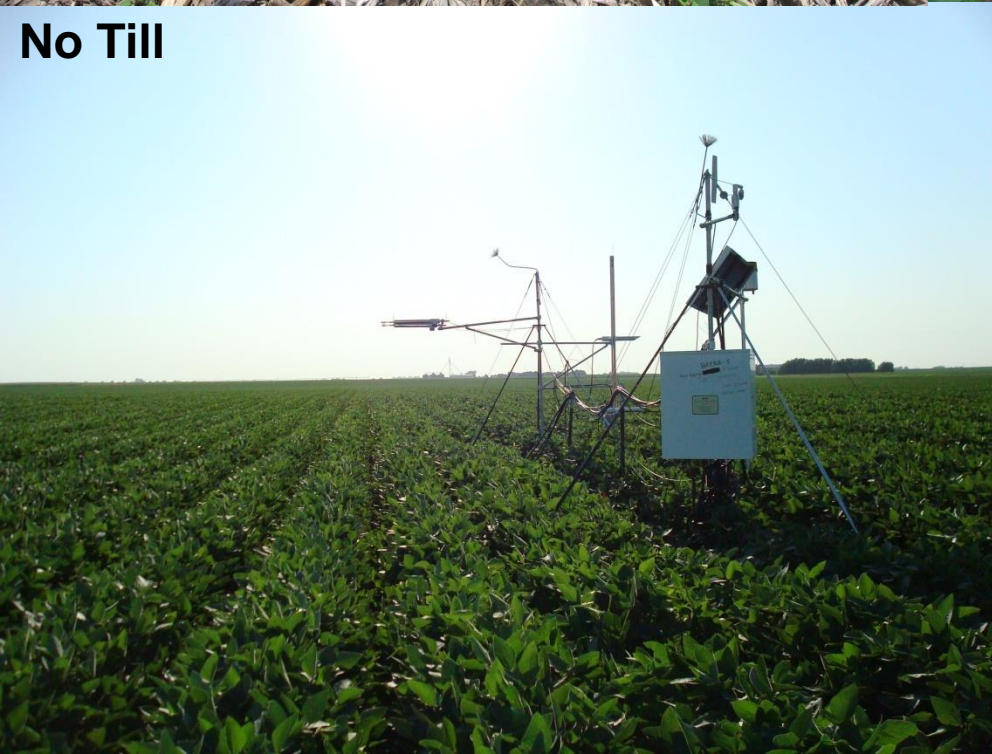
Close-up of Tower Locations

1 miles



2 miles

No Till

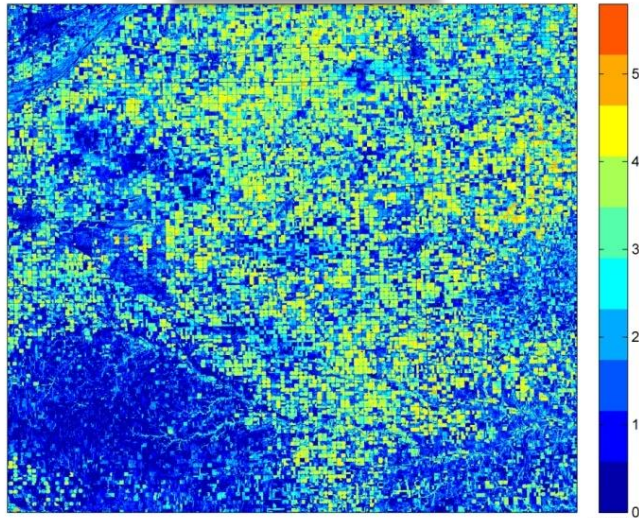


Disk Till

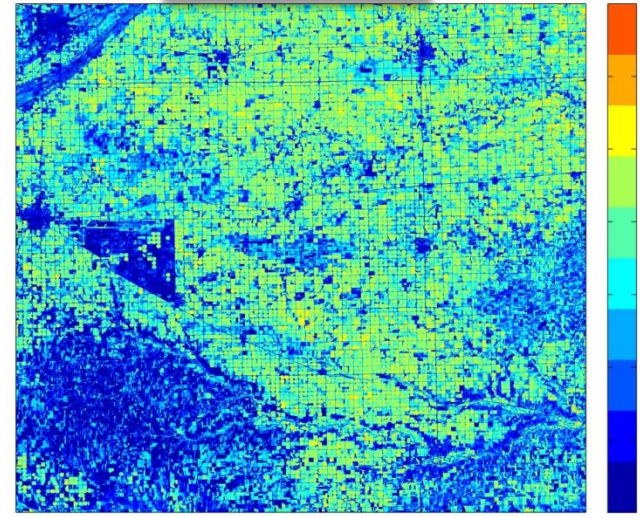


Scalar Outputs: LAI

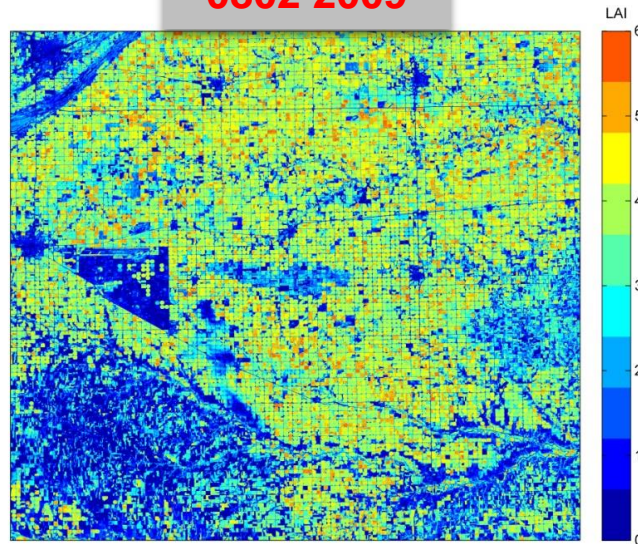
0701 2009



0717 2009

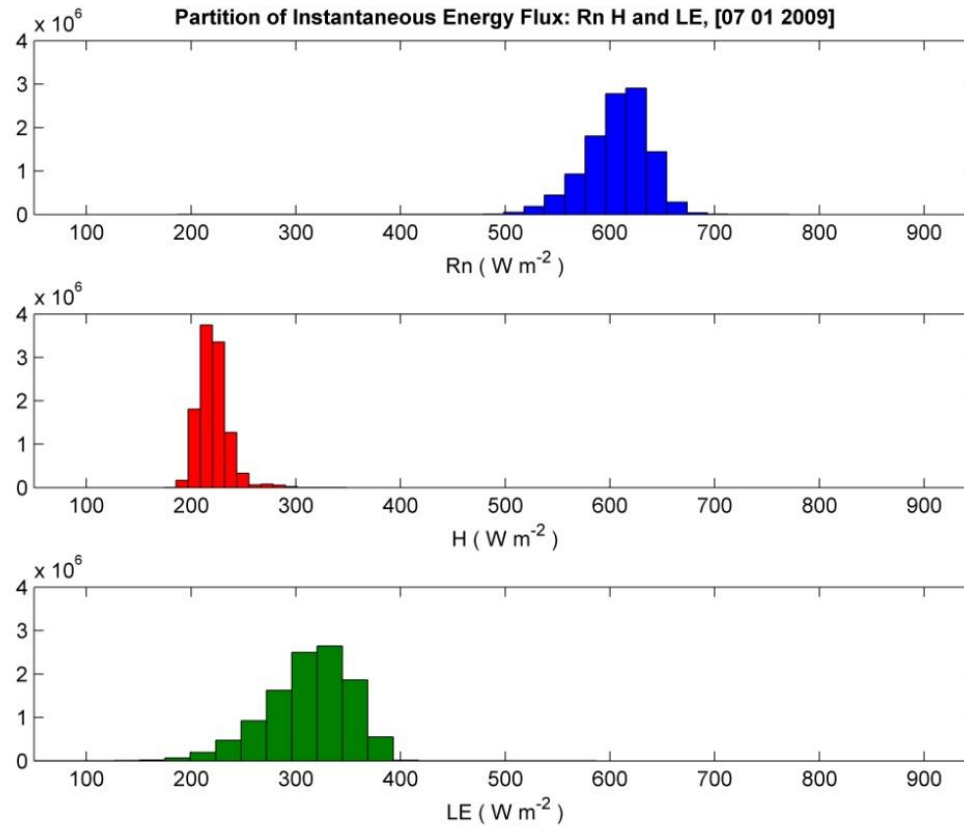


0802 2009



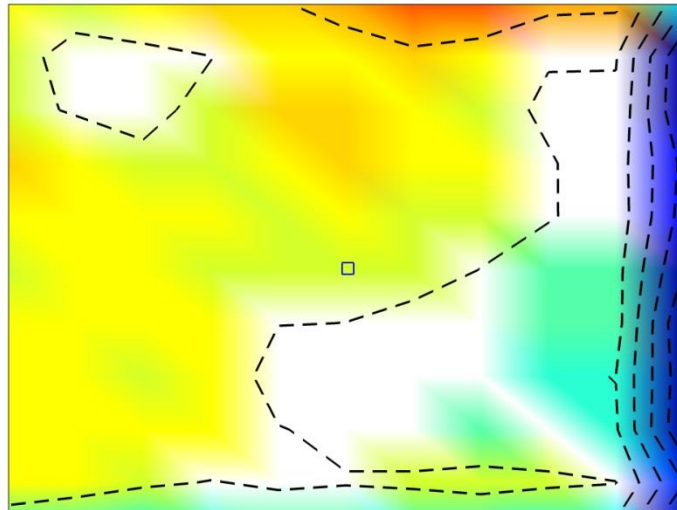
Scalar Flux Outputs

July 1st 2009

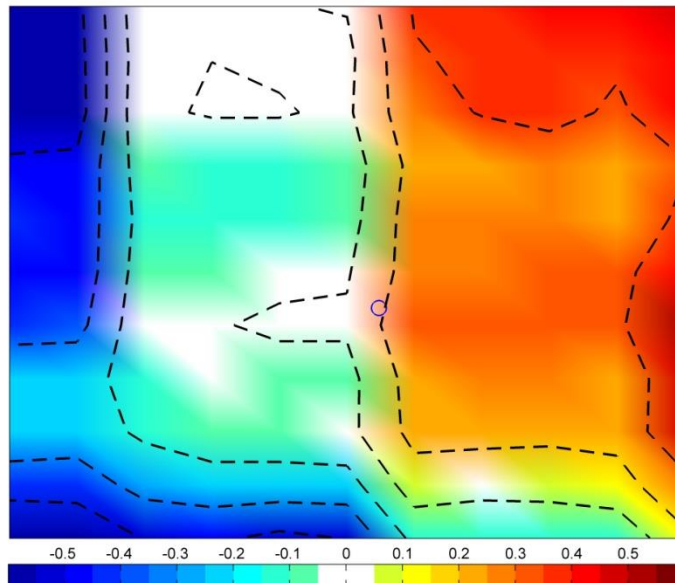


Validation: Daily ET [300 x 300m] for No Till vs. Disk Till

No Till: Field Mean ET = 6.8 mm d⁻¹, [0701 2009]



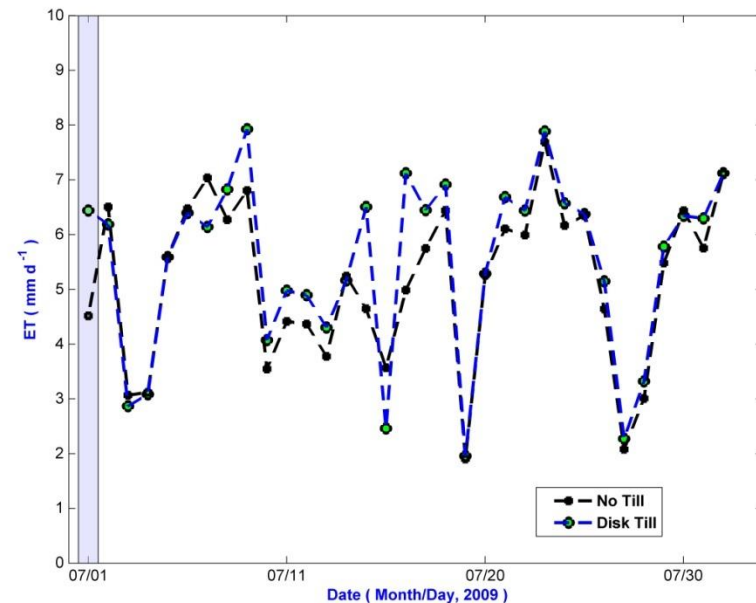
Disk Till: Field Mean ET = 6.7 mm d⁻¹, [0701 2009]



Variations from the Field Mean (mm d⁻¹)

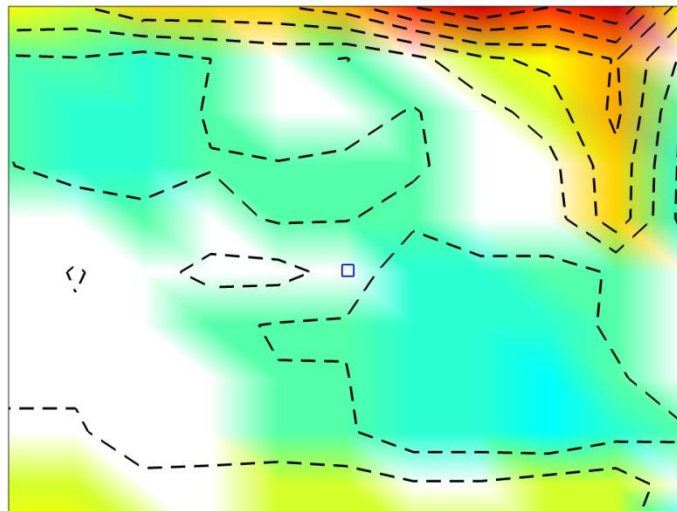
[0701 2009]

Observed ET_{NO Till} and ET_{Disk Till}

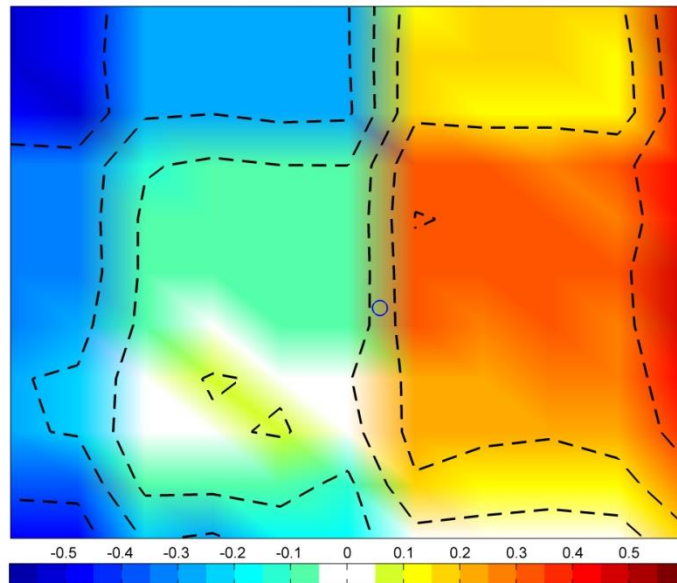


Validation: Daily ET [300 x 300m] for No Till vs. Disk Till

No Till: Field Mean ET = 4.8 mm d⁻¹, [0717 2009]



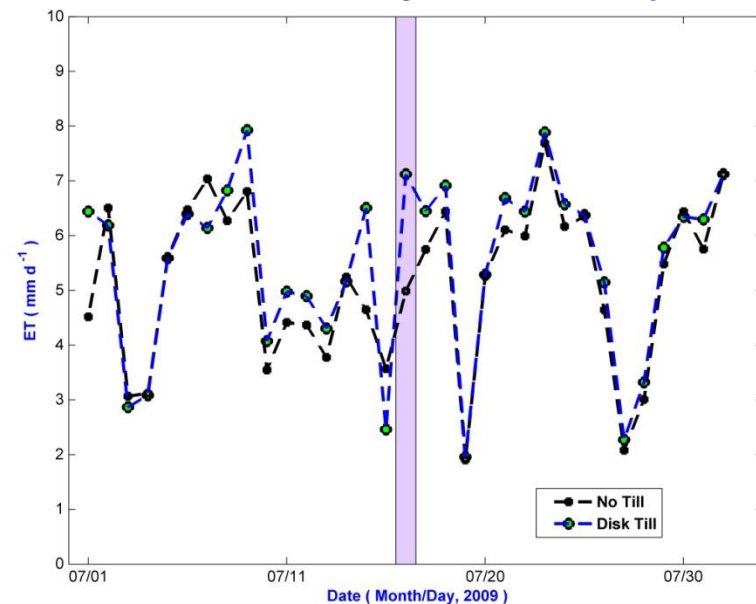
Disk Till: Field Mean ET = 5.7 mm d⁻¹, [0717 2009]



Variations from the Field Mean (mm d⁻¹)

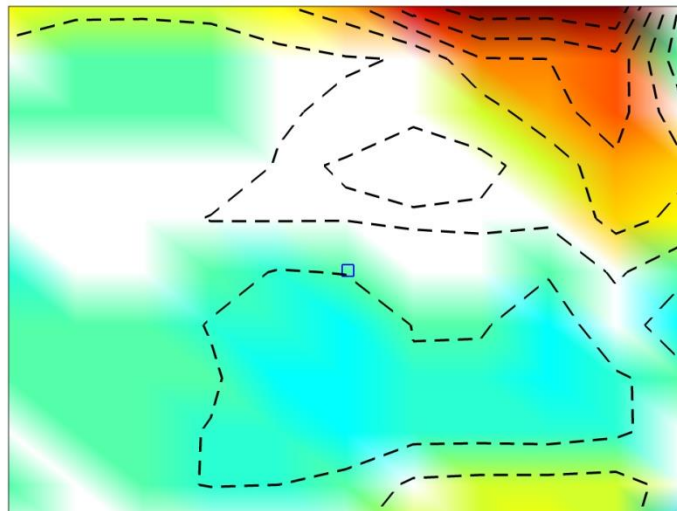
[0717 2009]

Observed ET NO Till and ET Disk Till

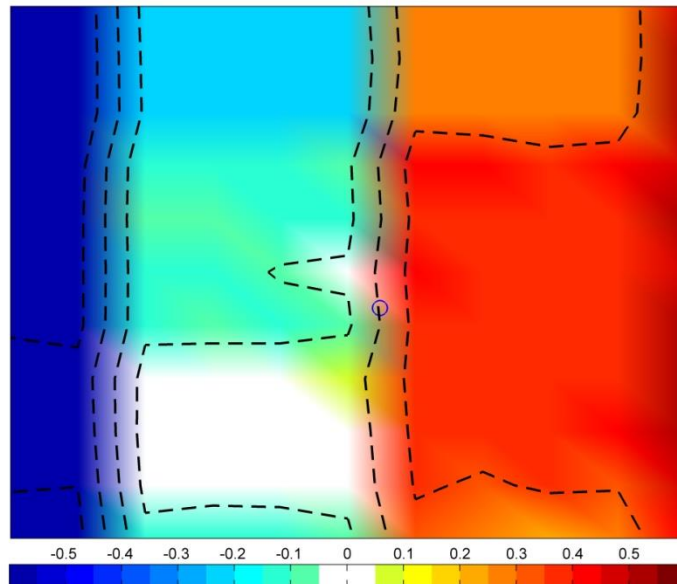


Validation: Daily ET [300 x 300m] for No Till vs. Disk Till

No Till: Field Mean ET = 7 mm d⁻¹, [0802 2009]



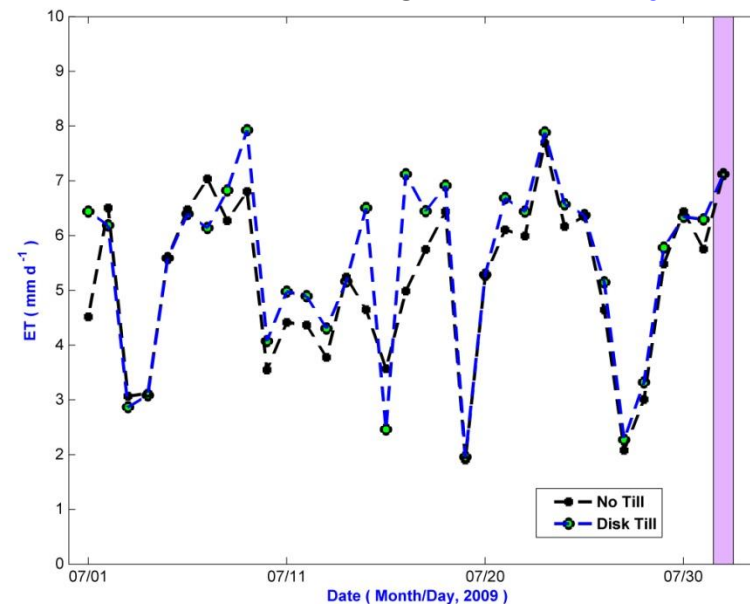
Disk Till: Field Mean ET = 7.7 mm d⁻¹, [0802 2009]



Variations from the Field Mean (mm d⁻¹)

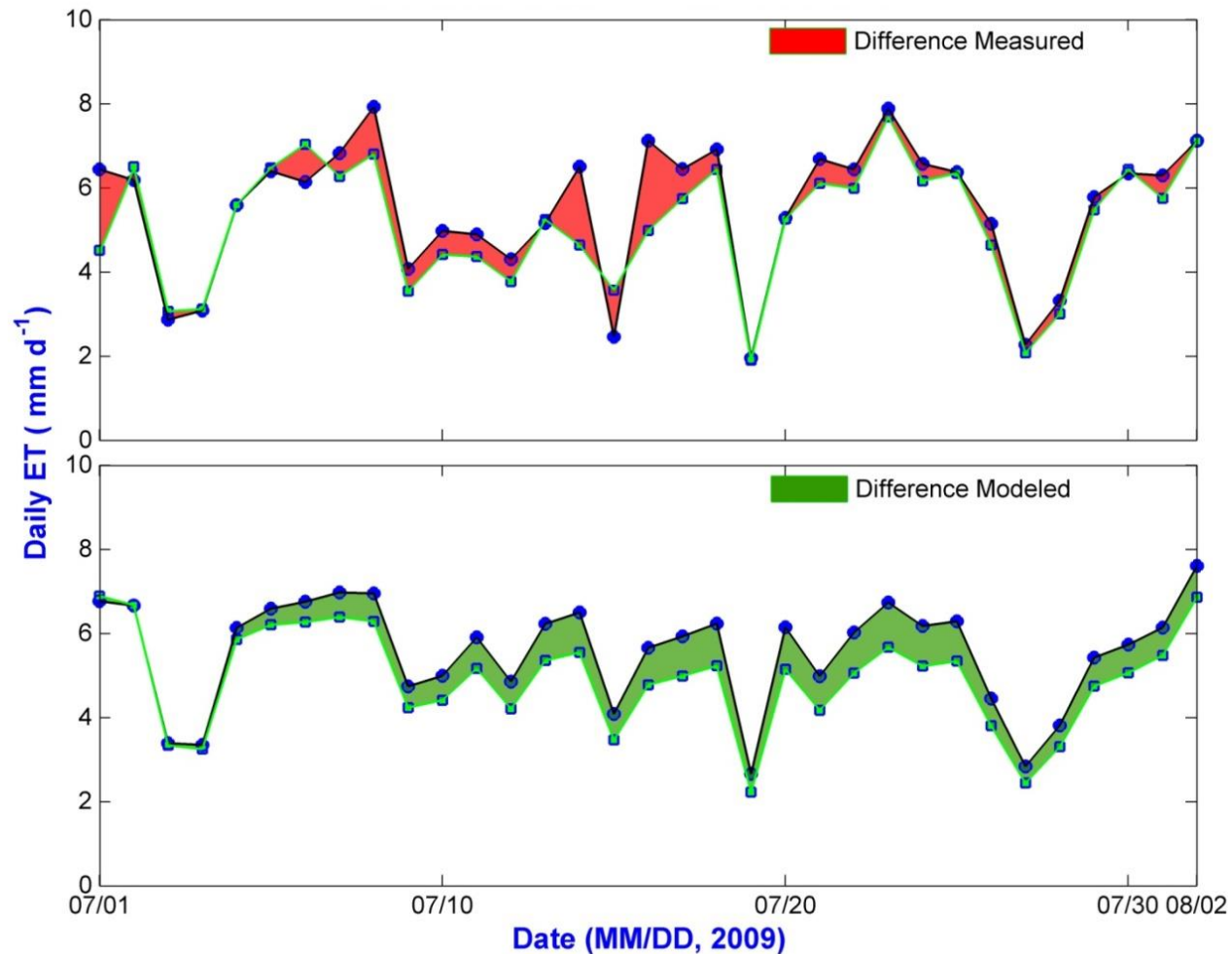
[0802 2009]

Observed ET NO Till and ET Disk Till

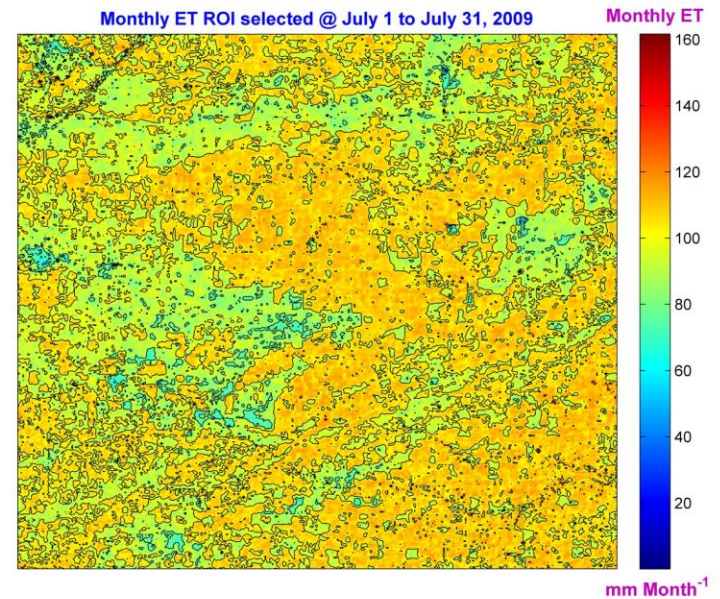
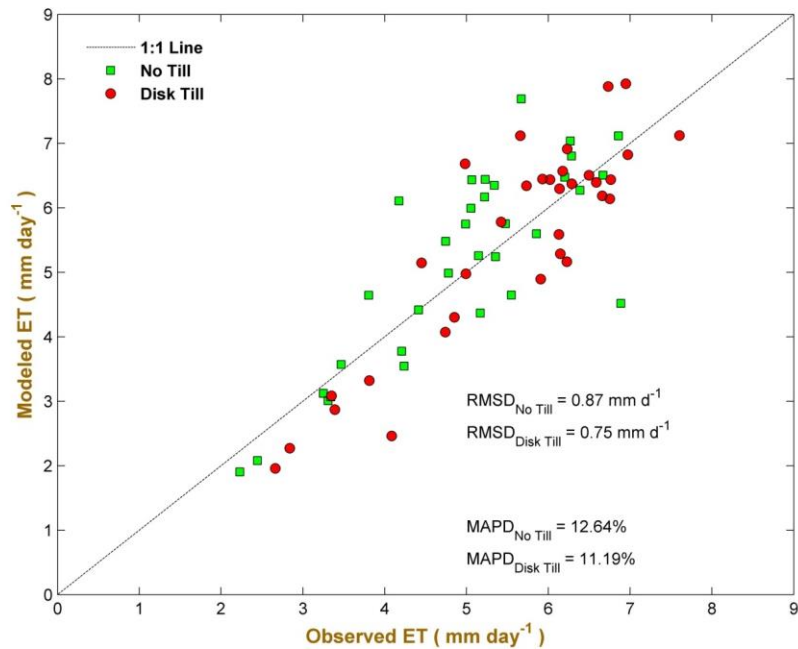


Comparison of Daily ET

Measured Difference (top) and Modeled Difference (Bottom)
between No Till (■) and Disk Till (●) Field



Modeling Performance and Monthly Spatial ET Estimate



Summary: ET Modeling

A modified surface energy balance model was developed. Models were performed well under both large scale [100 x 100 Km] and field scale --- R_{EX} and LU data Introduced.

Automated searching, locating, and estimating the endpoints of the hot and cold pixels made selection objective with less assumptions --- Automatic & Robust.

The models used have been designed to be robust to expected errors (around 12%) for daily ET validated by the point-measurements from Bowen ratio systems.

The field scale ET variations presented here suggest that disk till corn field had significantly and consistently larger ET than the no till corn fields in July 2009.

Mapping Tool: only four inputs

```
1 % OSM modeling and mapping ET
2 %
3 % This program is a research code for calculating ET by using satellites of
4 % Landsat 5 and 7 as well as local whether station information. It is
5 % workable under current condition when your selected ROI is appopporiate
6 % but WITHOUT ANY WARRANTY for your application purposes.
7 %
8 % Time: Jan. 2007 started up and continued in July 2009 at the UNL
9 % Status: Workable
10 % Author: Xiaomao Lin @ UNL
11 % Revision: 07_27_2009: it was working
12 % 08_03_2009: Optimalized pixel selection algorithm (Dry and Wet)
13 % 08_03_2009: Fixed dT algorithm
14 % 08_2009: Added the landuse and DEM
15 % 08_2009: Comparison confirmed with Ian
16 % 09_2009: Final comparison done
17 % 09_2009: Optimized the codes
18 % 01_2010: Comparison re-confirmed with Towers
19 % 02_2010: OK_status with
20 clear all; clc; close all;
21 % *****
22 % Step 1: INPUTS for OSM: 4 input groups
23 % *****
24 % Weather data is the mat format already inclduing HD st ed lat lon ele
25 % HD contains 9 variables (see STNbasicINFO.m) inside
26 % 1.1 Weather station Info
27 STNPATHandName = 'd:\mat\et_pm\matdata\Claycenter2005_9hr';
28 % *****
29 % 1.2 Input sat image file
30 % *****
31 SATimPATHandName= 'd:\sat_data_center\L5029032_03220090701_B';
32 %SATimPATHandName = 'd:\sat_data_center\L5029032_03220090717_B';
33 %SATimPATHandName= 'd:\sat_data_center\L5029032_03220090802_B';
34 % 1.3 Input landuse and land cover info
35 LULCimPATHandName = 'd:\sat_data_center\Landuse_p29r32_2005.tif';
36 DEMimPATHandName = 'd:\sat_data_center\dem_30m_p29r32_float.tif';
37 % 1.4 Input soil property info
38 %DEMimPATHandName = 'd:\sat_data_center\dem_30m_p29r32.tif';
39 SOILfcPATHandName = 'd:\sat_data_center\fc_fraction_p29r32_30m.tif';
40 SOILwpPATHandName = 'd:\sat_data_center\wp_fraction_p29r32_30m.tif';
41 %LULCimPATHandName = 'd:\sat_data_center\jly2009\landuse_2005_pwgs84.tif';
42 %DEMimPATHandName = 'd:\sat_data_center\jly2009\p29r32_051905_dem_30m_wgs84_float.tif';
43 %SOILfcPATHandName = 'd:\sat_data_center\jly2009\fc_fraction_p29r32_30m.tif';
44 %SOILwpPATHandName = 'd:\sat_data_center\jly2009\wp_fraction_p29r32_30m.tif';
45
```

Input I

Input II

Input III

Input IV

References

1. P. J. Sellers et al, 1995, Science
2. John Norman et al, 1995, AFM
3. James Wallance, 1995, AFM
4. Shuttleworth and Wallace, 1985

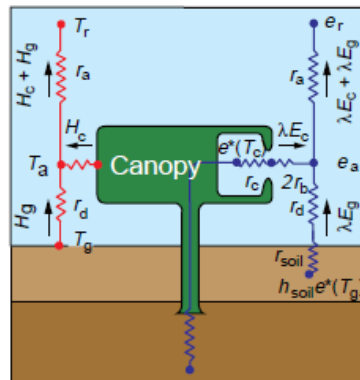
Reference height z_r

Atmosphere

Canopy air space

Surface soil layer

Root zone layer

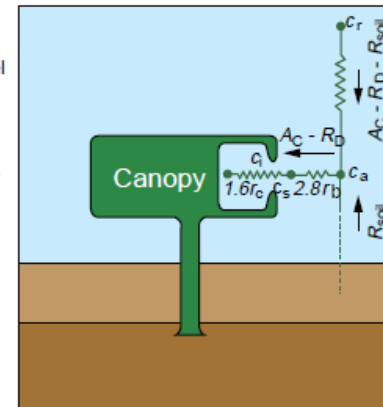


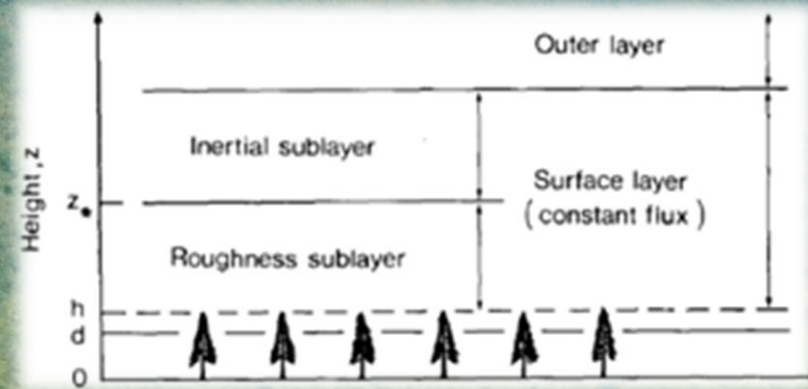
C

Atmospheric CO₂, etc
Tracer - transport model

Canopy photosynthesis
- conductance model

Soil respiration model

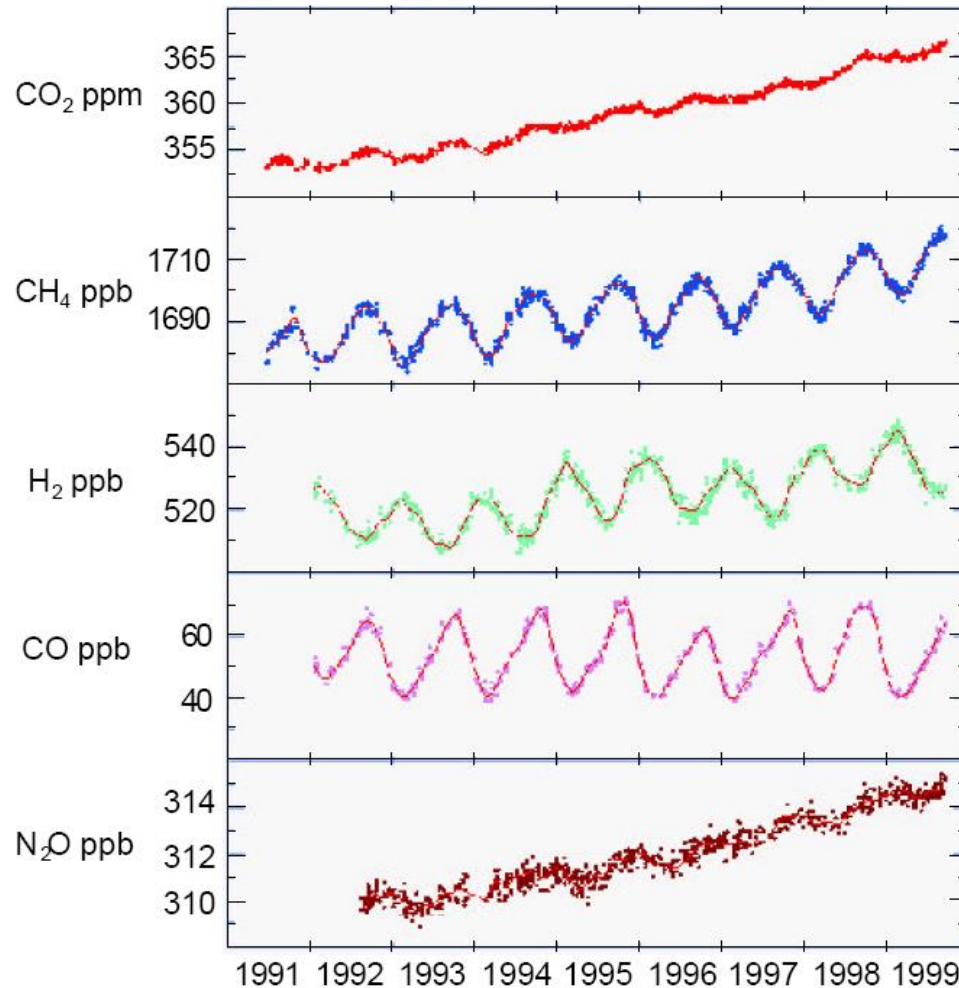




II: Uncertainties in Eddy Covariance Flux Estimate

1. Spatial Context of Flux vs. Sensor Heights
2. High Frequency Loss vs. Sensor Heights
3. Low frequency Loss vs. Sensor Heights.

Why EC Fluxes of Trace Gas are Important ?



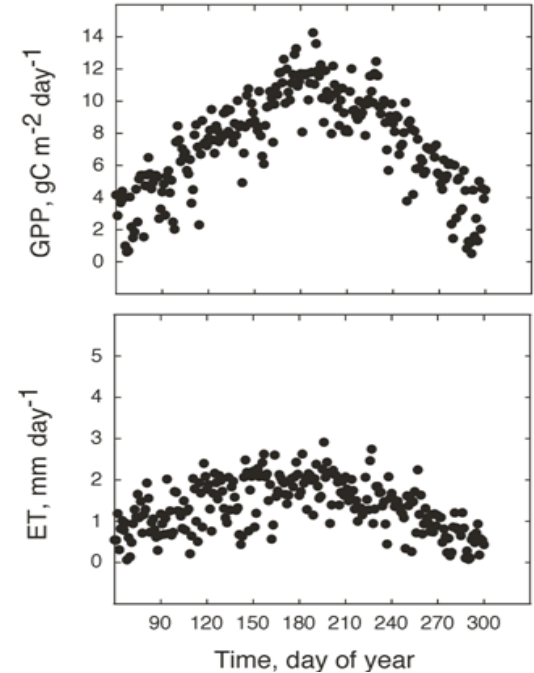
Eddy Covariance: From Measurements to Fluxes



$$H = \rho c_p \overline{w'T'}$$

$$LE = \lambda \overline{w'q'}$$

$$F_c = \overline{w'c'}$$



- u v w , and T_{sonic}
- H_2O and CO_2 (IRGA)
- Pressure
- Mean T_a and RH_a
- Diagnostic Status

Data Processing

- F_c (carbon flux)
- LE (water flux)
- H_s (sensible heat flux)

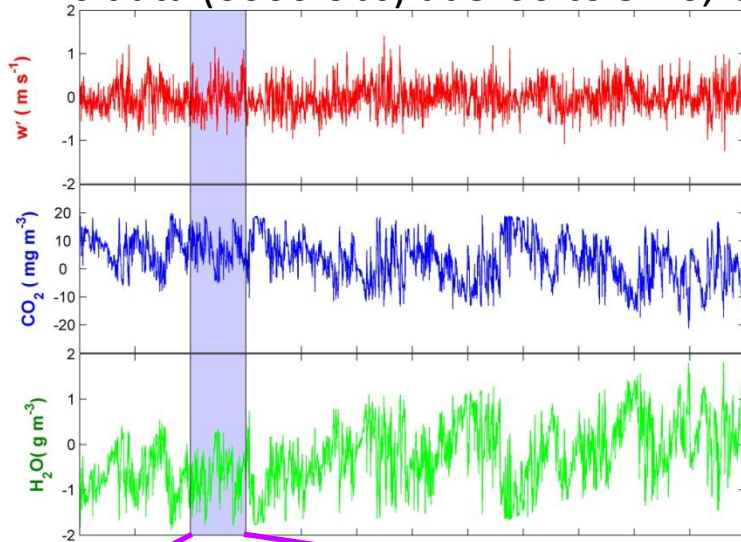
10Hz

Eddy Size (Limited Bandwidth)

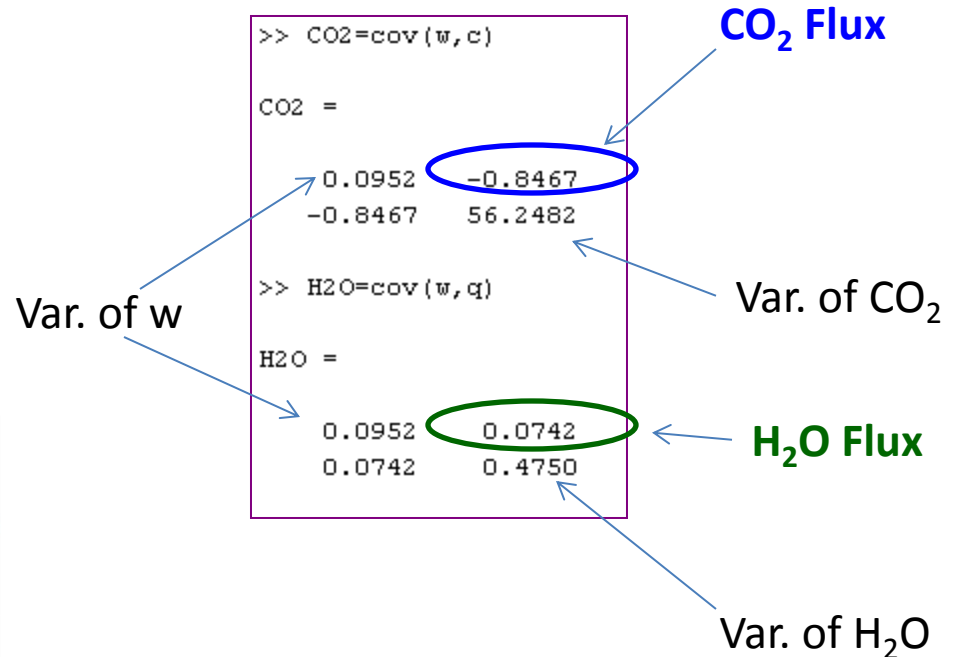
0.000556 Hz (30 mins)

What is the Eddy Covariance in a simple way?

10 mins data (6000 obs) at 9:00 to 9:10, Grassland



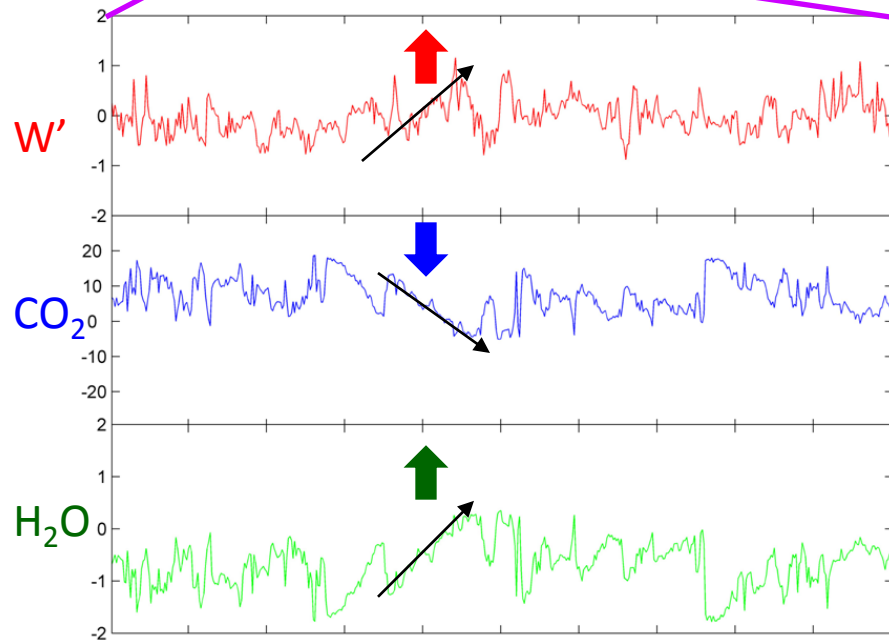
$$\text{Cov}(w, c) = E[(w - \bar{w})(c - \bar{c})] = E[w' c']$$



So, we have

$$\begin{aligned} \text{CO}_2 \text{ Flux} &= -0.8467 \text{ m s}^{-1} \text{ mg m}^{-3} \\ &= -0.8467 \text{ mg m}^{-2} \text{ s}^{-1} \end{aligned}$$

$$\begin{aligned} \text{H}_2\text{O Flux} &= 0.0742 \text{ m s}^{-1} \text{ g m}^{-3} \\ &= 0.0742 \text{ g m}^{-2} \text{ s}^{-1} \\ &= 176.4 \text{ W m}^{-2} \end{aligned}$$



The Juice of the Eddy Covariance

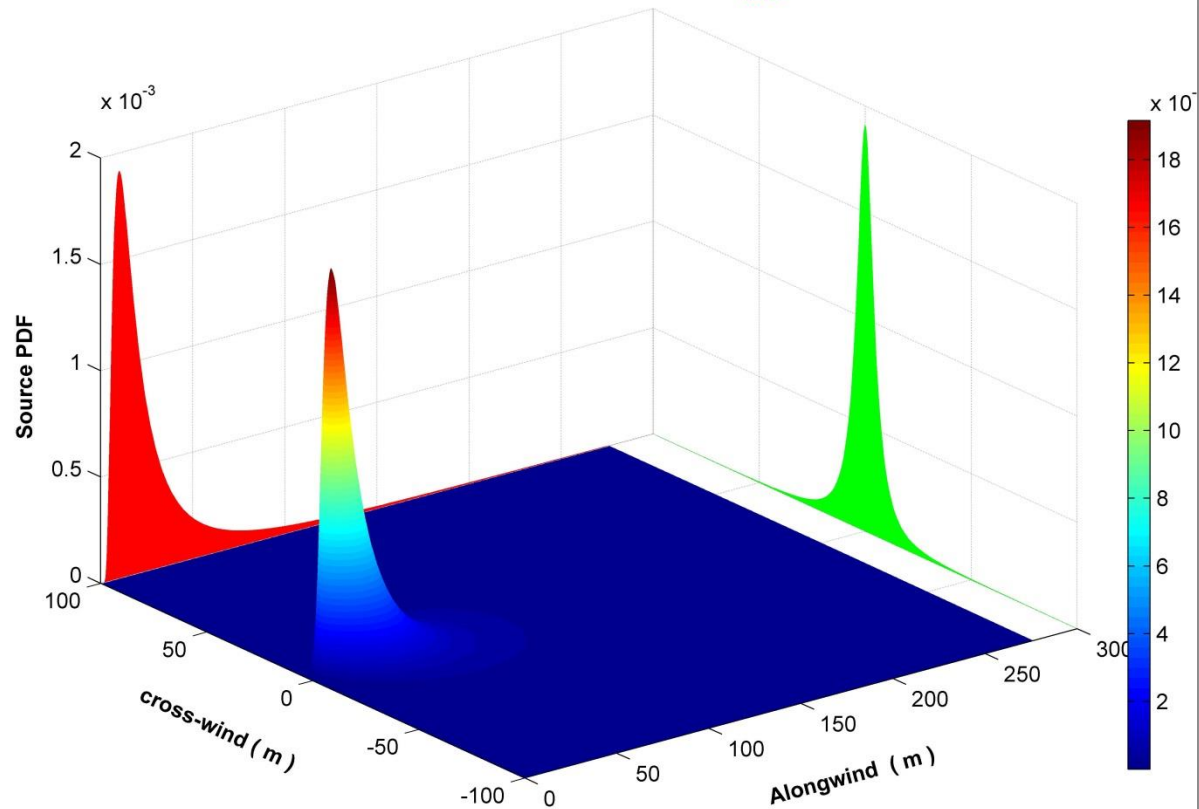
Start from mass conservation equation (CO₂, or H₂O) or Navier-Stokes equation, then, apply Reynolds decomposition and averaging, along with the turbulent continuity equation in the x-z planes, it will lead to:

$$\begin{aligned}
 \underbrace{F_v}_{\text{Total Flux}} &= L_v \underbrace{\overline{w' \rho_v'} \Big|_{h_m}}_{F_v^{EC}: \text{Eddy Cov.}} \\
 &= \underbrace{\int_0^{h_m} L_v \frac{\partial \overline{\rho_v}}{\partial t} dz}_{F_v^{ST}: \text{Storage}} + \underbrace{\int_0^{h_m} L_v \left(\bar{u} \frac{\partial \overline{\rho_v}}{\partial x} \right) dz}_{F_v^{HA}: \text{Hori. Adv}} + \underbrace{\int_0^{h_m} L_v \left(\bar{w} \frac{\partial \overline{\rho_v}}{\partial z} \right) dz}_{F_v^{VA}: \text{Vert. Adv}}
 \end{aligned}$$

An Example of Scalar Footprint Analysis

Footprint Context

Fig. 6. One shot for landfill at 0:00 of Aug. 1, 2010. $F_{CH_4} = 43.8$, $DIR = 33^\circ$



Spectral Attenuation of Scalar Flux

$$\langle \mathbf{w}' \mathbf{c}' \rangle = \int_0^\infty \mathbf{Co}_{wc}(\mathbf{f}) d\mathbf{f}$$

$$\langle \mathbf{w}' \mathbf{c}' \rangle_m = \int_0^\infty \mathbf{H}_c(\mathbf{f}) \mathbf{Co}_{wc}(\mathbf{f}) d\mathbf{f}$$

Cospectrum model:

$$\frac{f \mathbf{Co}_{wc}(f)}{\langle \mathbf{w}' \mathbf{c}' \rangle} = \frac{2}{\pi} \frac{f / f_m}{(1 + (f / f_m)^\mu)^\alpha}$$

Spectral correction:

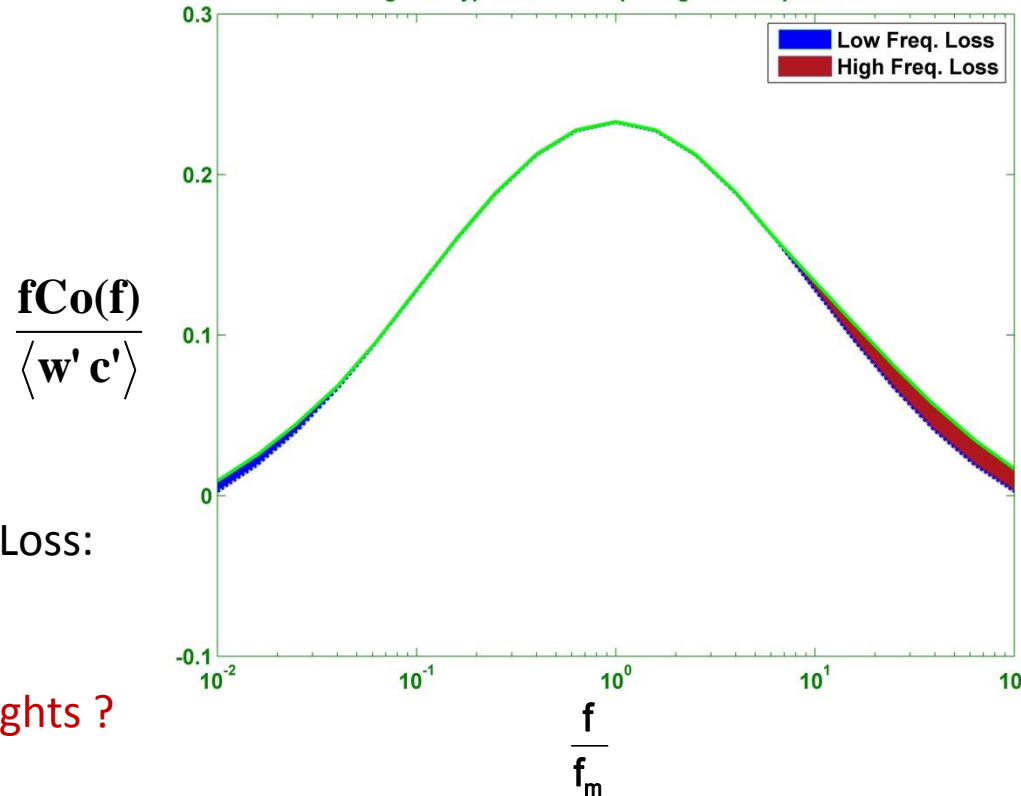
$$\frac{\langle \mathbf{w}' \mathbf{c}' \rangle_m}{\langle \mathbf{w}' \mathbf{c}' \rangle} = \underbrace{\frac{1}{1 + (2\pi f_m \tau_c)^\alpha}}_{\text{I}} \underbrace{\frac{(2\pi f_m \tau_b)^\alpha}{1 + (2\pi f_m \tau_b)^\alpha}}_{\text{II}}$$

I: a single-pole, low-pass RC filter for all path average, displacement, and other high-freq.

II: block average considered as a high-pass filter if assume the $\tau_b = T_B / 2.8$ (Kaimal, 1989).

Cospectra Models for EC Flux Corrections

Fig. 1a. Hypothetical Freq.-Weighted Cospectrum



Low Freq. Flux Loss:

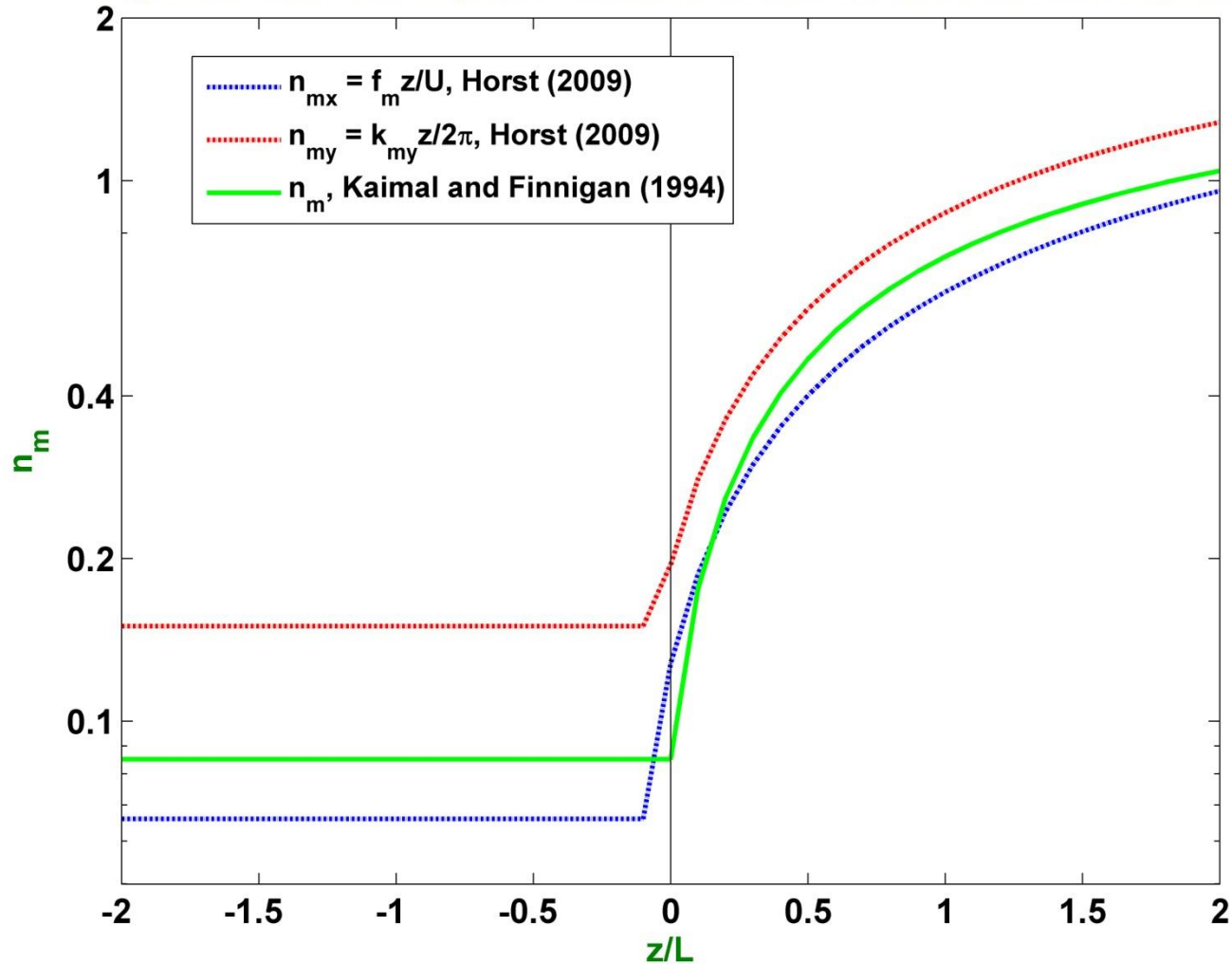
Block Average
30 mins vs. Heights ?

High Freq. Flux Loss:

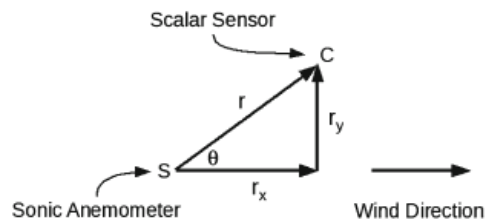
- Path average?
- Time Response?
- Tube attenuation (if CP)?
- Sensor Displacement?

A Key in Spectral Models: Maxima (f_m or n_m) of Cospectra

Fig.H. Dimensionless freq at the maxima of streamwise and crosswind cospectra



Sensor Displacement: High Freq. Flux Loss Vs. Heights

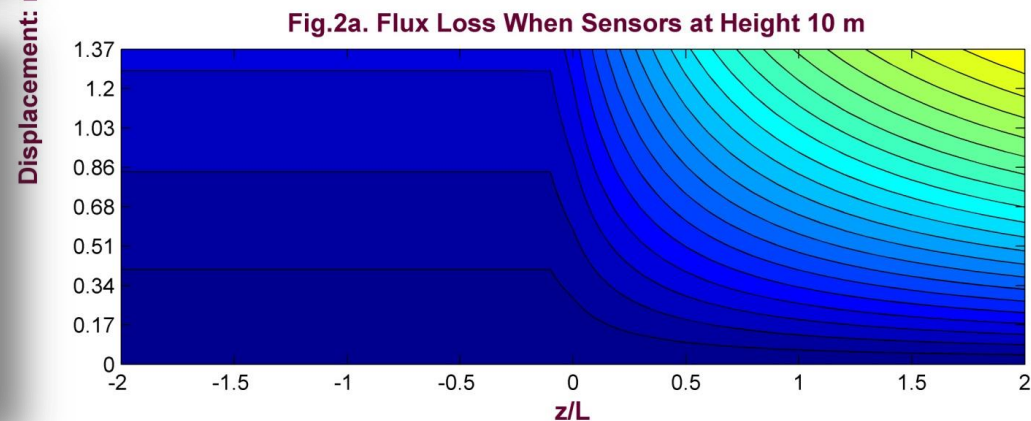
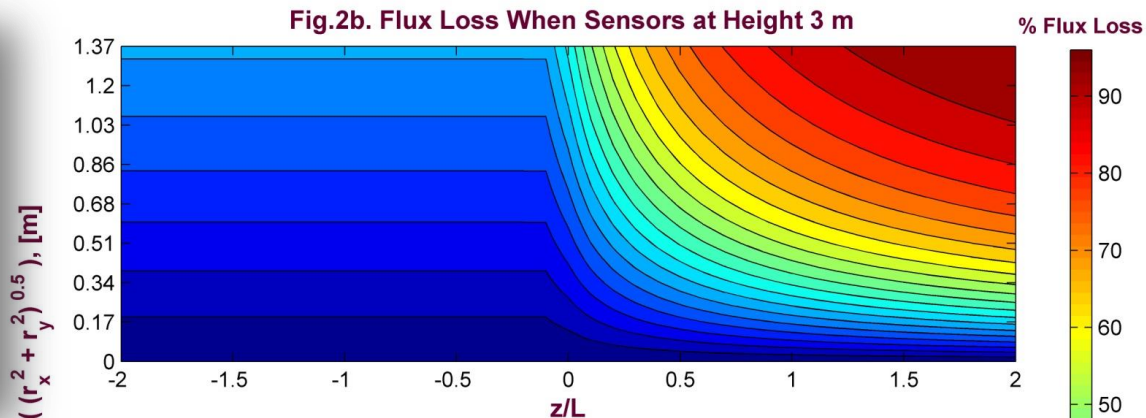


$$\frac{F(r_x, r_y)}{F_0} = \exp[-(\ln^2 Ax + \ln^2 Ay)^{1/2}]$$

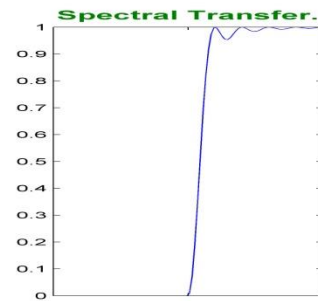
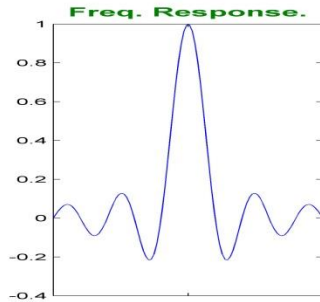
$$Ax = \exp\left(-\frac{2\pi}{z} n_{mx}\right)$$

$$Ay = \exp\left(-\frac{2\pi}{z} n_{my}\right)$$

- Horst and Lenschow, 2009. BLM



Block Average: Low Freq. Flux Loss vs. Heights



Approximate Model

$$\frac{F}{F_0} = \frac{(2\pi n_m \tau_b \frac{u}{z_d})^\alpha}{1 + (2\pi n_m \tau_b \frac{u}{z_d})^\alpha}$$

$$\tau_b = \frac{T_B}{2.8}$$

- Modified from Massman 2000 . AFM.



Fig.1a. Flux Loss When Sensors at Height 3 m

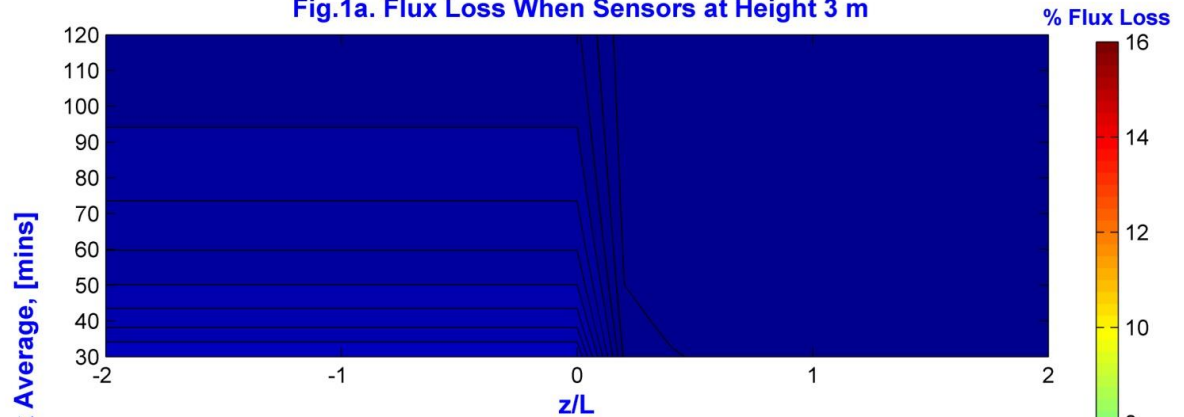
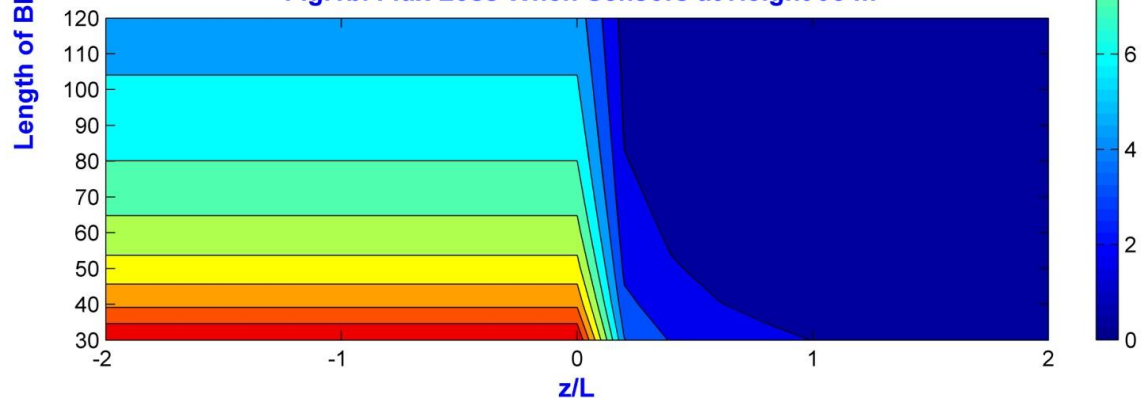
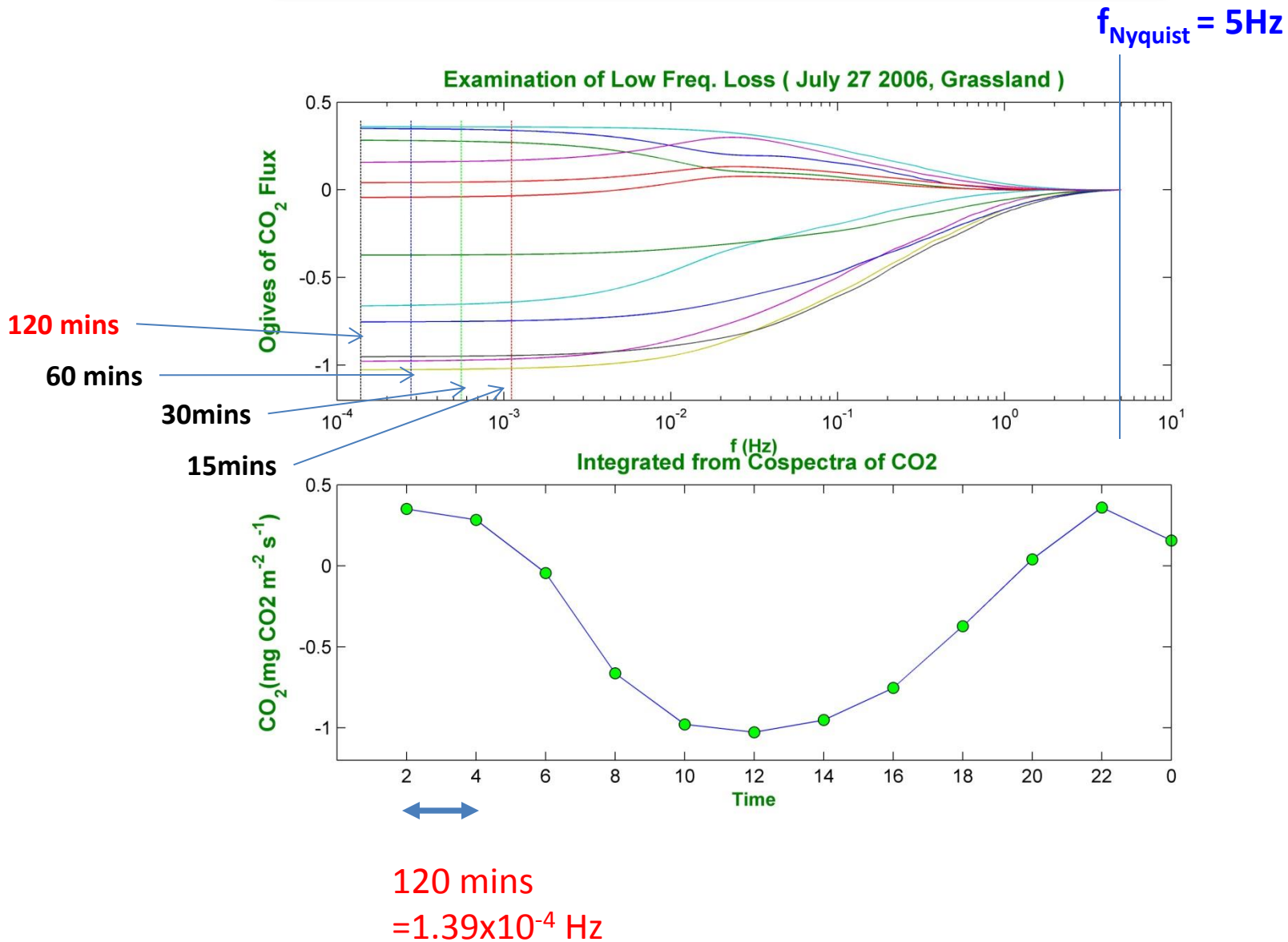


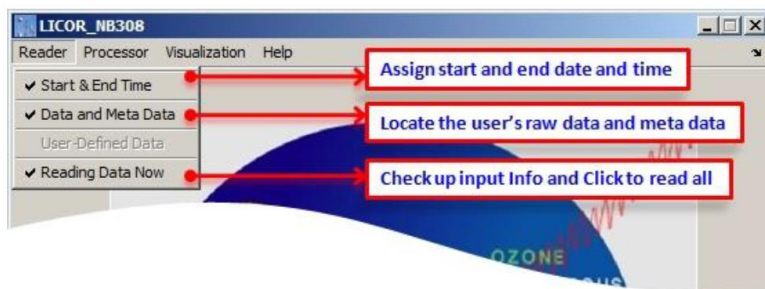
Fig.1b. Flux Loss When Sensors at Height 98 m



Visualization of Low Freq. Flux Loss

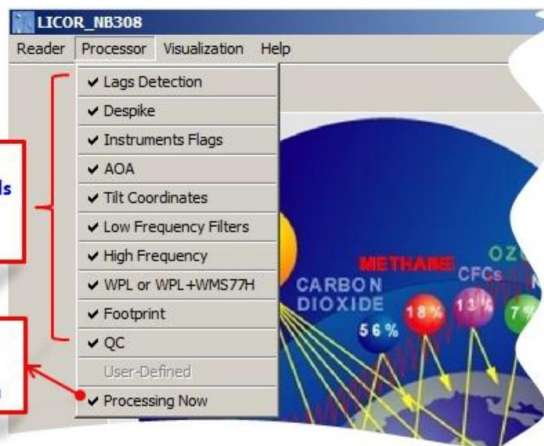


EC Software for Ecosystem Flux Computation, Analysis, and Visualization



Configure all processing models OR don't touch Just use default

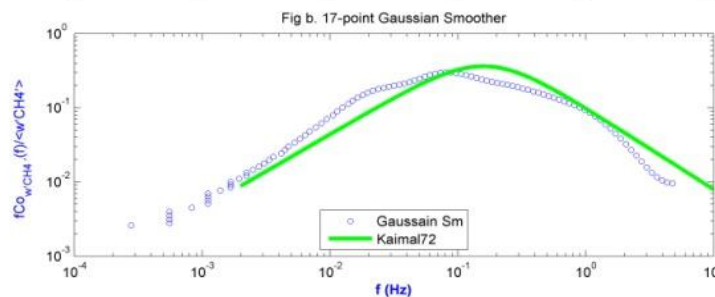
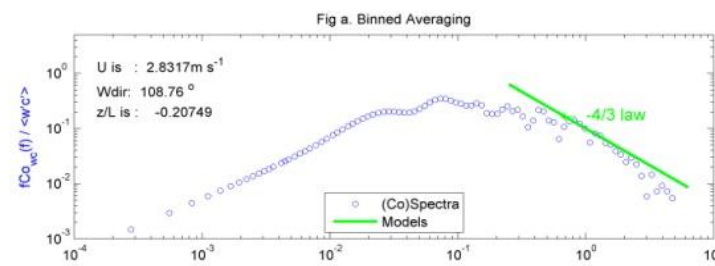
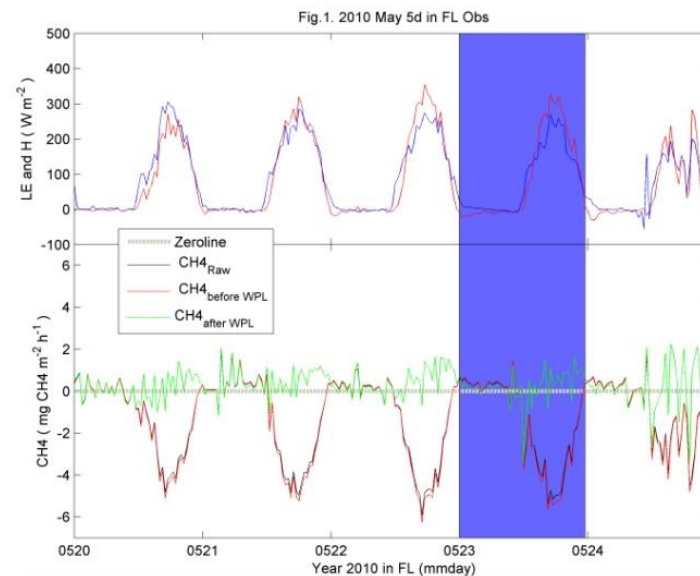
Check up setups Click to process Click to save data



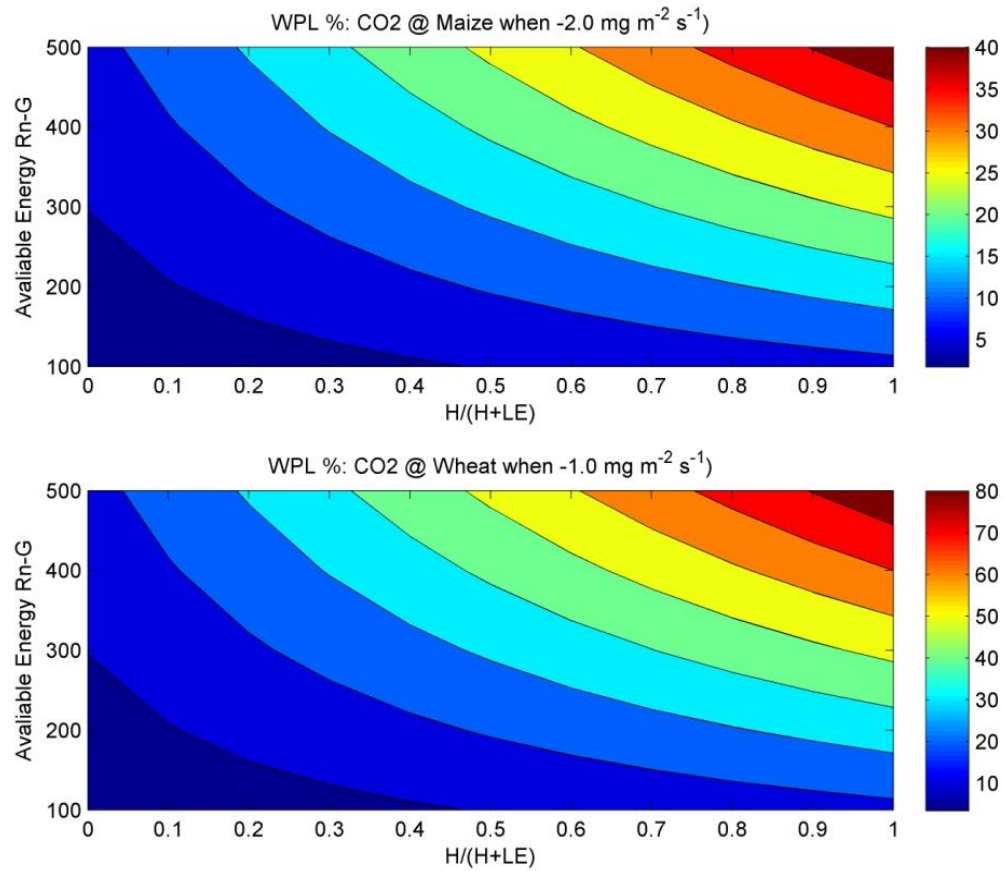
Show all scalar fluxes for all days

Show all footprints, wind spd, dir, and freq.

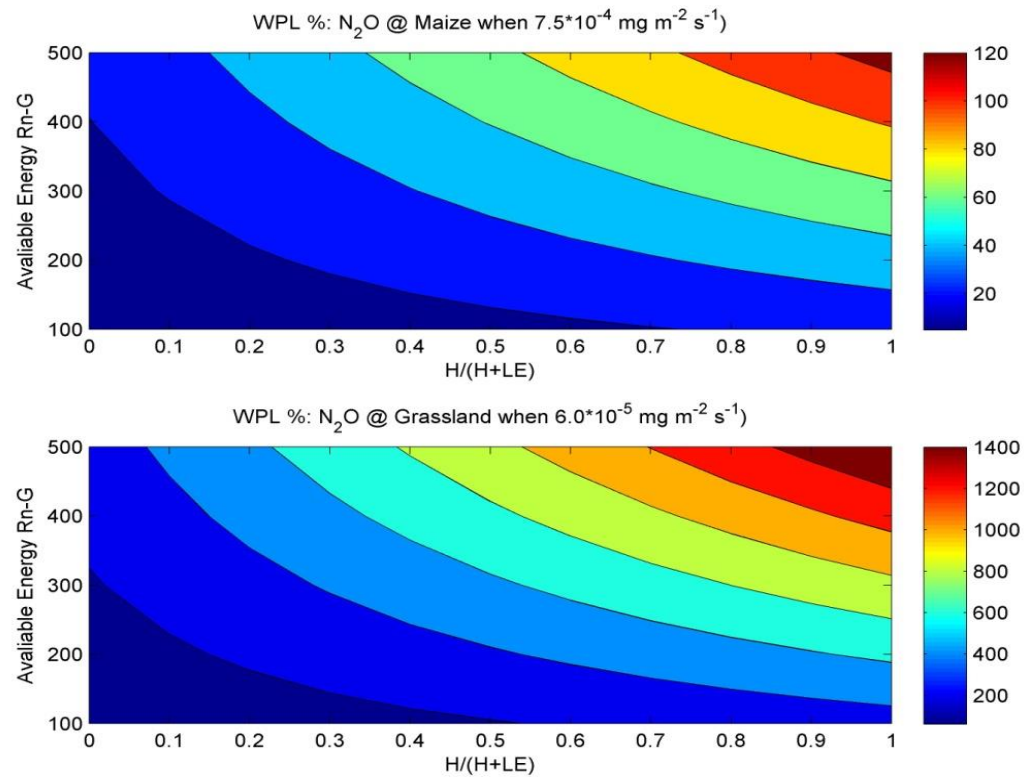
Show co spectra for all scalars



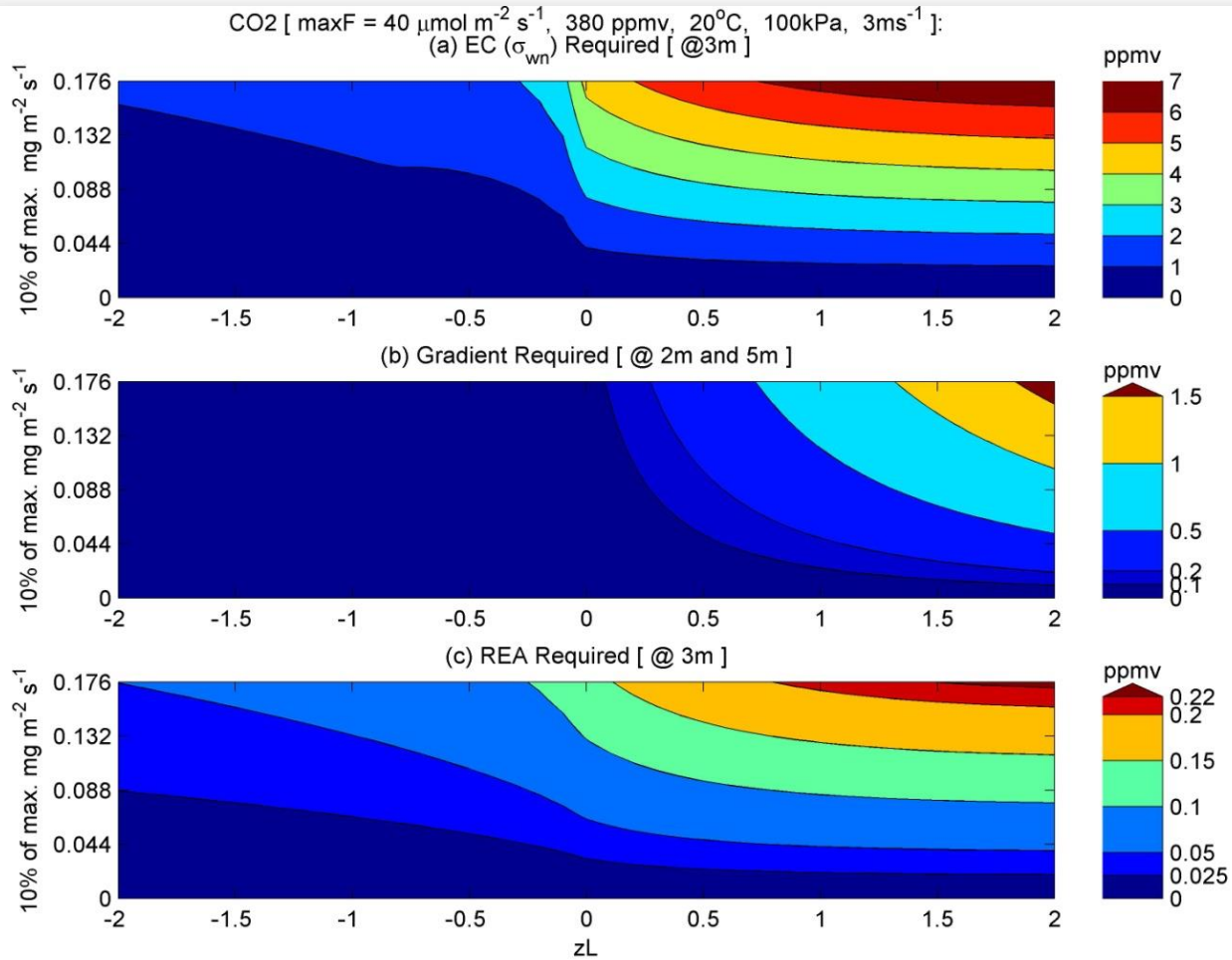
WPL for CO₂ Flux



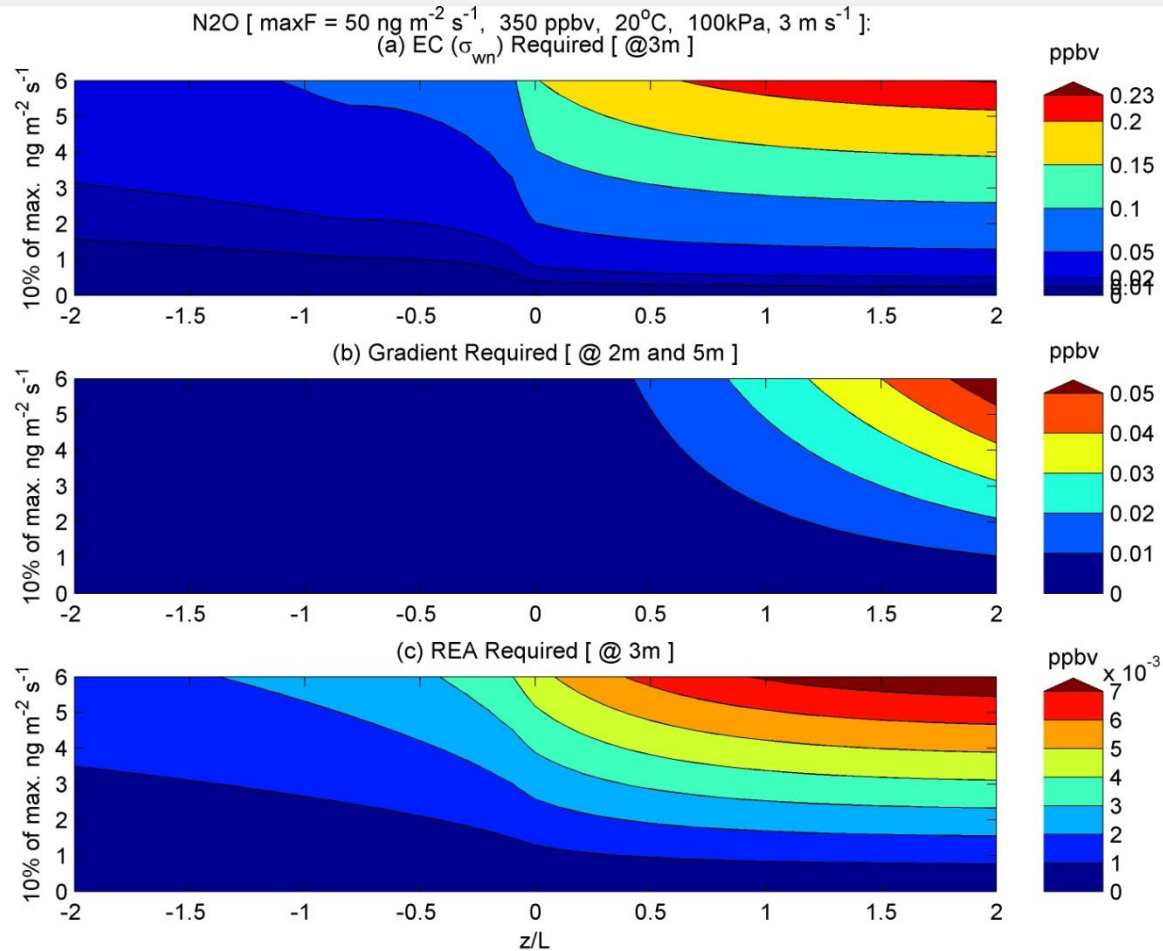
WPL for N₂O Flux



Analyzer's Requirement for CO₂ Flux



Analyzer's Requirement for N₂O Flux



Recent Experiments from 2011 to 2013





CLIMATE SUMMIT

WHAT IF IT'S
A BIG HOAX AND
WE CREATE A BETTER
WORLD FOR NOTHING?

- ENERGY INDEPENDENCE
- PRESERVE RAINFORESTS
- SUSTAINABILITY
- GREEN JOBS
- LIVABLE CITIES
- RENEWABLES
- CLEAN WATER, AIR
- HEALTHY CHILDREN
- ETC. ETC.



YOL
Pitt

12/19 USA TODAY

The End



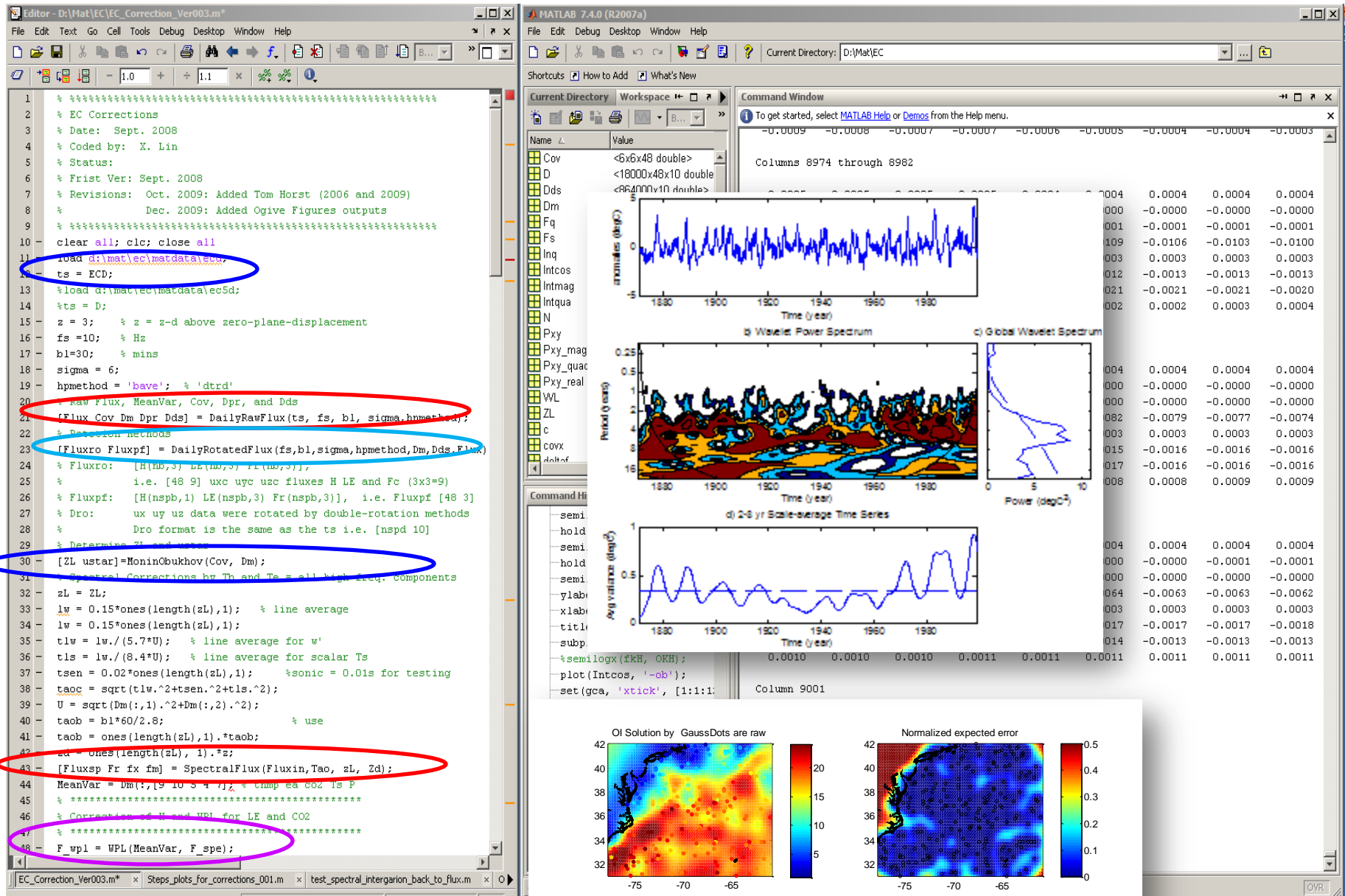


Enabling Technologies

Enabling Technologies



Models Implemented and Improved: EC Corrections and Visualizations



How does Satellite Information do for ET ?

Satellite-Based Land Surface Energy Balance:

--- Thermal images provide T_R Information.

--- Visible and infrared images are used for calculating:

- ❖ Spectral radiances,
- ❖ Spectral reflectance and transmittance,
- ❖ NDVI, LAI, albedo, biomass, and
- ❖ Other biophysical variables.

Sensible Heat Flux:

$$H = \rho C_p \frac{T_{AC} - T_A}{R_A}$$

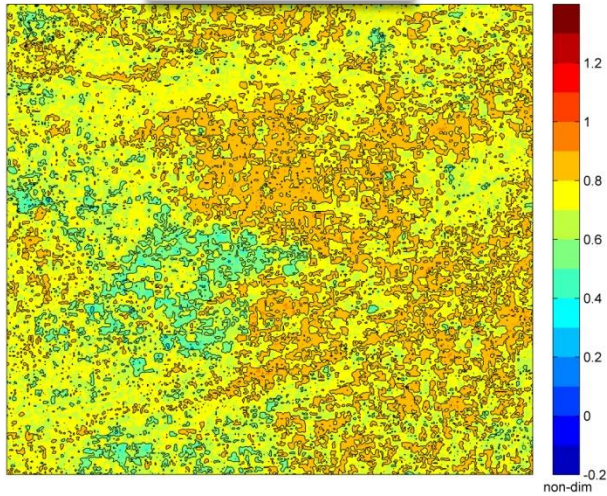
Aerodynamic and Radiometric Temperatures:

$$T_{AC} \propto T_R$$

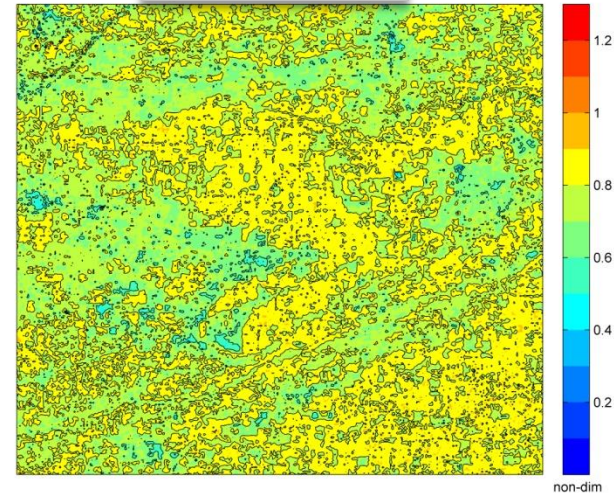
Fraction of Reference ET (ETrF)

$$\text{ETrF} = \frac{\text{ET}_{\text{INST}}}{\text{ETr}}$$

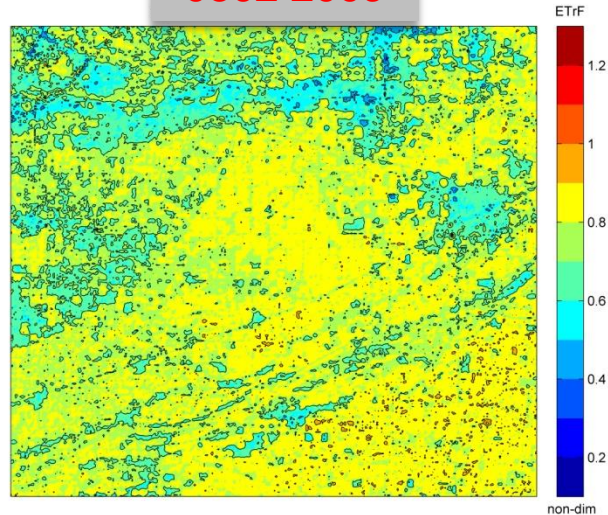
0701 2009



0717 2009

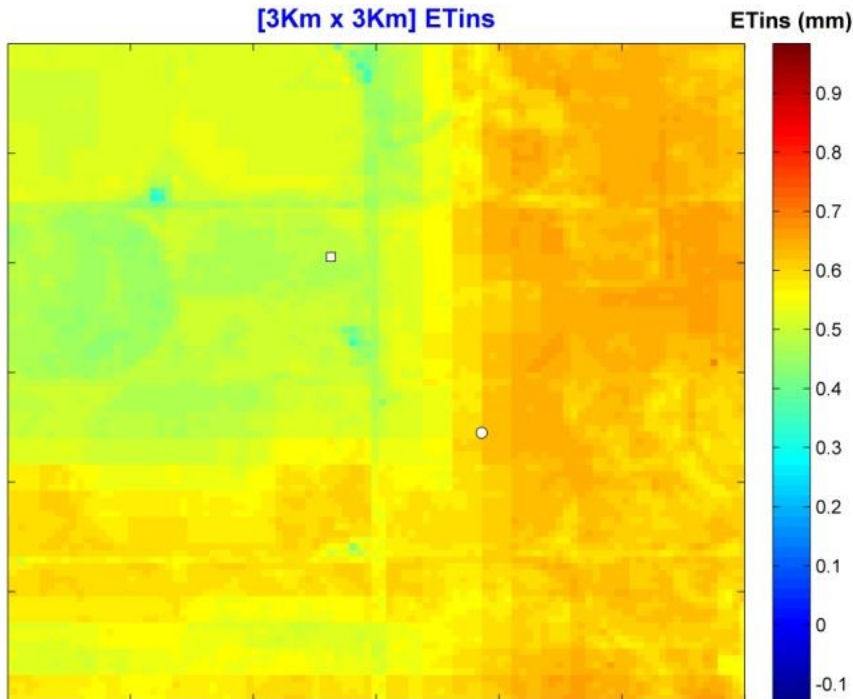


0802 2009

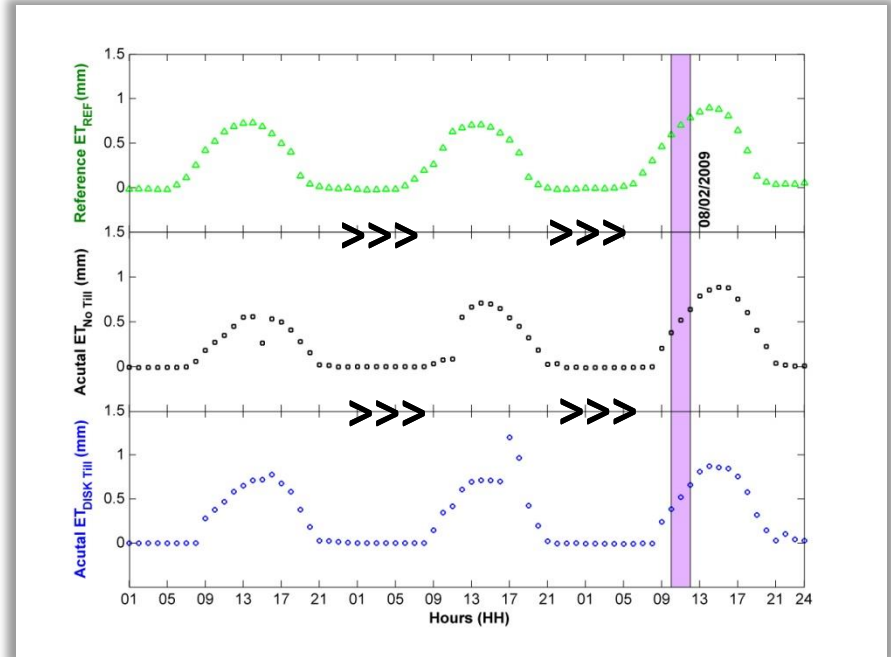


Hourly ET

[08 02 2009]



Modeled ET at Corn Fields



Observed ET_r , $ET_{NO\ Till}$, $ET_{DISK\ Till}$

Key Parameterization

For major crop lands:

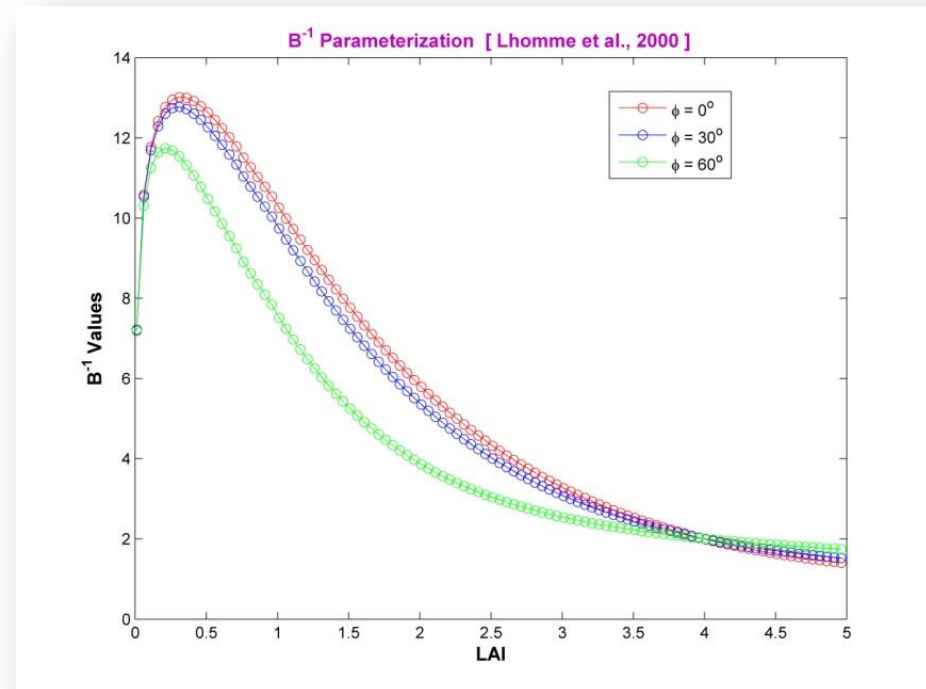
$$Z_{OM} = \frac{h_c - d}{\exp\left(\frac{ku_{h_c}}{u_*} - \psi_H\right)}$$

$$Z_{OH} = \frac{Z_{OM}}{\exp(kB^{-1})}$$

For non crop lands:

$$Z_{OM} = \exp[a_1 \text{NDVI} + b_1]$$

$$R_{EX} = \left[\sum_{i=1}^6 a_i \text{LAI}^i \right] u_*^{-1}$$

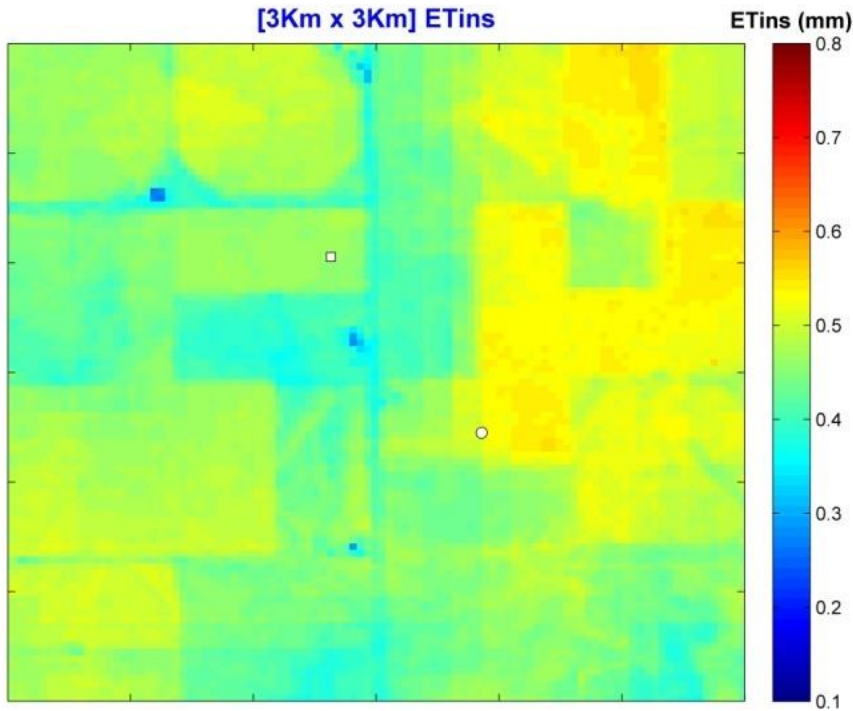


Lhomme et al. 2000

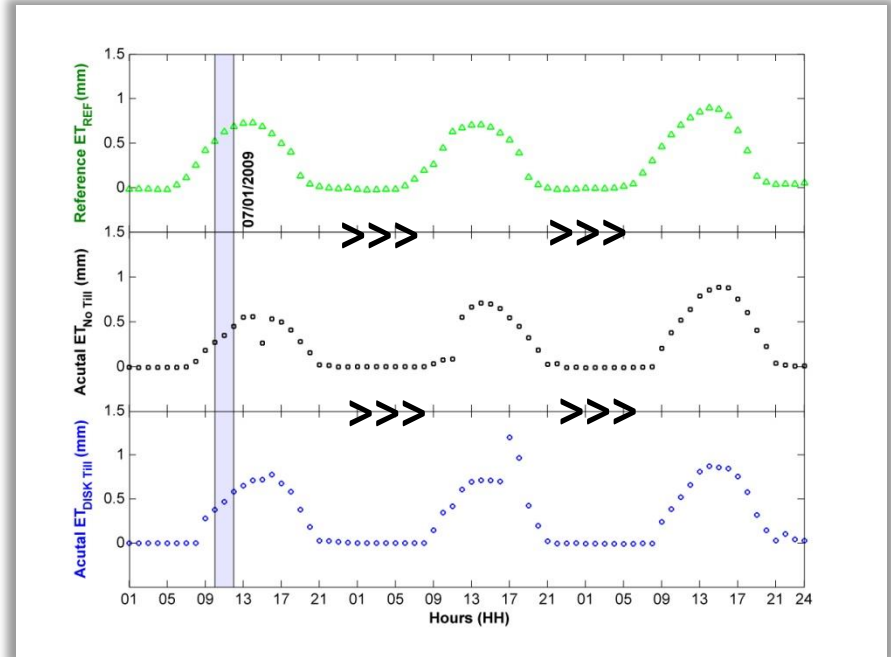
$\phi = 0$ for Landsat TM sensors

Hourly ET

[07 01 2009]



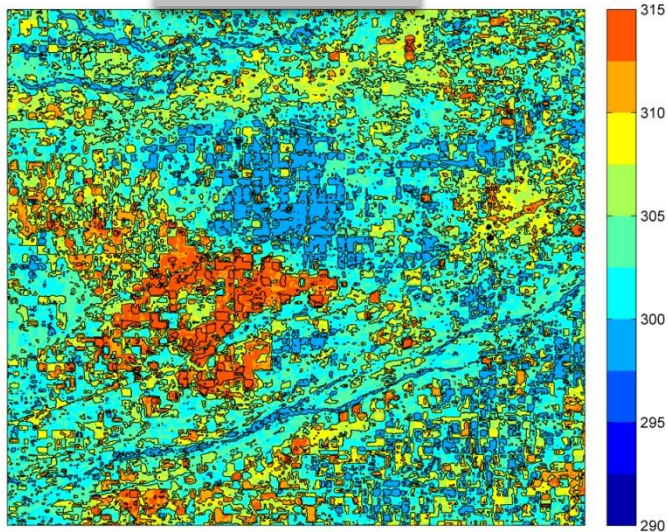
Modeled ET at Corn Fields



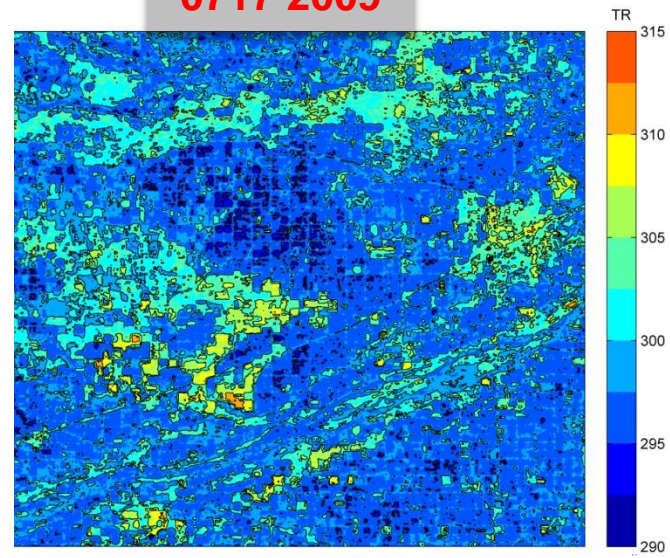
Observed ET_r , $ET_{NO\ Till}$, $ET_{DISK\ Till}$

Scalar Outputs: T_R

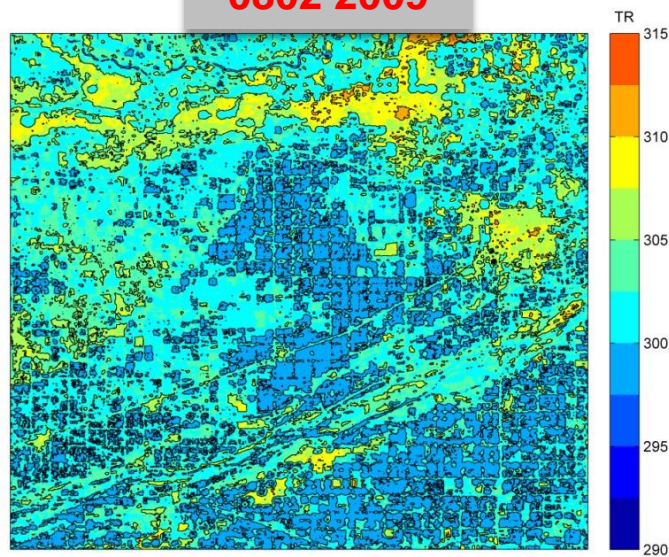
0701 2009



0717 2009

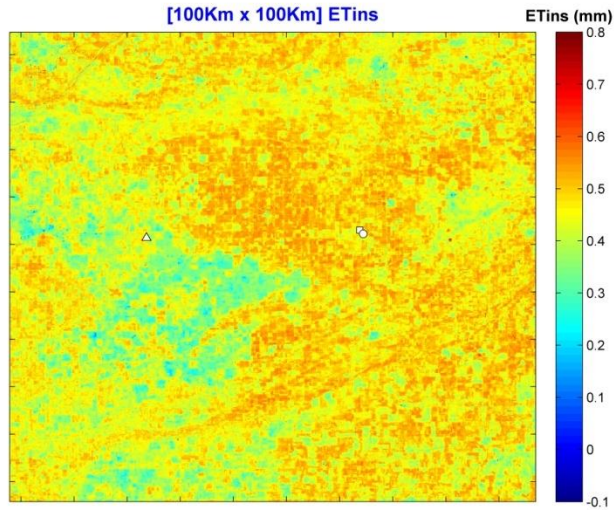


0802 2009

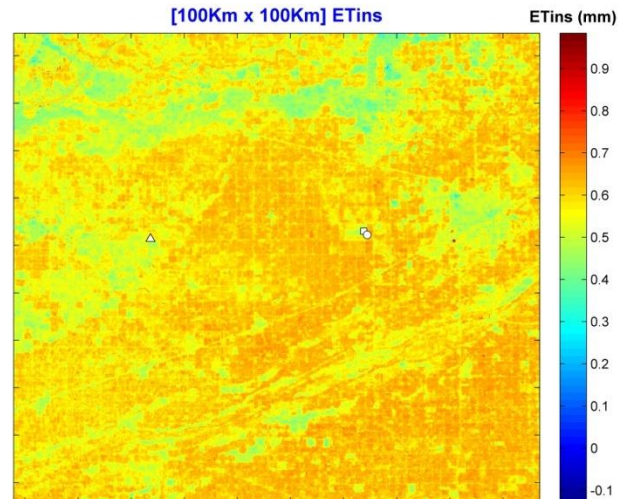
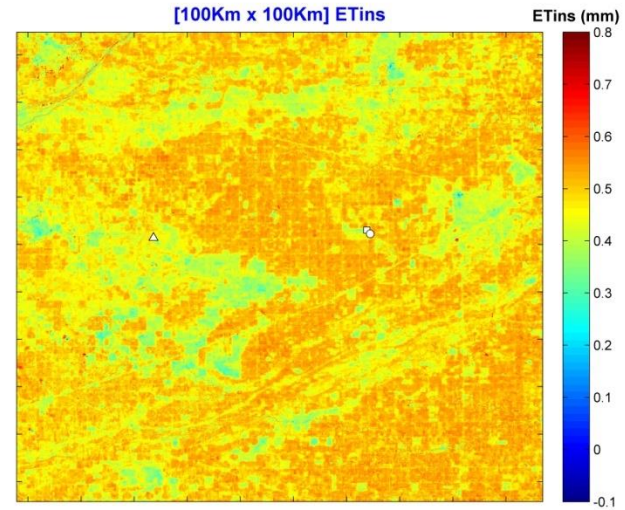


Midday Instantaneous ET as an Average of Daily ET

July 01 2009



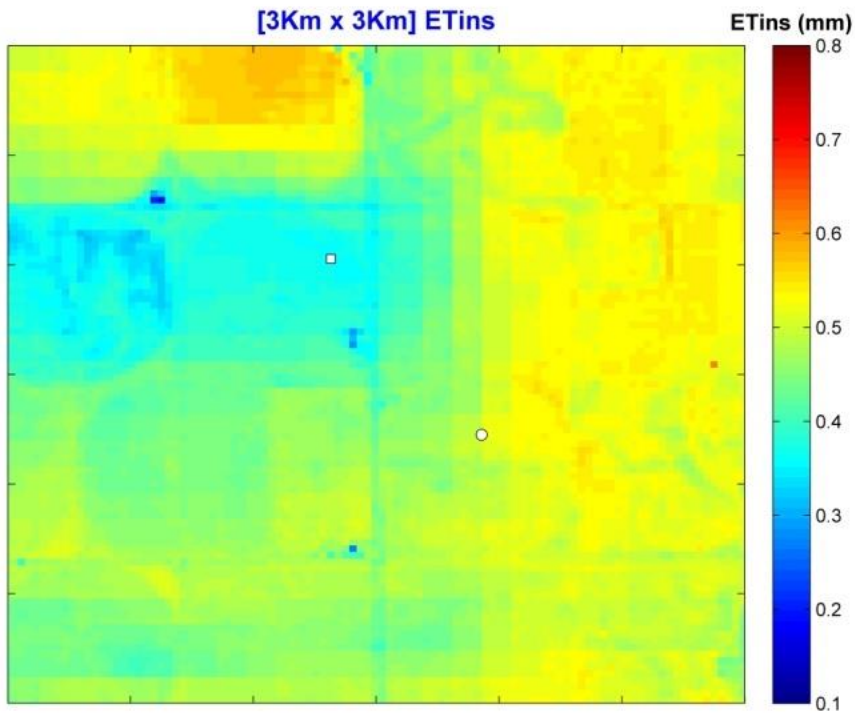
July 17 2009



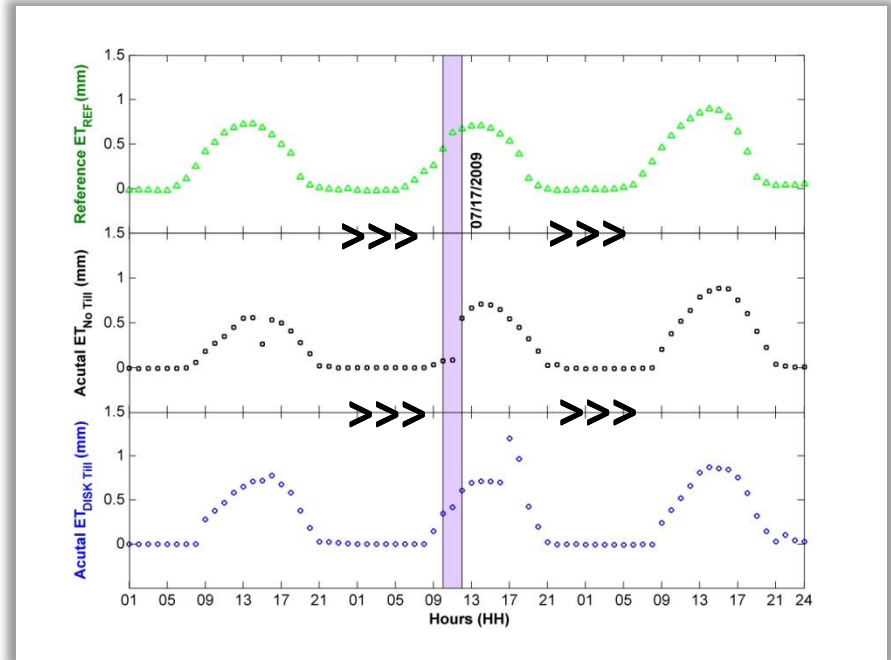
Aug. 02 2009

Hourly ET

[07 17 2009]



Modeled ET at Corn Fields



Observed ET_r , $ET_{NO\ Till}$, $ET_{DISK\ Till}$

Uncertainty in EC Fluxes

raw: after despike (outlier removed).

dr: Double rotations (\bar{v} and \bar{w} = 0).

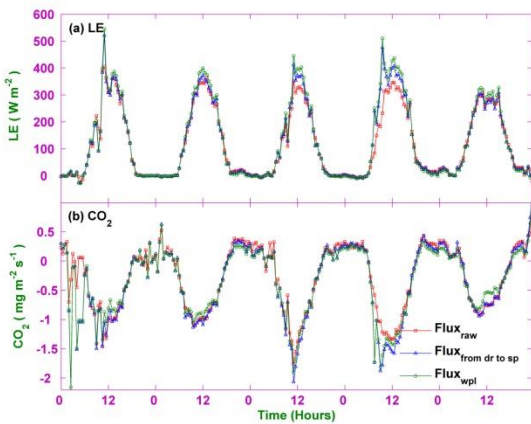
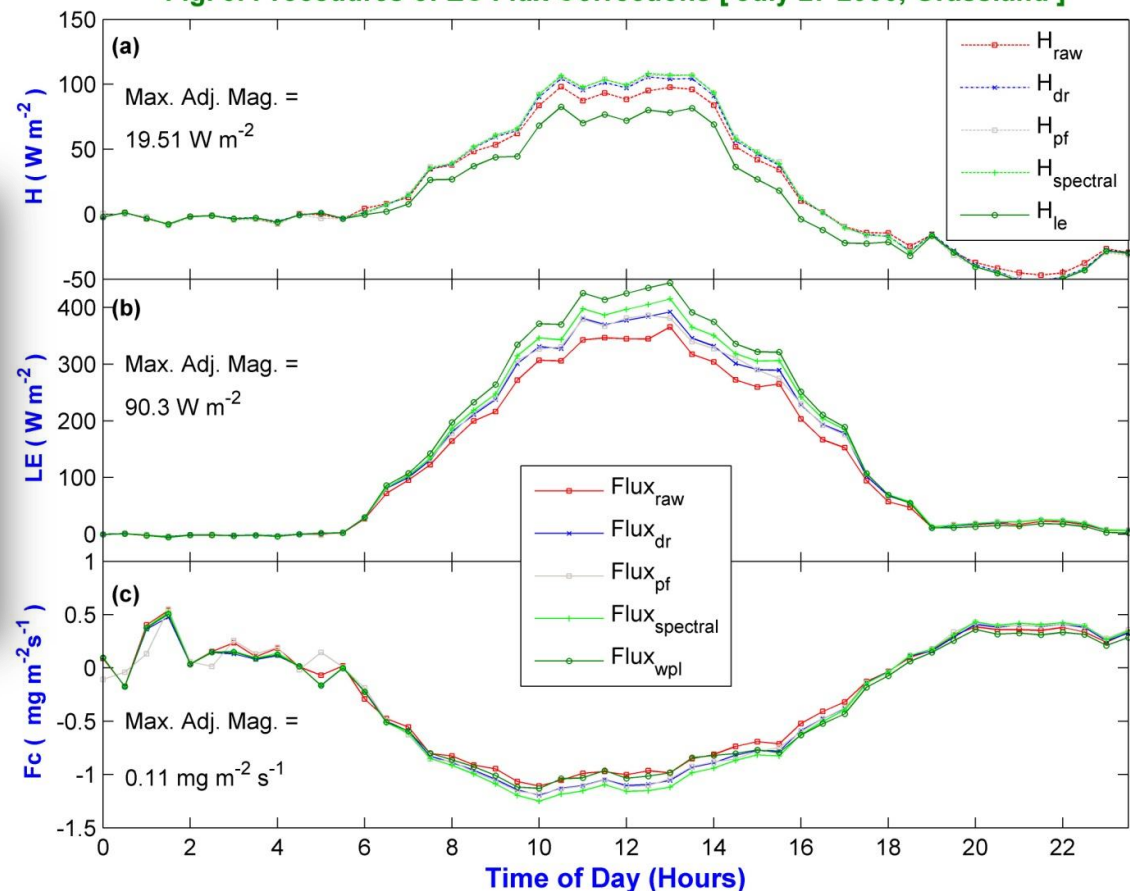
pf: Planar-fit method for rotation (5d).

spectral: low and high freq. loss.

wpl: Web correction (H and LE)

H_{le} : Corrected H only by the LE.

Fig. 3. Procedures of EC Flux Corrections [July 27 2006, Grassland]



Aug. 1-5, 2006. Grassland